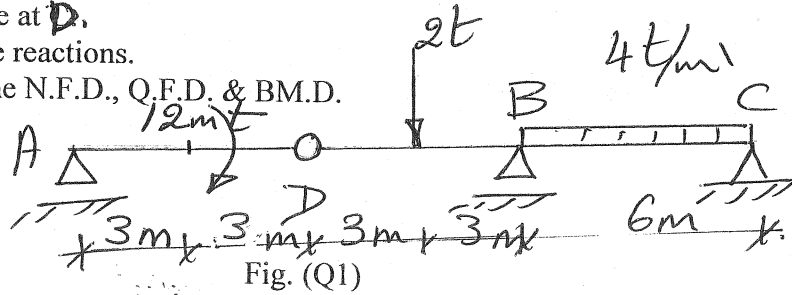


Q1

For the shown beam:

1. Separate at D.
2. Find the reactions.
3. Draw the N.F.D., Q.F.D. & B.M.D.



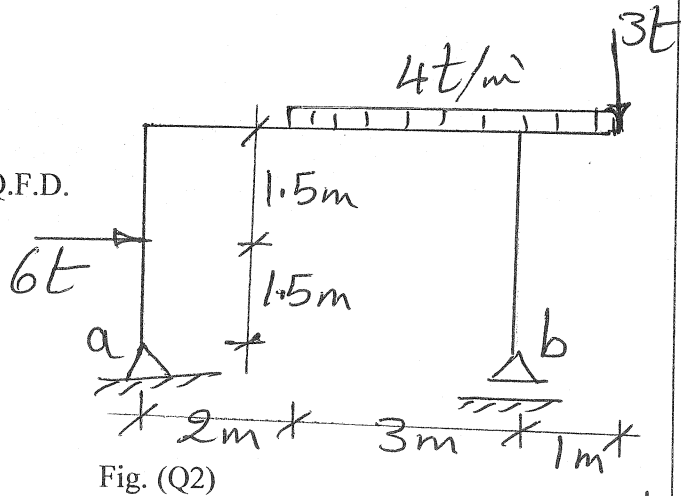
ILO's

- [a2] [2 marks]
- [a2] [2 marks]
- [a2,b3,c2] [4 marks]

Q2

For the shown Frame:

1. Find the reactions.
2. Draw the N.F.D., Q.F.D.
3. Draw B.M.D.



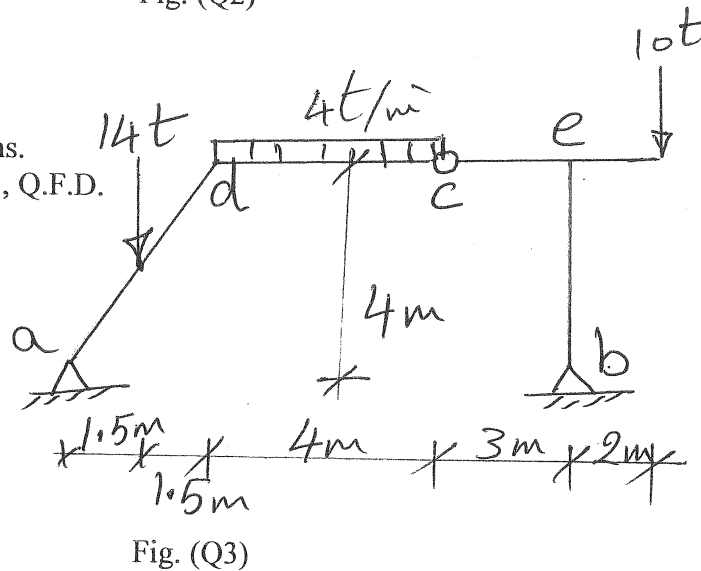
[Total 8]

- [a2] [2 marks]
- [a2,b3,c2] [4 marks]
- [a2,b3,c2] [4 marks]

Q3

For the shown Frame:

4. Find the reactions.
5. Draw the N.F.D., Q.F.D.
6. Draw B.M.D.

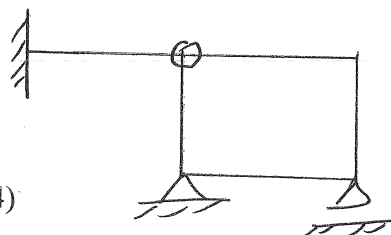


[Total 10]

- [a1] [2 marks]
- [a2,b3,c2] [4 marks]
- [a2,b3,c2] [4 marks]

Q4

Discuss the stability and determinacy of the shown structure:



[b1,c1]

[2 marks]

[Total 2]

[Total 30]

Q1

① $\sum M @ C = 0$

$$2 \times 12 + 2 \times 9 + 4 \times 6 \times 3 - 6 Y_B = 0$$

$$\Rightarrow Y_B = 19.0 t$$

② $\sum F_y = 0$

$$2 + 2 + 4 \times 6 - 19.0 - Y_C = 0$$

$$\Rightarrow Y_C = 9.0 t$$

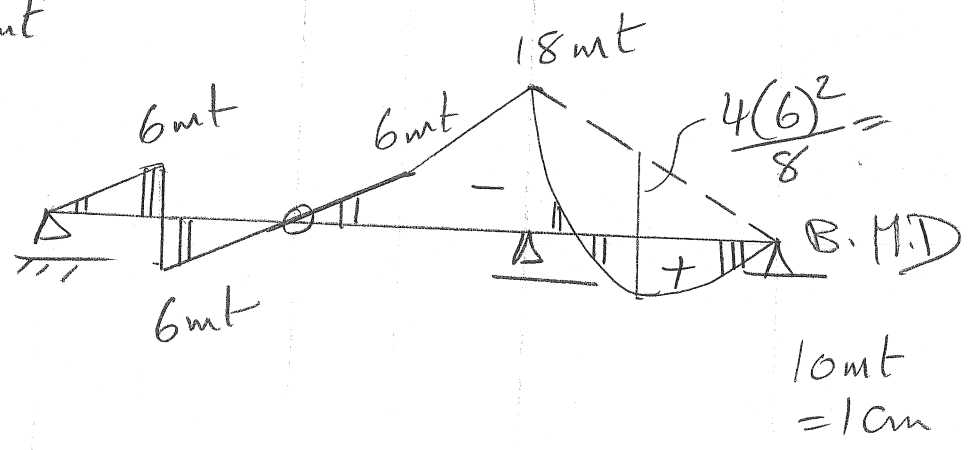
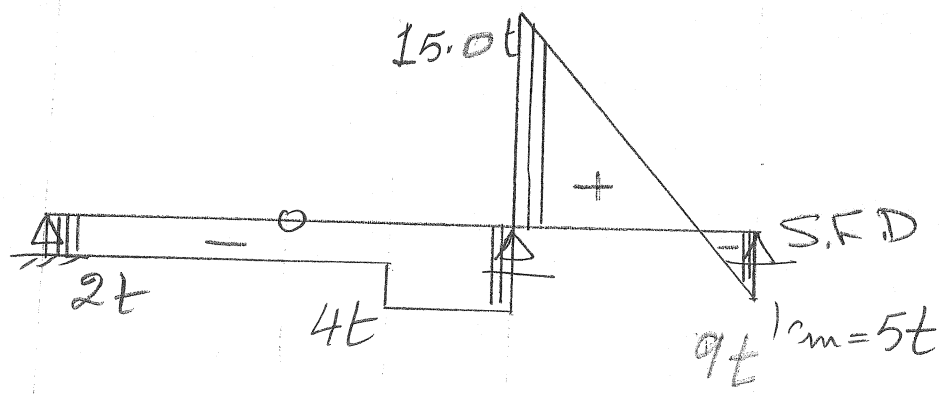
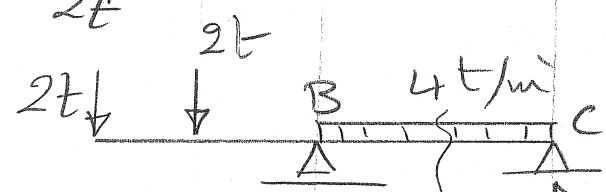
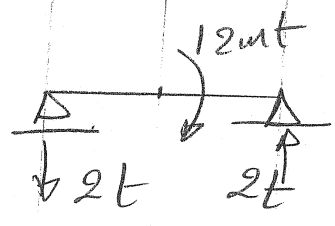
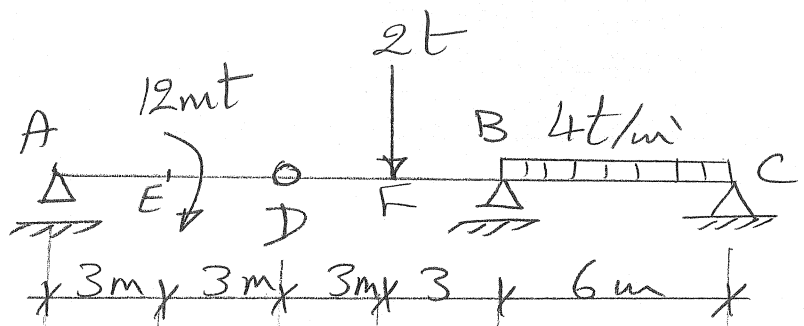
$$M_E = -2 \times 3 = -6 tm$$

6ft

$$M_{ER} = -6 + 12 = +6 mt$$

$$M_F = -2 \times 3 = -6 mt$$

$$M_B = -2 \times 6 - 2 \times 3 = -18 mt$$



Q2

$\sum M @ a = 0$

$$6 \times 1.5 + 4 \times 4 \times 4 + 3 \times 6 - 5 Y_b = 0$$

$$\therefore Y_b = 18.2 t$$

$\sum F_y = 0$

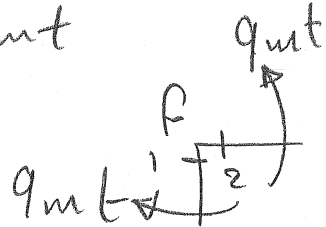
$$\therefore Y_a + 18.2 - 4 \times 4 - 3 = 0$$

$$\therefore Y_a = 0.8 t$$

$M_c = 6 \times 1.5 = 9 mt$

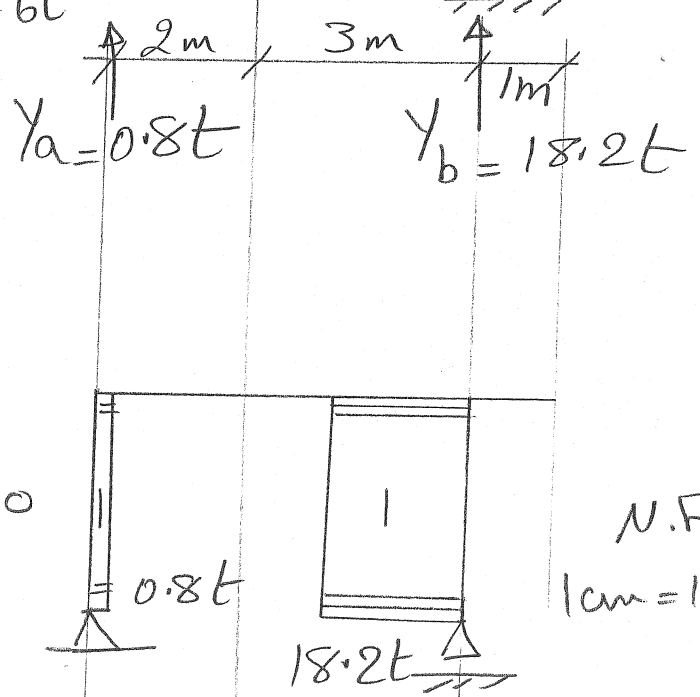
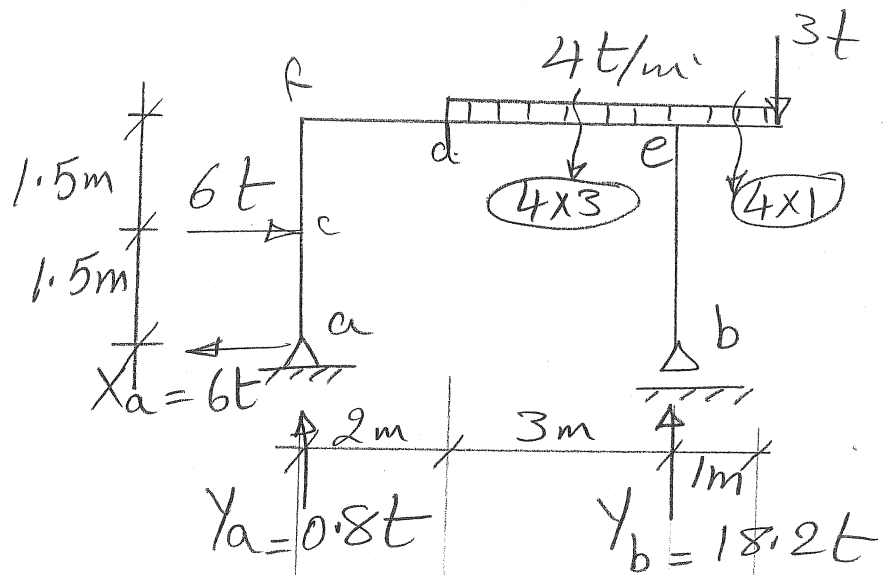
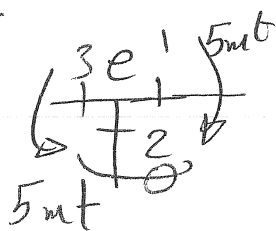
$M_{F_1} = 6 \times 3 - 6 \times 1.5 = 9 mt$

$M_d = 0.8 \times 2 + 6 \times 3 - 6 \times 1.5 = 10.6 mt$

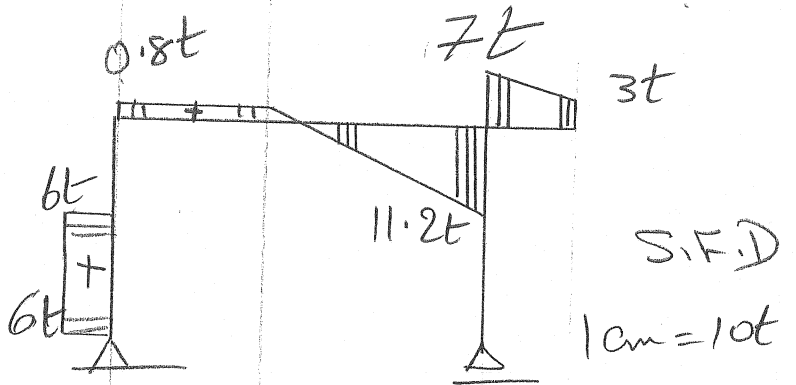


$M_{e_1} = -3 \times 1 - 4 \times 1 \times 0.5$

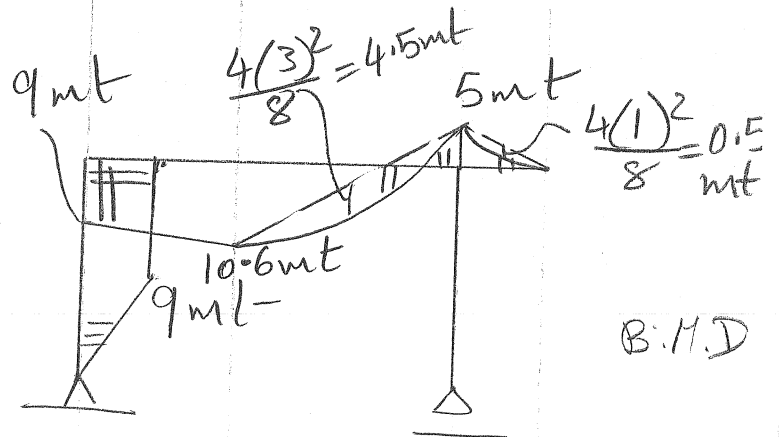
$M_{e_1} = -5 mt$



N.F.D.
1cm = 10t



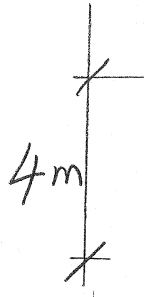
S.F.D.
1cm = 10t



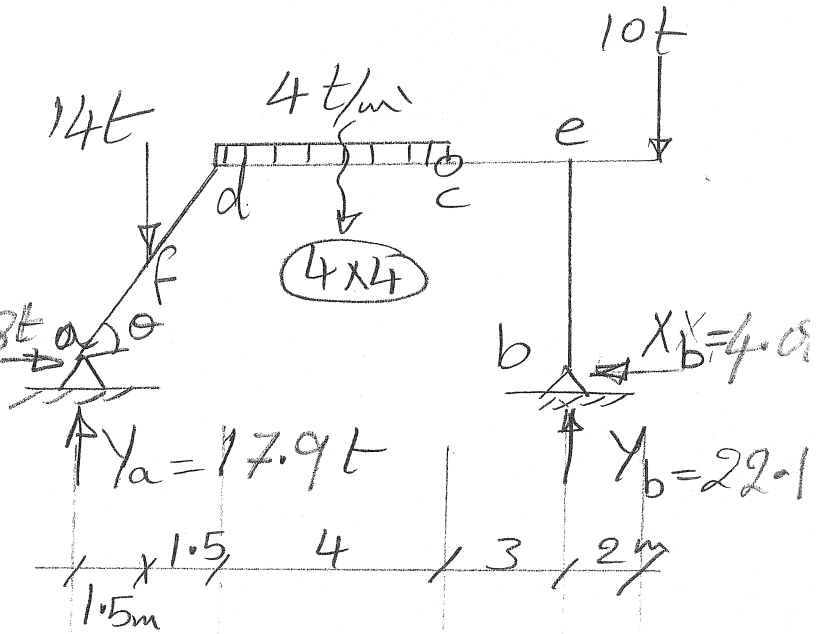
B.M.D

Q3

$\tan \theta = \frac{4}{3}$
 $\sin \theta = 0.8$
 $\cos \theta = 0.6$



$X_a = 4.08t$



① $\sum M @ a = 0$

$14 \times 1.5 + 4 \times 4 \times 5$
 $- 10 Y_b + 10 \times 12 = 0$

$\therefore Y_b = 22.1$

② $\sum F_y = 0$

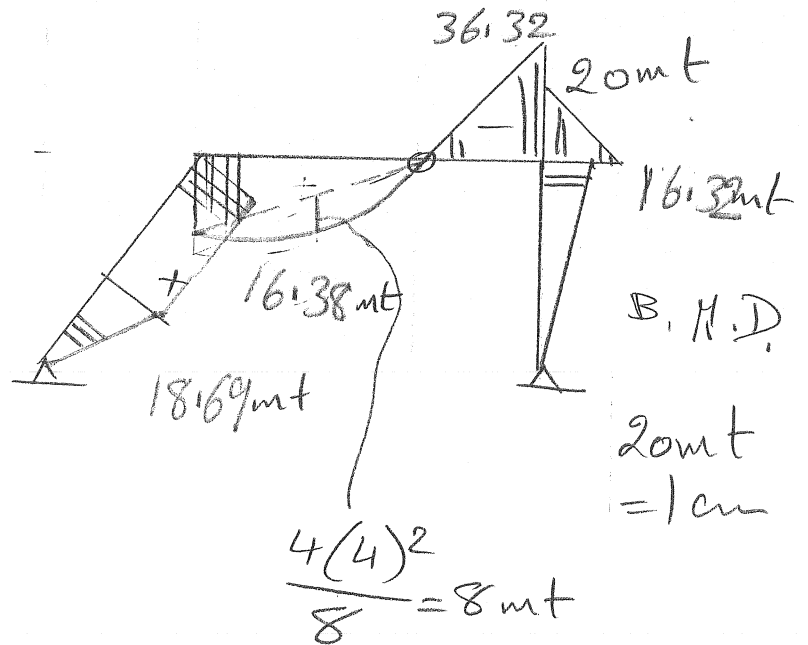
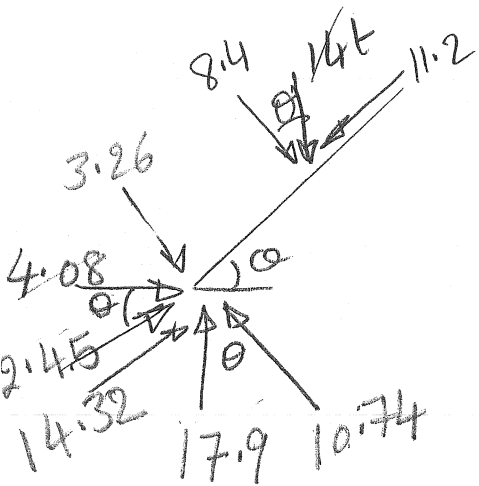
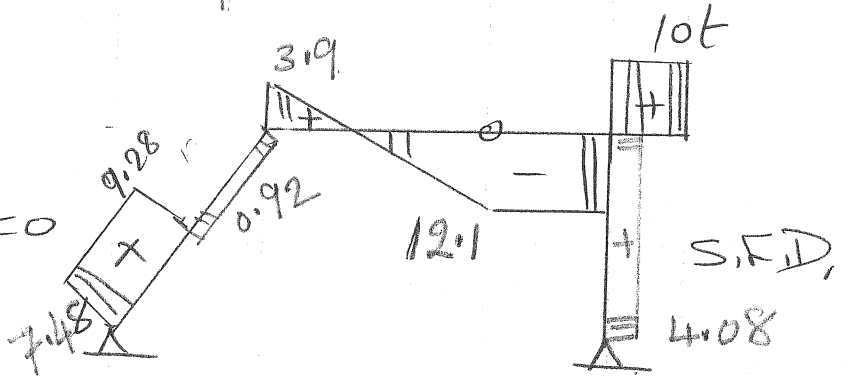
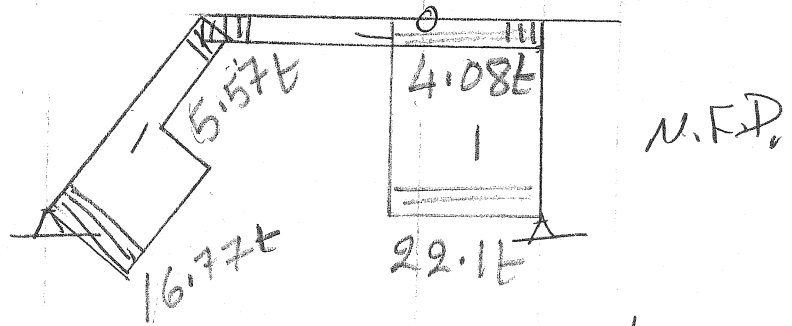
$-14 - 4 \times 4 - 10 + Y_a + Y_b = 0$

$\therefore Y_a = 17.9t$

③ $\sum M_{CR} = 0$

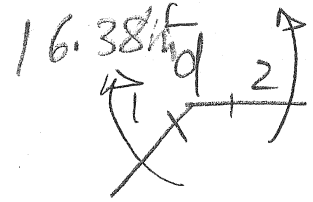
$10 \times 5 + 4 X_b - 22.1 \times 3 = 0$

$\therefore X_b = 4.08$



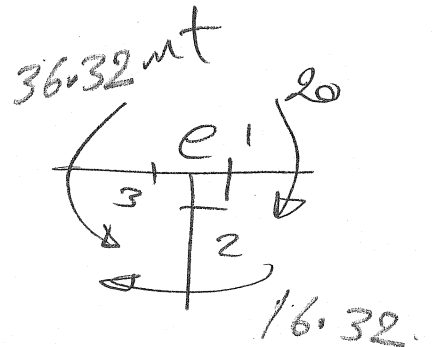
$$M_f = 17.9 \times 1.5 - 4.08 \times 2$$

$$= 18.69 \text{ mt}$$



$$M_{e_1} = -10 \times 2 = -20 \text{ mt}$$

$$M_{e_2} = -4.08 \times 4 = -16.32 \text{ mt}$$



$$M_{d_1} = -4.08 \times 4 - 14 \times 1.5 + 17.9 \times 3$$

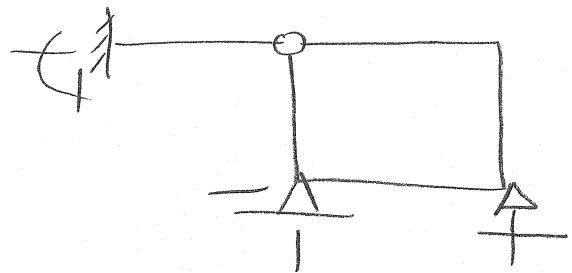
$$= 16.38 \text{ mt}$$

Q4

$$u = 6 + 3 = 9$$

$$E = 3 + (3 - 1) = 5$$

\therefore Stable & 4 times st. indep.



Higher Technological Institute
10th Ramadan City
(6th October Branch)

Department of Civil Engineering

Course : Theory of Structures(2) (CT 112)
Examiner: Dr.Manal Kamal Zaki

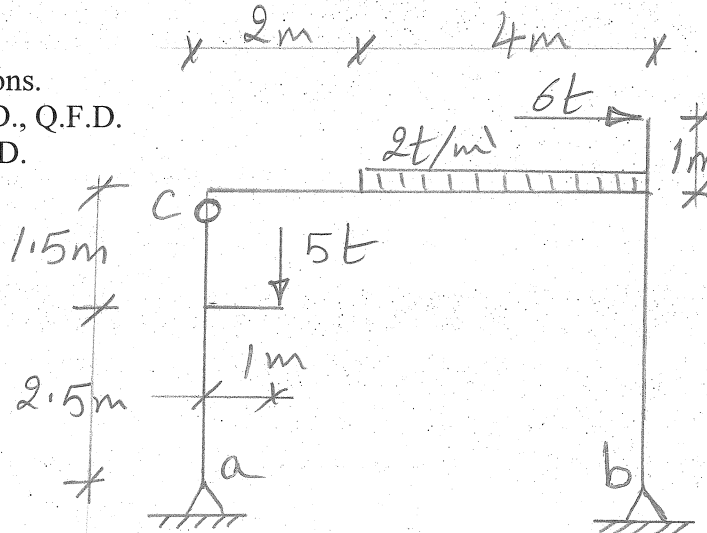
Term : Sept.-Oct. 2017-2018
Time : 90 min

Final exam

Question 1 {16 Marks}

For the shown frame:

1. Find the reactions.
2. Draw the N.F.D., Q.F.D.
3. Draw the B.M.D.



ILO's

[a2]

[4 marks]

[a2,b3,c2]

[8 marks]

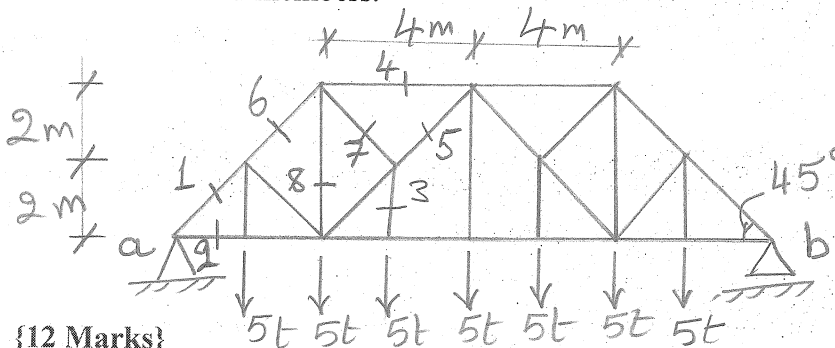
[a2,b3,c2]

[4 marks]

Question 2 {12 Marks}

For the shown truss:

1. Find the reactions.
2. Find the normal forces in the other marked members.



[a2]

[2 marks]

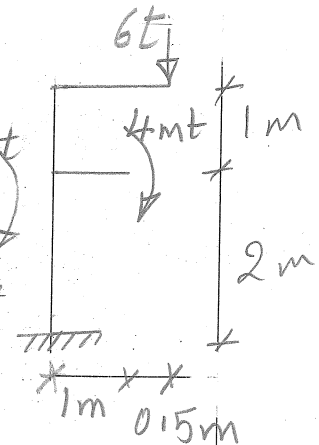
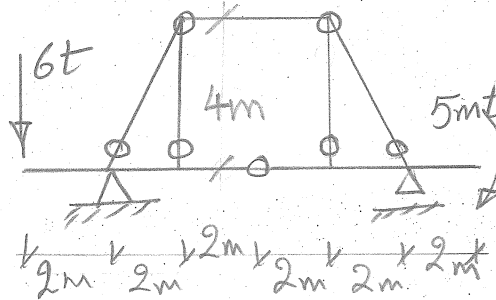
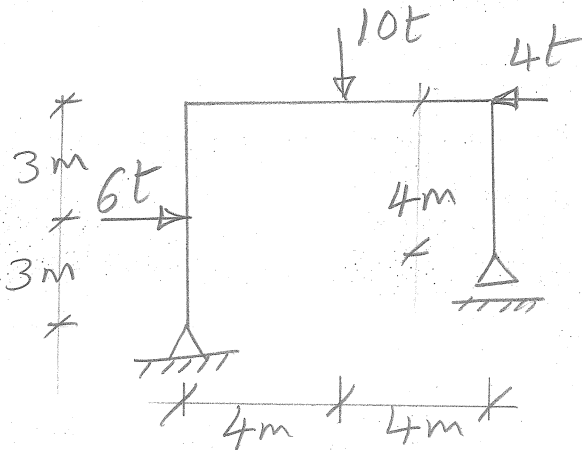
[a3,b3,c3]

[8 marks]

Question 3 {12 Marks}

For the shown structures:

1. Find the forces in the link members.
2. And draw the B.M.D. only.



[a2,a4,c4]

[12 marks]

Examination committee: 1-Name *Dr. Manal Zaki*
 2-Name *Ahmed Alagiz*

Signature *Manal*
 Signature *Ahmed*

Q1

$$\sum M @ c \text{ left} = 0$$

$$\therefore 5 \times 1 - 4X_a = 0$$

$$\therefore X_a = 1.25t$$

$$\sum F_x = 0$$

$$\therefore X_b - 6 - 1.25 = 0$$

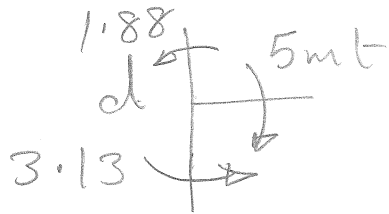
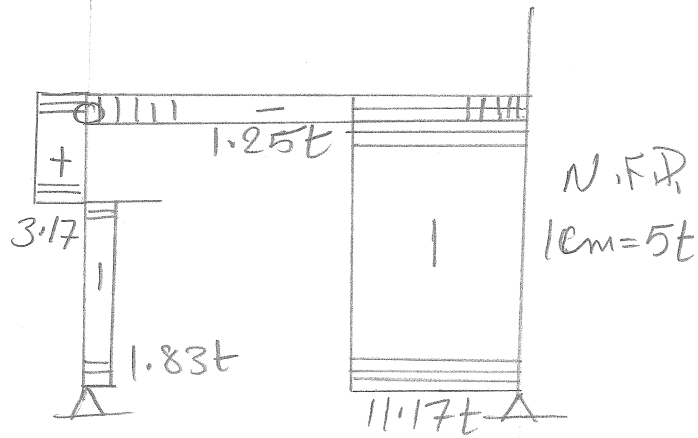
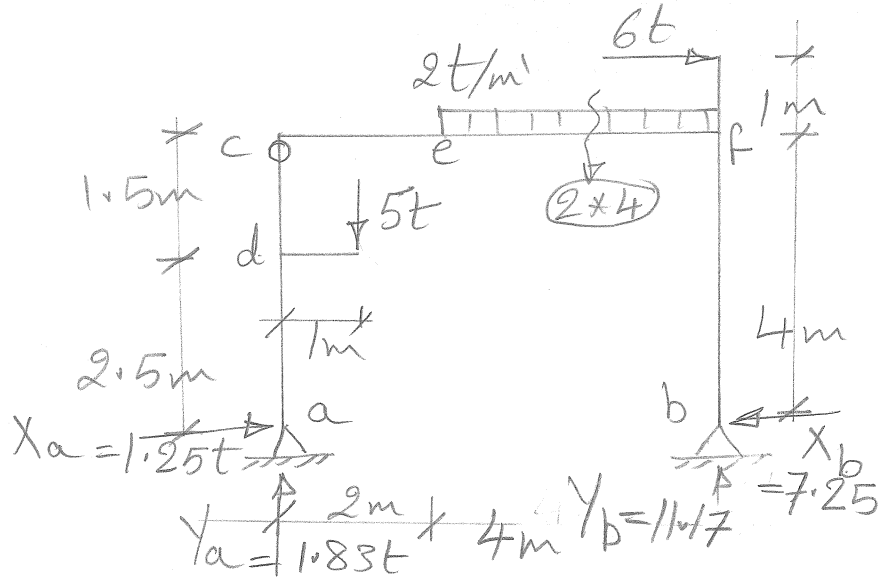
$$\therefore X_b = 7.25t$$

$$\sum M @ a = 0$$

$$\therefore 5 \times 1 + 2 \times 4 \times 4$$

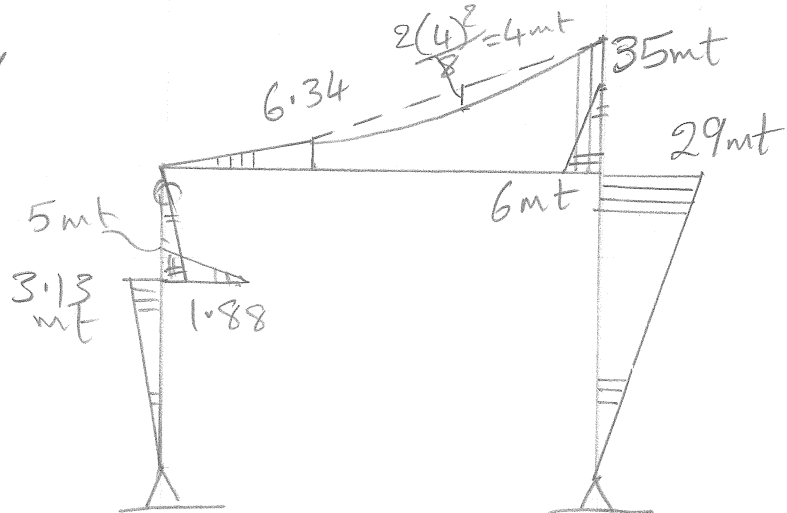
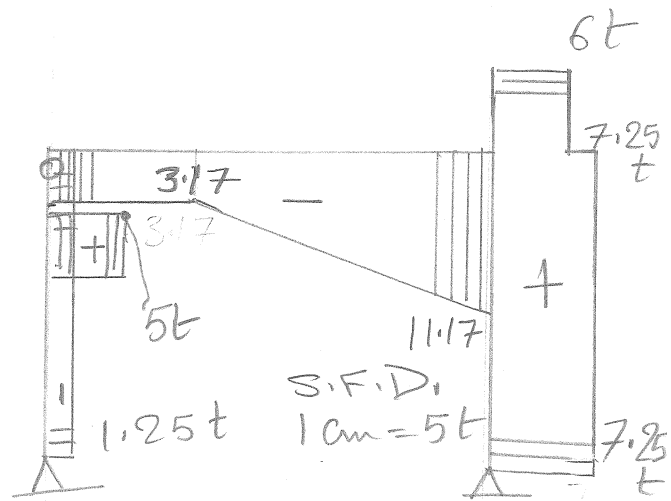
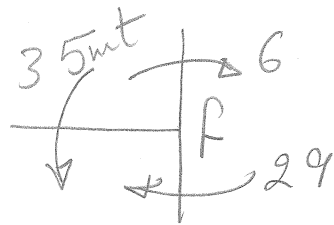
$$+ 6 \times 5 - 6Y_b = 0$$

$$\therefore Y_b = 11.17t$$

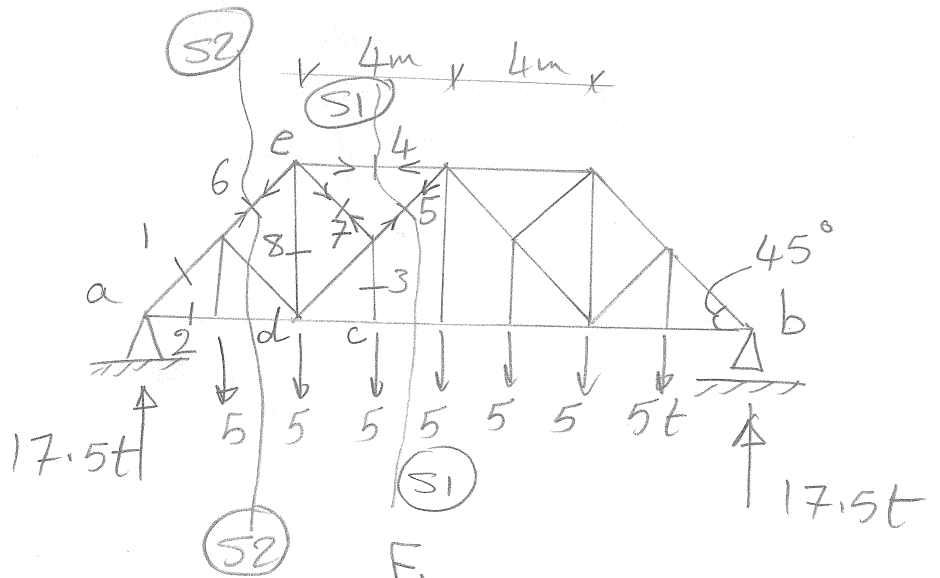


$$M_e = 1.83 \times 2 - 1.25 \times 4 - 5 \times 1$$

$$= -6.34 \text{ mt}$$



Q2

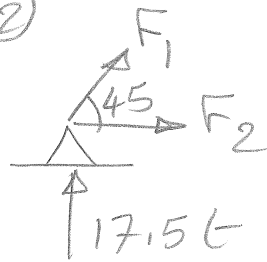


Joint a

$$\sum F_y = 0$$

$$\therefore 17.5 + F_1 \sin 45 = 0$$

$$\therefore \boxed{F_1 = -24.75t} \text{ comp.}$$



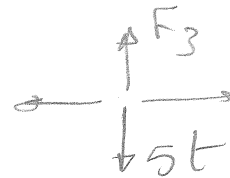
$$\sum F_x = 0$$

$$\therefore F_2 + F_1 \cos 45 = 0$$

$$\therefore \boxed{F_2 = +17.5t} \text{ tens.}$$

Joint c

$$\boxed{F_3 = +5t} \text{ tens.}$$



Section S1-S1

$$\textcircled{1} \sum M @ d \text{ left} = 0$$

$$17.5 \times 4 + 4F_4 + 5 \times 2 - 5 \times 2 = 0$$

$$\therefore \boxed{F_4 = -17.5t} \text{ comp}$$

$$\textcircled{2} \sum F_{y \text{ left}} = 0$$

$$\therefore 17.5 - 3 \times 5 + F_5 \cos 45 = 0 \therefore \boxed{F_5 = -3.54t} \text{ Comp}$$

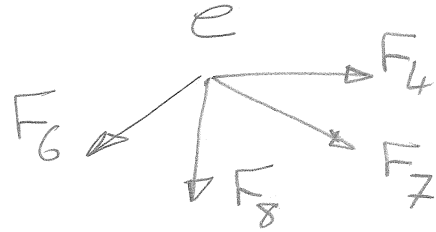
Section S2-S2

$$\sum M @ d \text{ left} = 0$$

$$17.5 \times 4 - 5 \times 2 + F_6 * 2\sqrt{2} = 0 \therefore \boxed{F_6 = -21.21t} \text{ Comp}$$

Joint e:

$$\textcircled{1} \sum F_x = 0$$



$$\therefore -F_6 \sin 45 + F_4 + F_7 \cos 45 = 0$$

$$\therefore -(-21.21) \sin 45 + (-17.5) + F_7 \cos 45 = 0$$

$$\therefore \boxed{F_7 = +3.54 \text{ t}} \text{ tens.}$$

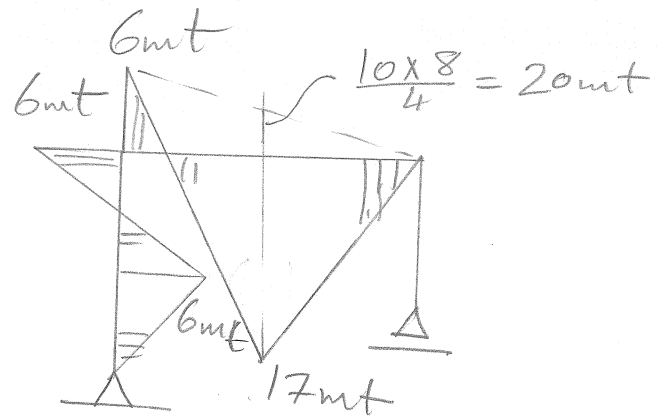
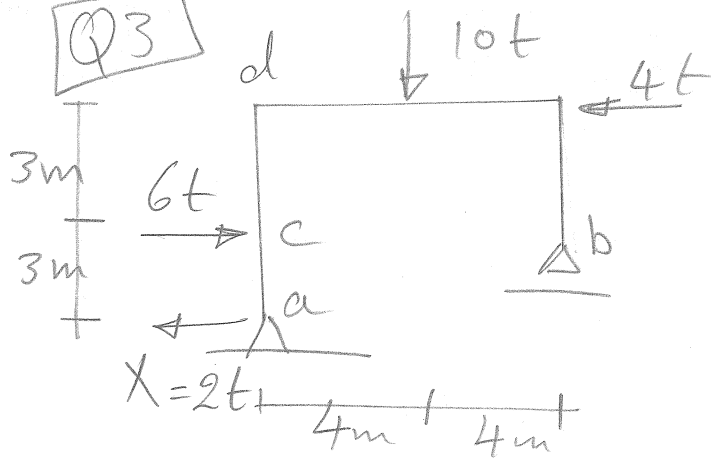
$$\textcircled{2} \sum F_y = 0$$

$$\therefore F_8 + F_7 \sin 45 + F_6 \sin 45 = 0$$

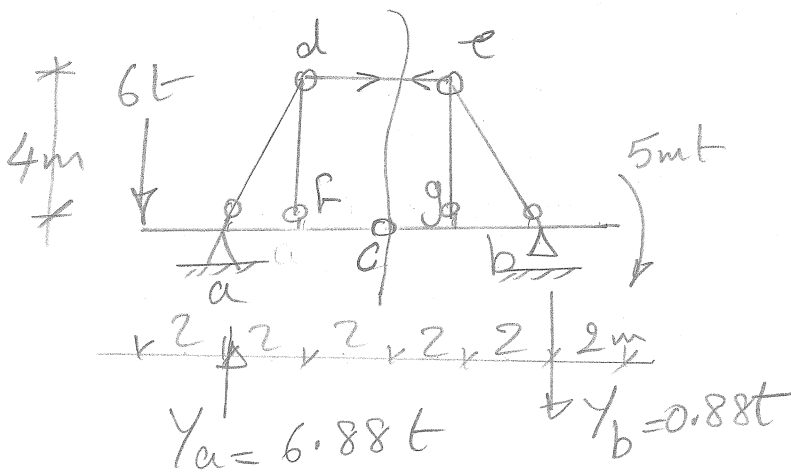
$$\therefore F_8 + 3.54 \sin 45 - 21.21 \sin 45 = 0$$

$$\therefore \boxed{F_8 = +12.50 \text{ t}}$$

Q3



$$M_d = 2 \times 6 - 6 \times 3 = -6mt$$



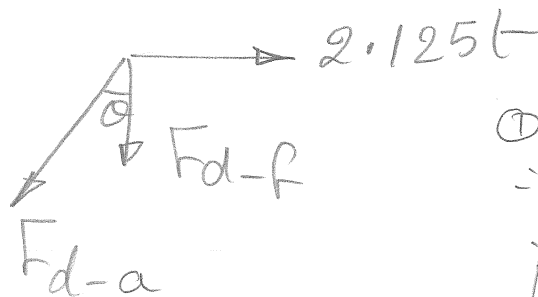
$$\sum M @ b = 0$$

$$6 \times 6 - 8Y_a - 5 = 0$$

$$\therefore Y_a = 6.88t$$

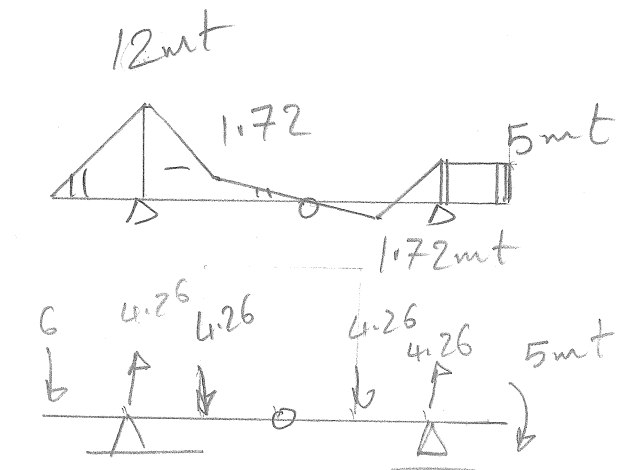
Joint d

$$\tan \theta = \frac{1}{2}$$



$$M_f = -6 \times 4 + 4.26 \times 2 + 6.88 \times 2 = -1.72$$

$$M_g = -5 + 4.26 \times 2 - 0.88 \times 2 = +1.76$$



$$\sum M @ c_{left} = 0$$

$$6 \times 6 - 6.88 \times 4 - F_{d-e} \times 4 = 0$$

$$F_{d-e} = 2.125t \text{ tens.}$$

$$\textcircled{1} \sum F_x = 0$$

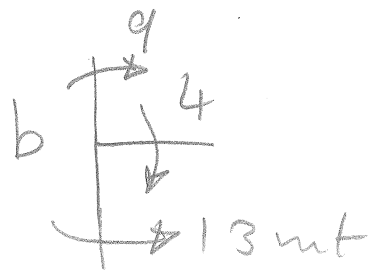
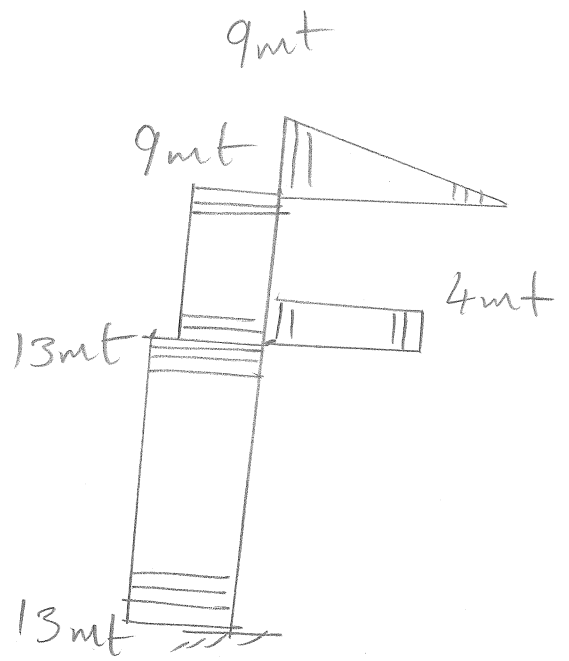
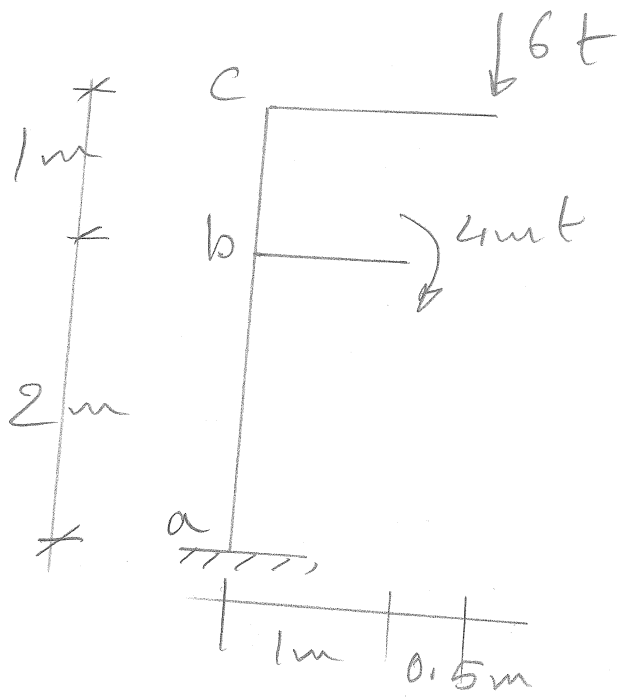
$$\therefore F_{d-a} \sin \theta - 2.125 = 0$$

$$F_{d-a} = 4.76t$$

$$\textcircled{2} \sum F_y = 0$$

$$\therefore F_{d-f} + F_{d-a} \cos \theta = 0$$

$$F_{d-f} = -4.26t$$



Q1

For the shown frame:

1. Find the reactions.
2. Draw the N.F.D., Q.F.D.
3. Draw the B.M.D.

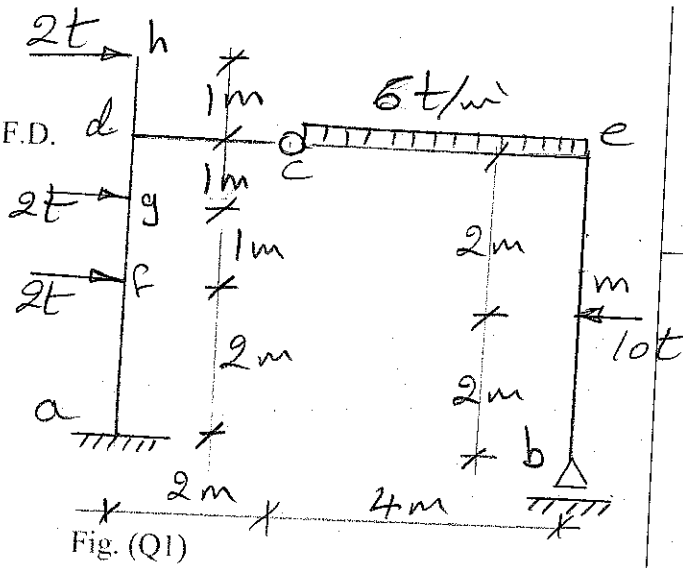


Fig. (Q1)

ILO's

[a2,d1]

[3 marks]

[a2]

[8 marks]

[a2,c1]

[5 marks]

[Total 16]

Q2

For the shown truss:

1. Find the reactions.
2. Find the normal forces in the marked members.

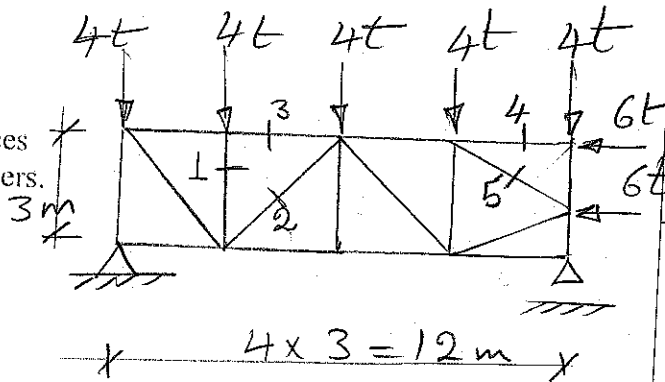


Fig. (Q2)

[a2]

[2 marks]

[a2,c1]

[10 marks]

[Total 12]

Q3

For the shown structures:

1. Find the forces in the link members.
2. And draw the B.M.D. only

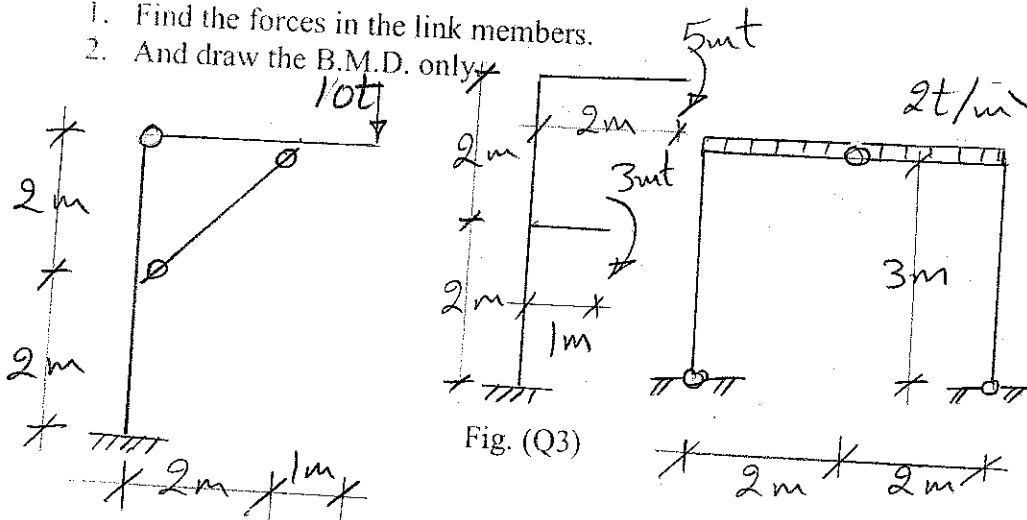


Fig. (Q3)

a2,c1,d1

[12 marks]

[Total 12]

Q1

① $\sum M@c_{right} = 0$

$6 \times 4 \times 2 + 10 \times 2 - Y_b \times 4 = 0$
 $\Rightarrow Y_b = 17t$

② $\sum F_y = 0$

$Y_a + 17 - 6 \times 4 = 0$
 $\Rightarrow Y_a = 7t$

③ $\sum F_x = 0 \rightarrow X_a = 4t$

④ $\sum M@c_{left} = 0$

$7 \times 2 + M_a - 4 \times 4 - 2 \times 2 - 2 \times 1 + 2 \times 1 = 0$
 $M_a = 6mt$

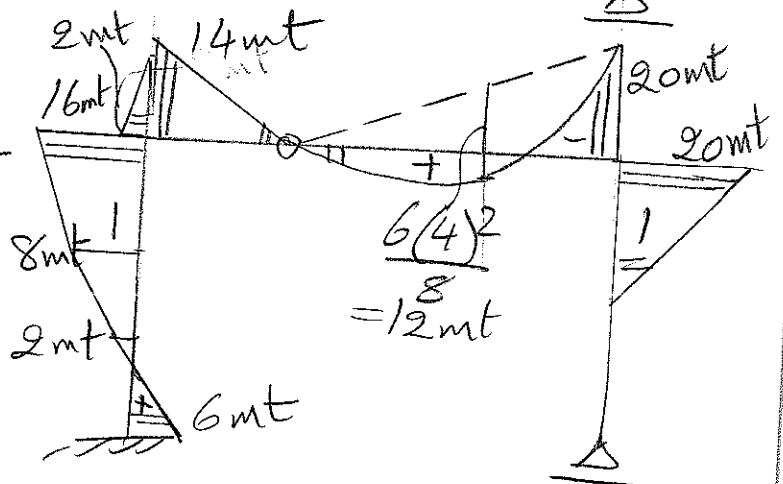
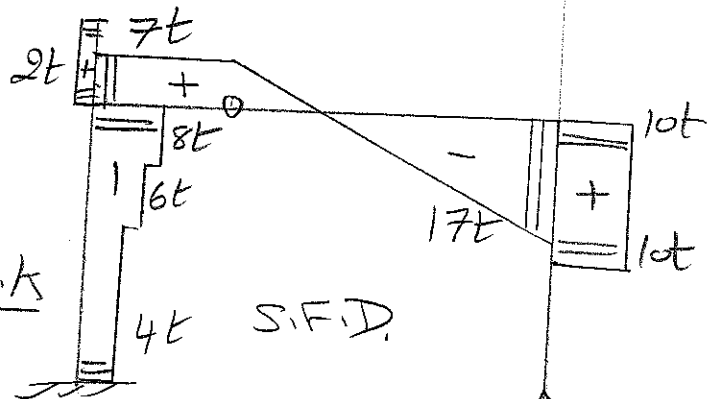
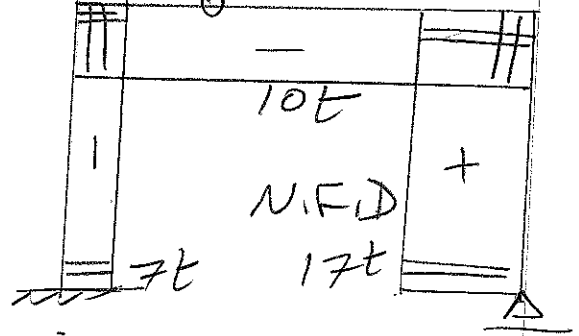
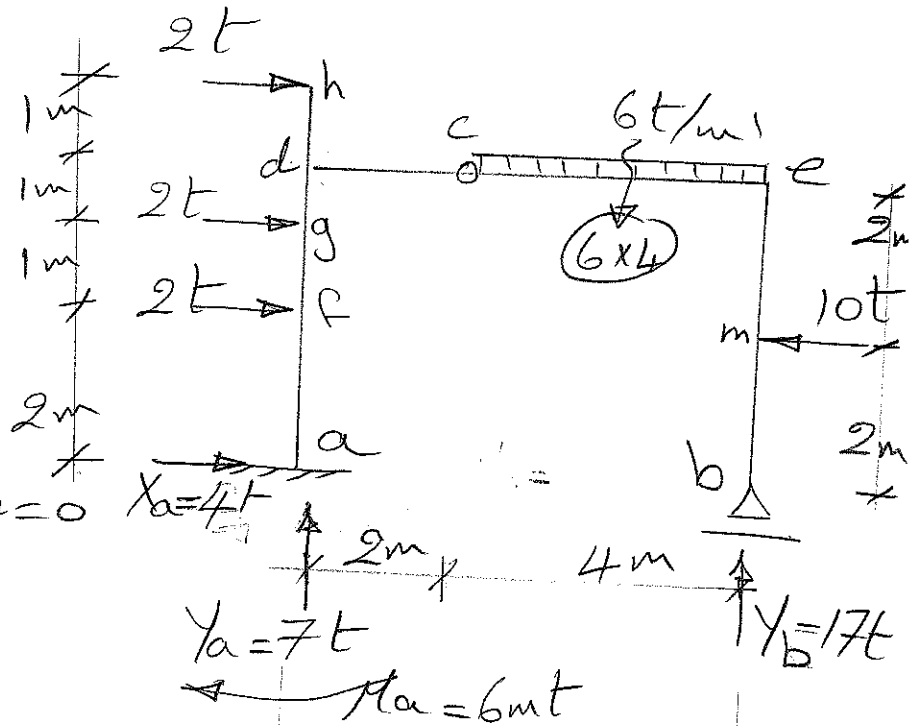
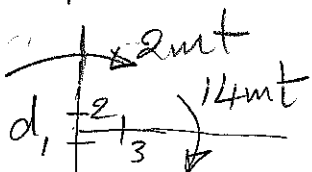
check $\sum M@b = 0$

$10 \times 2 + 6 \times 4 \times 2 - 7 \times 6 - 6 - 2 \times 2 - 2 \times 3 - 2 \times 5 = 0 \text{ o.k.}$

$M_f = 6 - 4 \times 2 = -2tm$

$M_g = 6 - 4 \times 3 - 2 \times 1 = -8mt$

$M_d = 6 - 4 \times 4 - 2 \times 2 - 2 \times 1 = -16mt$



Q2

$$\sum M @ a = 0$$

$$\begin{aligned} &= 4 \times [3 + 6 + 9 + 12] \\ &- 6 [1.5 + 3] - 12 Y_b = 0 \end{aligned}$$

$$\Rightarrow Y_b = 7.75t$$

$$\Rightarrow Y_a = 12.25t$$

Joint g

$$\Rightarrow F_1 = -4t \text{ comp}$$

Section S1-S1

$$\sum F_{y \text{ left}} = 0$$

$$\Rightarrow 12.25 - 4 - 4 + F_2 \cos 45 = 0$$

$$\Rightarrow F_2 = -6.01t \text{ comp}$$

Joint l $\sum F_x = 0$

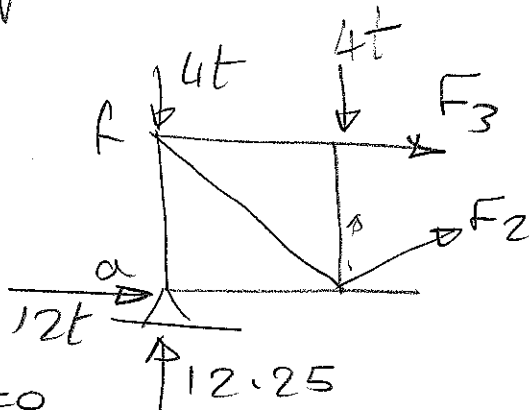
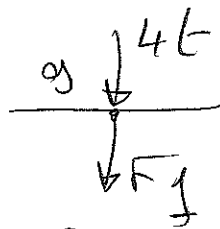
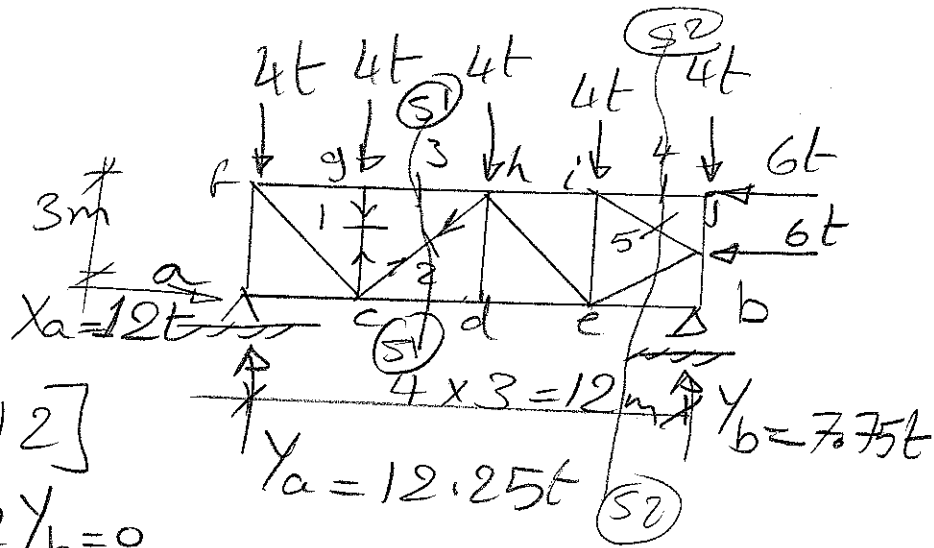
$$\Rightarrow F_4 = -6t \text{ comp}$$

Section S2-S2 $\sum M @ e = 0$

$$\begin{aligned} &3F_4 + 1.5F_5 \cos 0 + 3F_5 \sin 0 \\ &+ 6 \times 1.5 + 6 \times 3 - 4 \times 3 + 7.75 \times 3 = 0 \end{aligned}$$

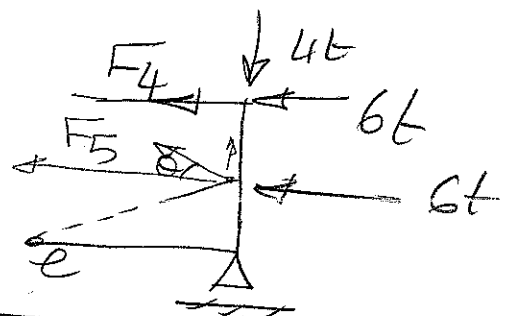
$$20.25 + 2.68F_5 = 0$$

$$\Rightarrow F_5 = -7.55t$$

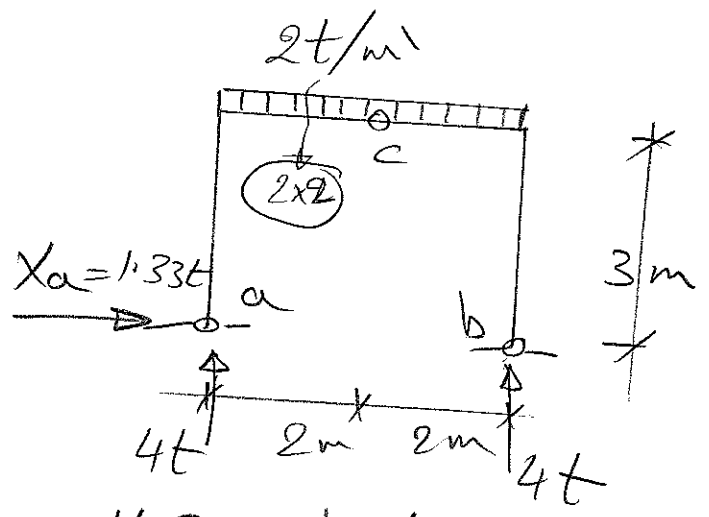
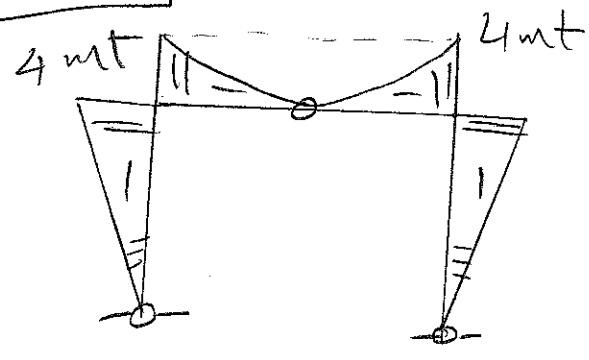


$$\begin{aligned} &\sum M @ c \text{ left} = 0 \\ &(12.25 - 4) \times 3 + 3F_3 = 0 \end{aligned}$$

$$\Rightarrow F_3 = 8.25t \text{ comp}$$



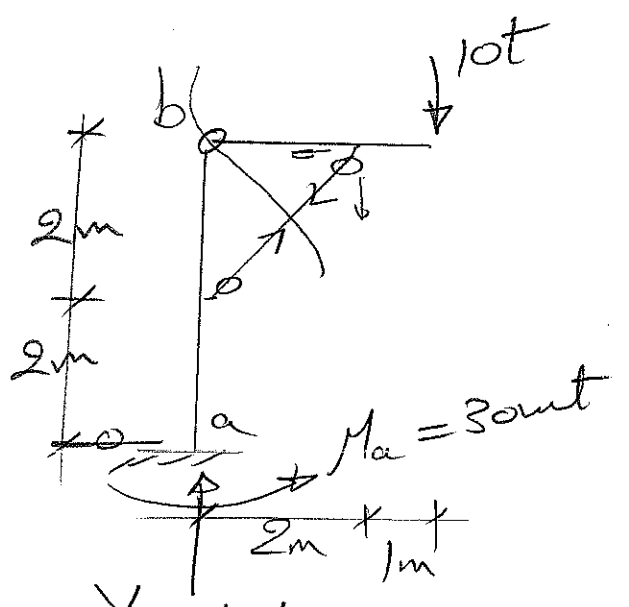
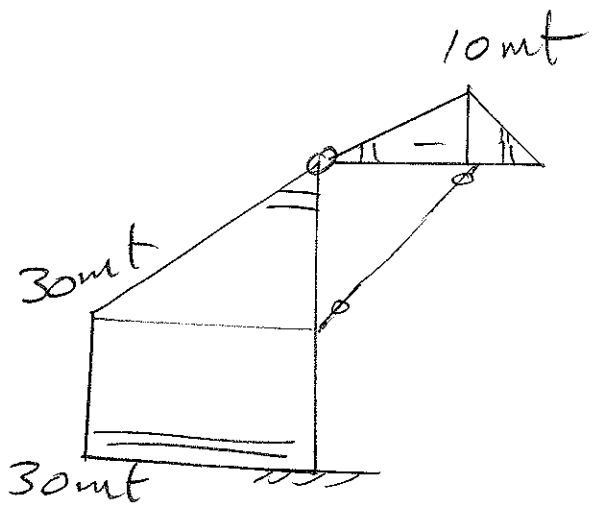
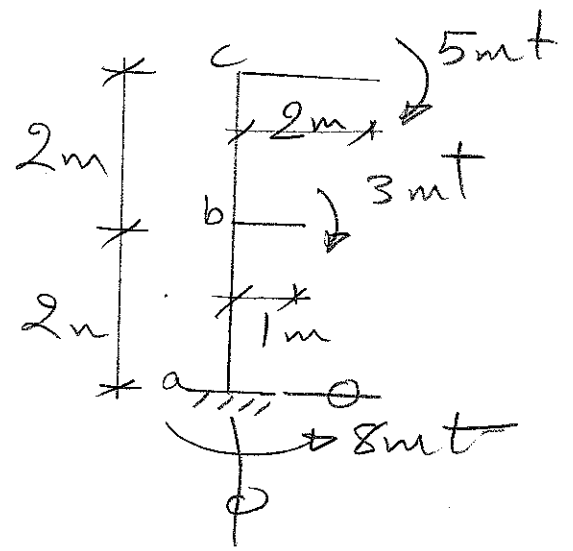
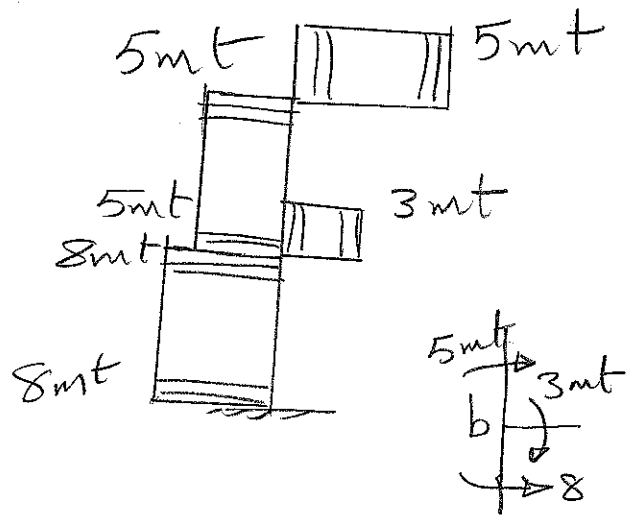
Q3



$$\sum M @ c_{right} = 0$$

$$\Rightarrow 2 \times 2 \times 1 + 3X_a - 4 \times 2 = 0$$

$$\Rightarrow X_a = 1.33t$$



$$\sum M @ b_{right} = 0$$

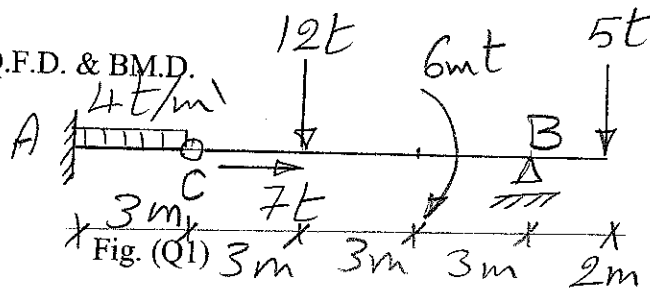
$$10 \times 3 + F \cos 45 \times 2 = 0$$

$$\Rightarrow [F = -21.2t]_{comp}, Y_a = 10t$$

Q1

For the shown beam:

1. Separate at C.
2. Find the reactions.
3. Draw the N.F.D., Q.F.D. & B.M.D.



ILO's

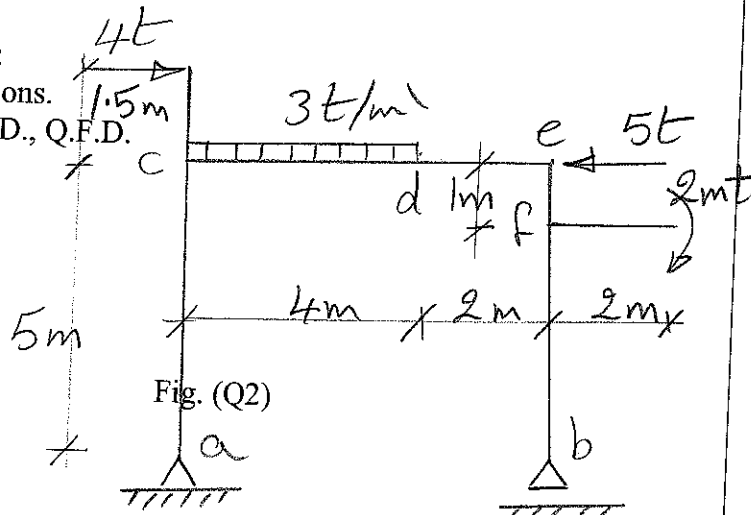
- [a2] [2 marks]
- [a2] [2 marks]
- [a2] [4 marks]

[Total 8]

Q2

For the shown Frame:

1. Find the reactions.
2. Draw the N.F.D., Q.F.D.
3. Draw B.M.D.



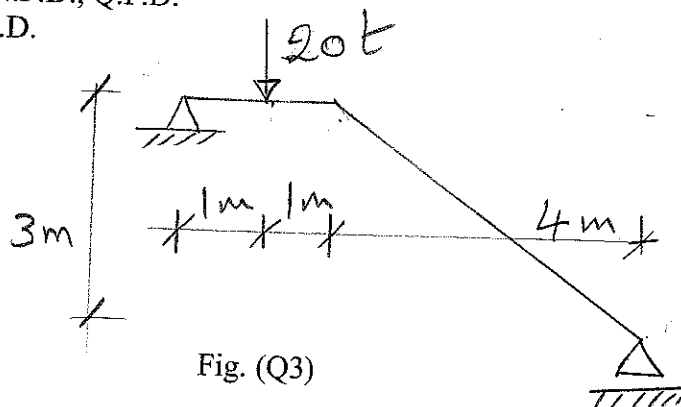
- [a1] [3 marks]
- [a2] [3 marks]
- [a2] [4 marks]

[Total 10]

Q3

For the shown Frame:

4. Find the reactions.
5. Draw the N.F.D., Q.F.D.
6. Draw B.M.D.

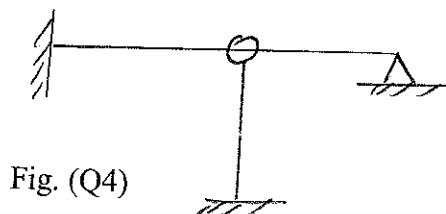


- [a1] [2 marks]
- [a2] [4 marks]
- [a2] [4 marks]

[Total 10]

Q4

Discuss the stability and determinacy of the shown structure:



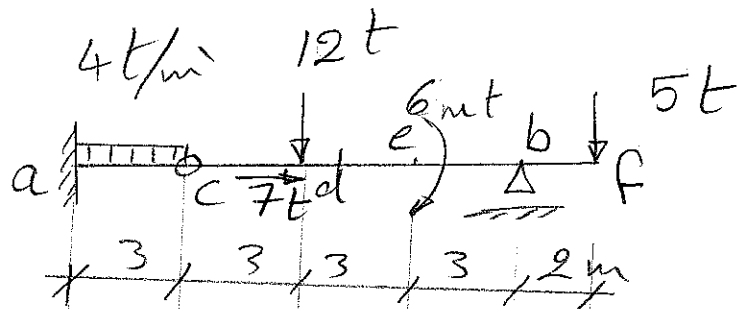
[d1]

[2 marks]

[Total 2]

[Total 30]

Q1



$$\sum M @ c = 0$$

$$12 \times 3 + 6 - 9Y_b + 5 \times 11 = 0$$

$$\therefore Y_b = 10.78 \text{ t}$$

$$\therefore Y_c = 6.22 \text{ t}$$

$$Y_a = 4 \times 3 + 6.22 = 18.22$$

$$\sum M @ a = 0$$

$$\therefore M_a - 4 \times 3 \times 1.5 - 6.22 \times 3 = 0 \quad 18.22 \text{ t}$$

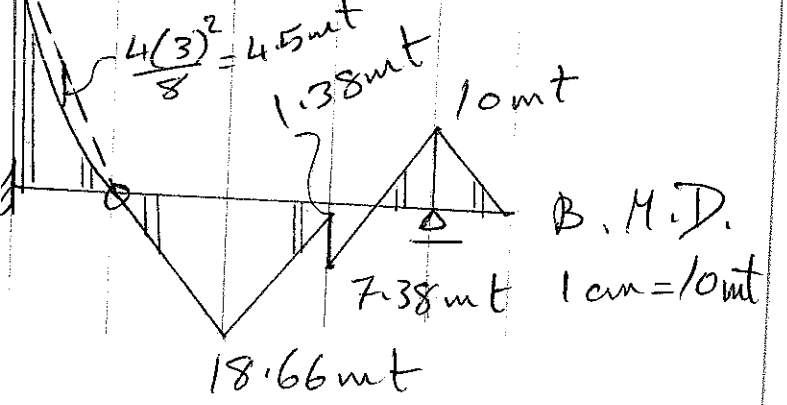
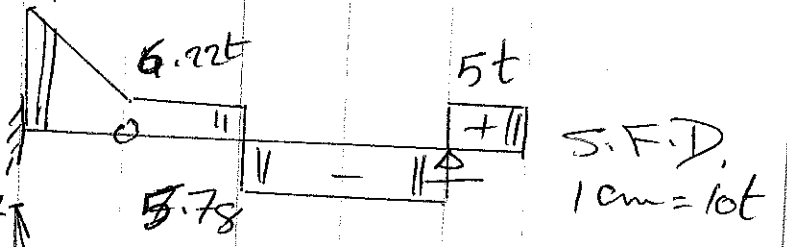
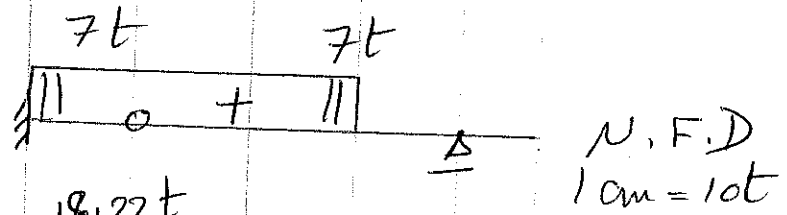
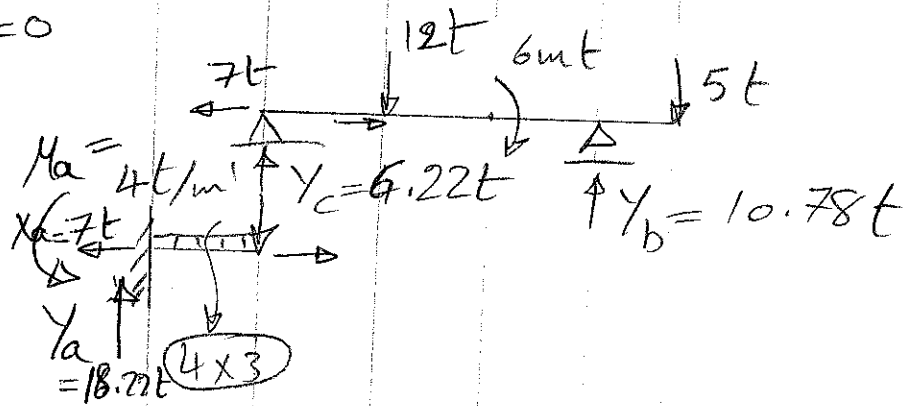
$$\therefore M_a = 36.67 \text{ mt}$$

$$M_b = -5 \times 2 = -10 \text{ mt}$$

$$M_{\text{right}} = -5 \times 5 + 10.78 \times 3 = +7.38$$

$$M_{\text{left}} = +7.38 - 6 = 1.38 \text{ mt}$$

$$M_d = 6.22 \times 3 = 18.66 \text{ mt}$$



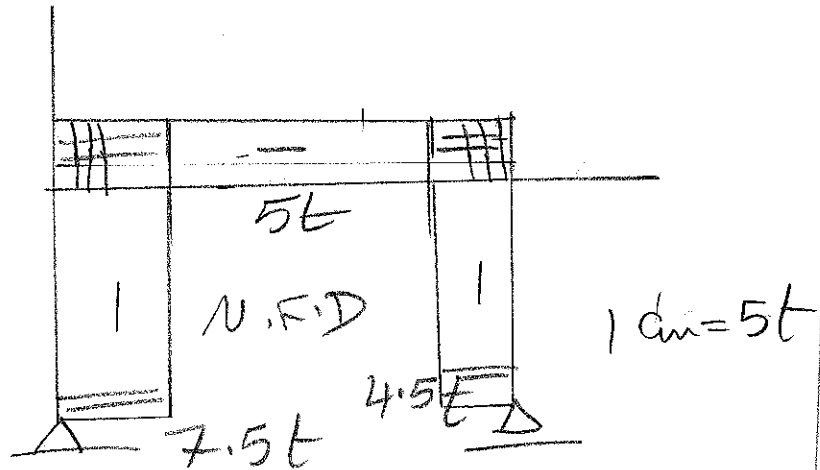
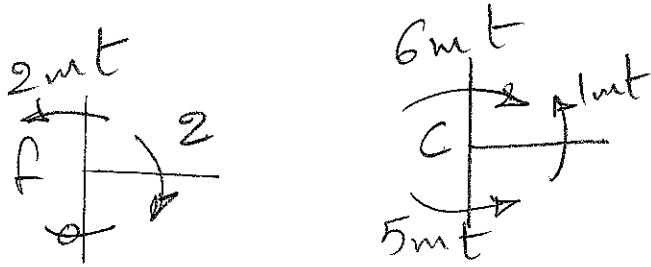
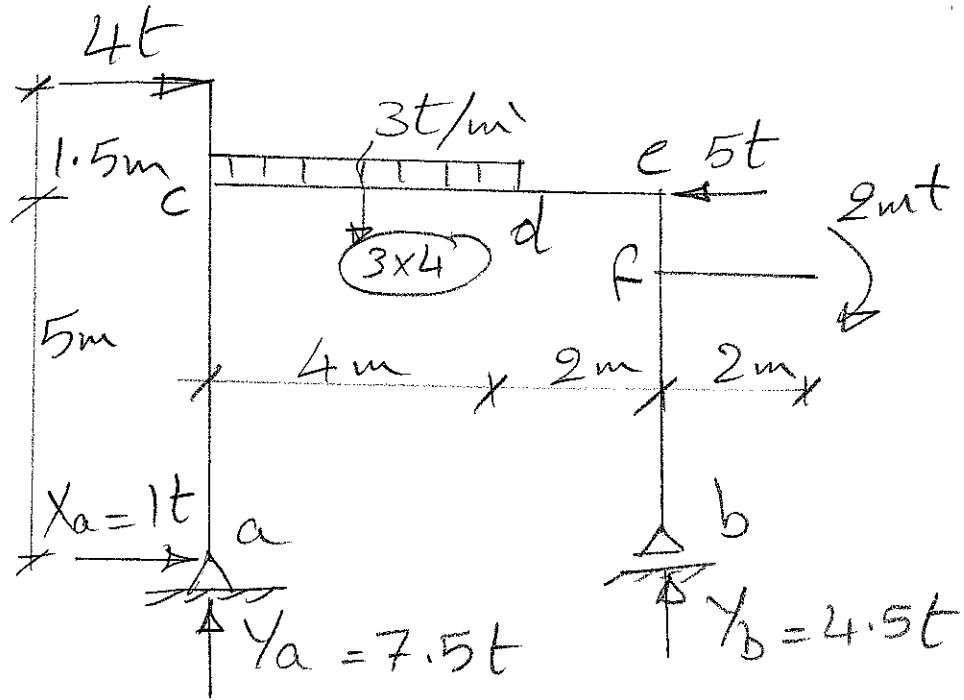
Q2

$$\sum M @ a = 0$$

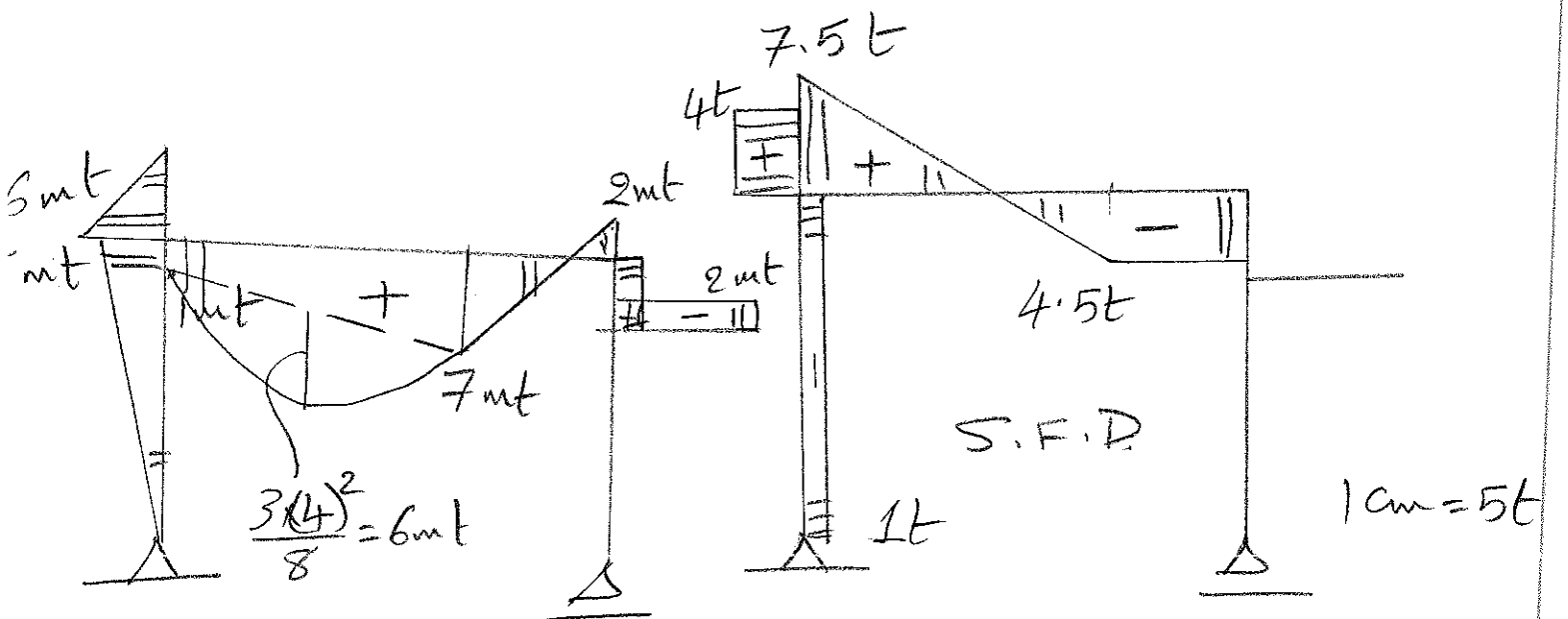
$$4 \times 6 \times 5 + 3 \times 4 \times 2 + 2 - 5 \times 5 - 6 \frac{y_b}{8} = 0$$

$$\Rightarrow y_b = 4.5t$$

$$\Rightarrow y_a = 7.5t$$



$$M_d = 4.5 \times 2 - 2 = 7mt$$



B.M.D
1cm = 5mt

Q3

① $\sum M @ a = 0$

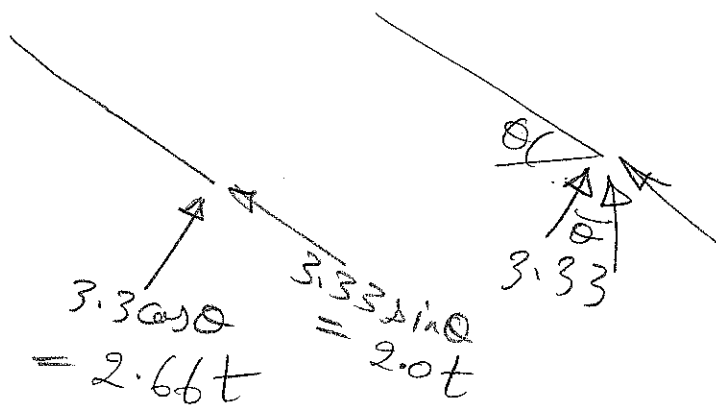
$20 \times 1 - 6Y_b = 0$

$\Rightarrow Y_b = 3.33t$

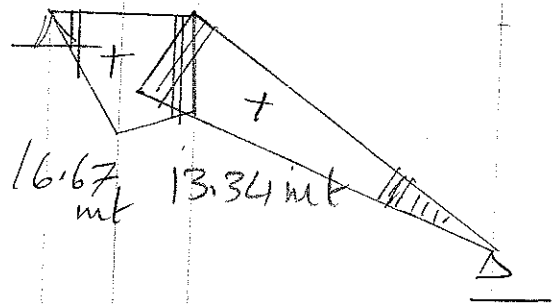
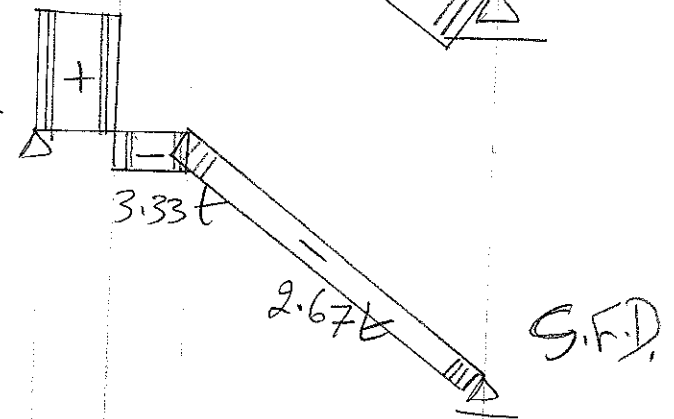
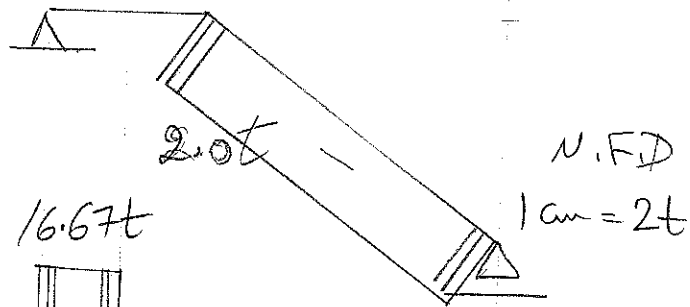
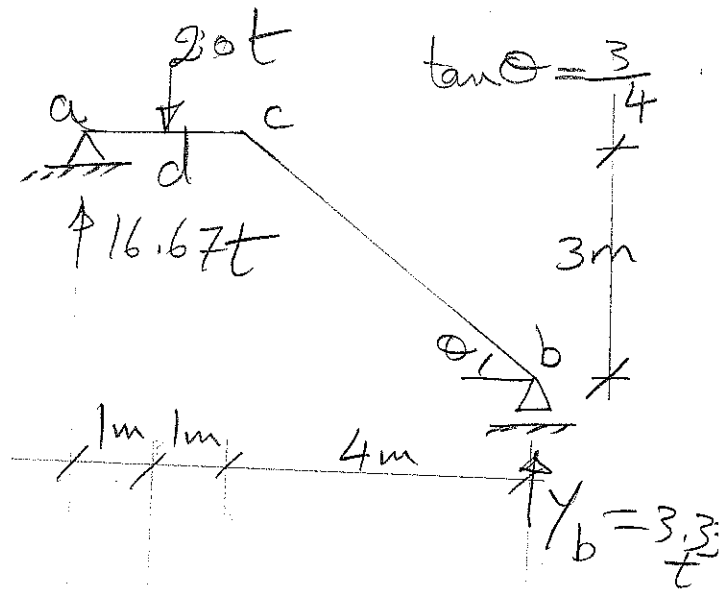
② $\sum F_y = 0$

$Y_a + Y_b - 20 = 0$

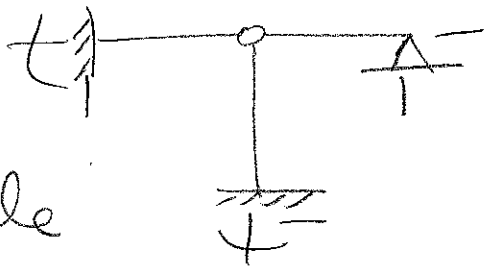
$\Rightarrow Y_a = 16.67t$



$M_c = 16.67 \times 2 - 20 \times 1 = +13.34$



Q4



Stable

$U = 8$

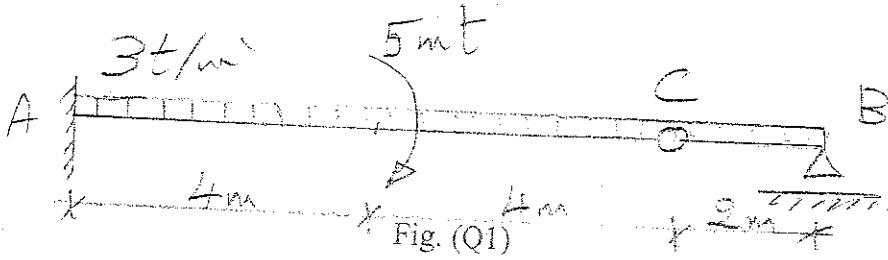
$E = 3 + (3 - 1) = 5$

\therefore 3 times st. indeterminate

Q1

For the shown beam:

1. Separate at C.
2. Find the reactions.
3. Draw the N.F.D., Q.F.D. & B.M.D.



ILO's

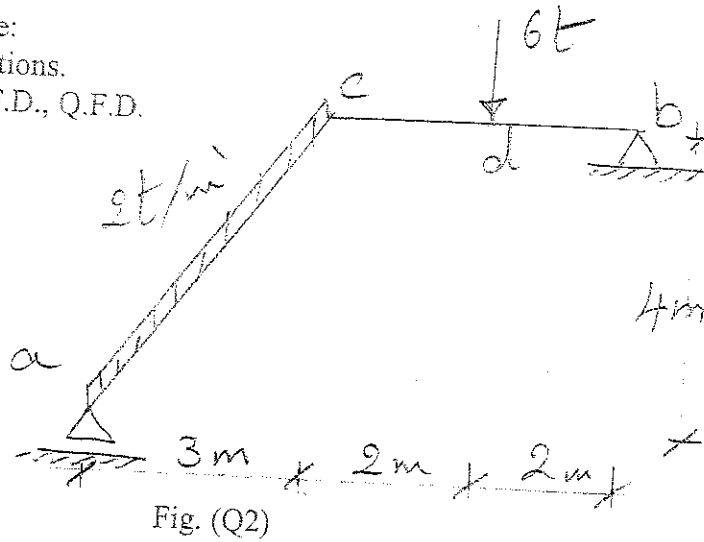
- | | |
|------|-----------|
| [a2] | [2 marks] |
| [a2] | [2 marks] |
| [a2] | [4 marks] |

[Total 8]

Q2

For the shown Frame:

1. Find the reactions.
2. Draw the N.F.D., Q.F.D.
3. Draw B.M.D.



- | | |
|------|-----------|
| [a1] | [3 marks] |
| [a2] | [3 marks] |
| [a2] | [4 marks] |

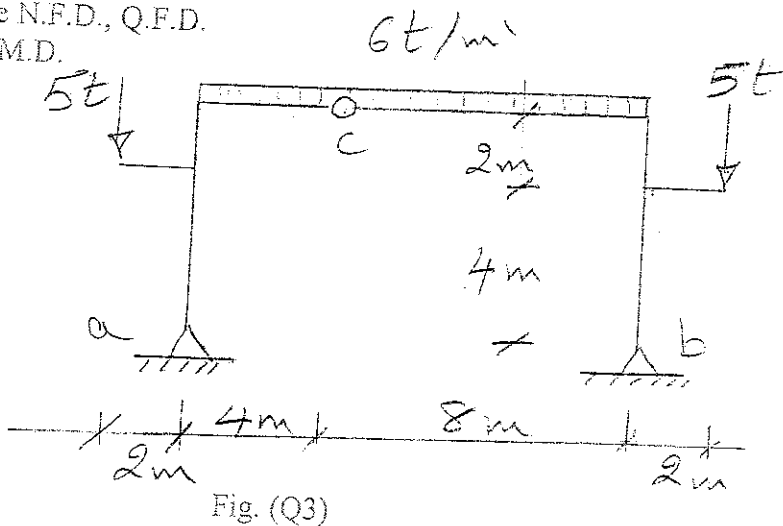
3

[Total 10]

Q3

For the shown Frame:

4. Find the reactions.
5. Draw the N.F.D., Q.F.D.
6. Draw B.M.D.

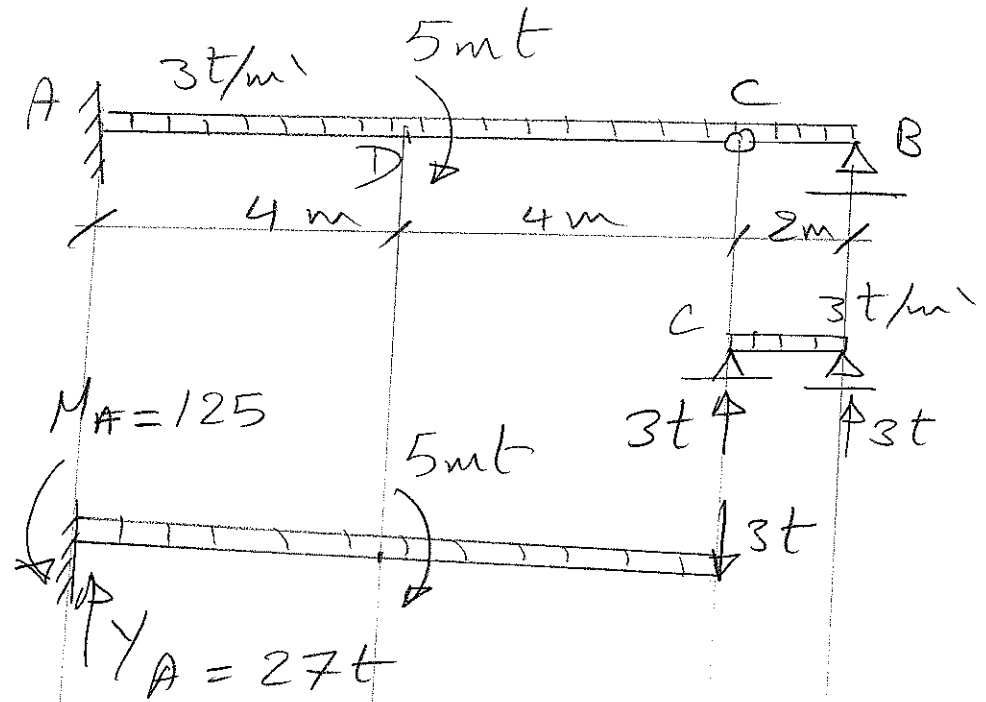


- | | |
|------|-----------|
| [a1] | [4 marks] |
| [a2] | [4 marks] |
| [a2] | [4 marks] |

[Total 12]

[Total 30]

Q1



$$\sum F_y = 0$$

$$Y_A = 3 + 3 \times 8 = 27t$$

$$\sum M @ A = 0$$

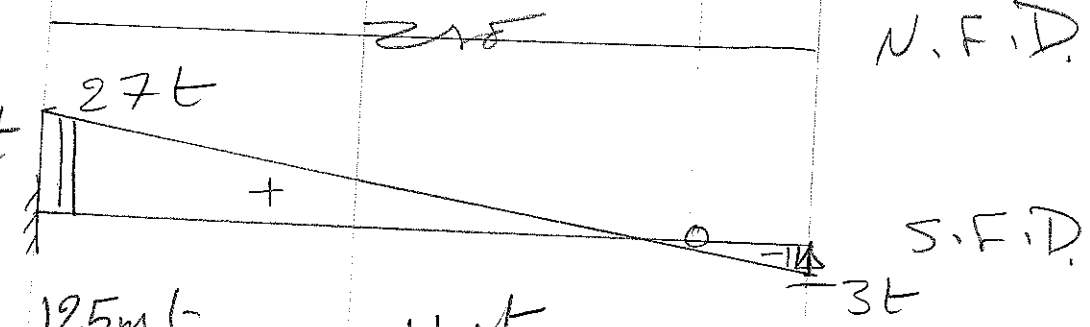
$$-M_A - 3 \times 8 \times 4$$

$$-5 - 3 \times 8 = 0$$

$$\therefore M_A = 125mt$$

$$M_A = 125$$

$$Y_A = 27t$$

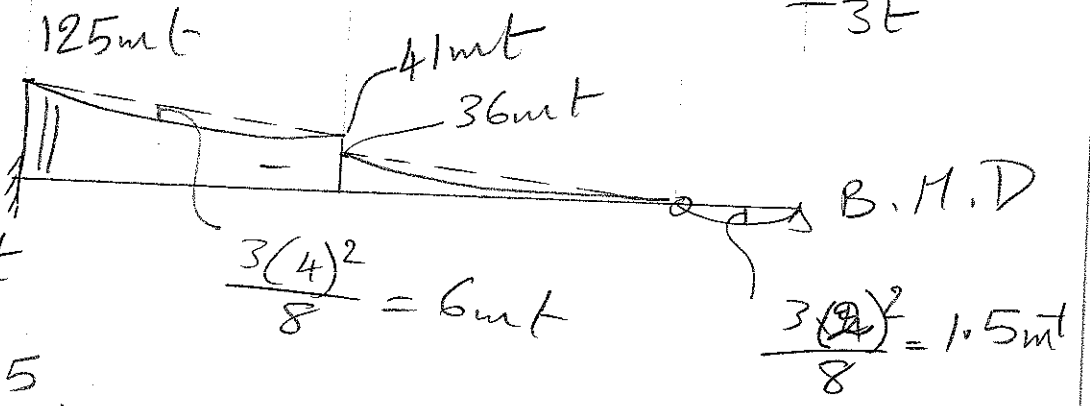


$$M_D \text{ right} = 3 \times 4 + 3 \times 4 \times 2 = 36mt$$

$$M_D \text{ left} = 36 + 5 = 41mt$$

$$\frac{3(4)^2}{8} = 6mt$$

$$\frac{3(2)^2}{8} = 1.5mt$$



Q2

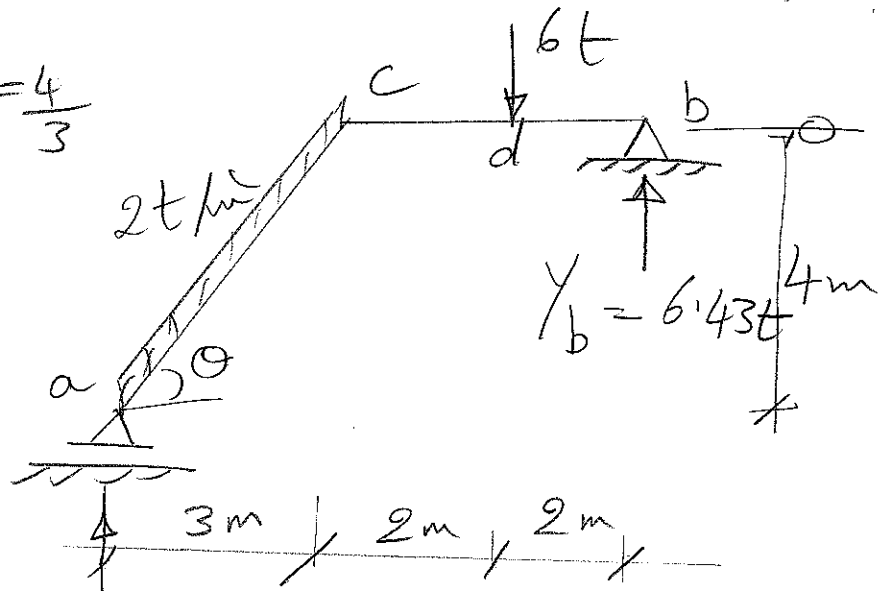
$$\tan \theta = \frac{4}{3}$$

$$\sum M @ b = 0$$

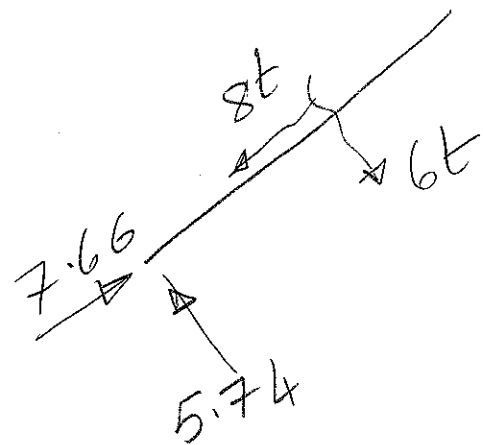
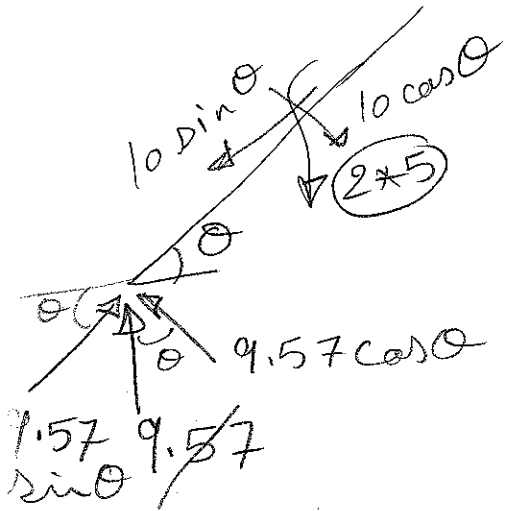
$$6 \times 2 + 2 \times 5 \times 5.5$$

$$- 7 Y_a = 0$$

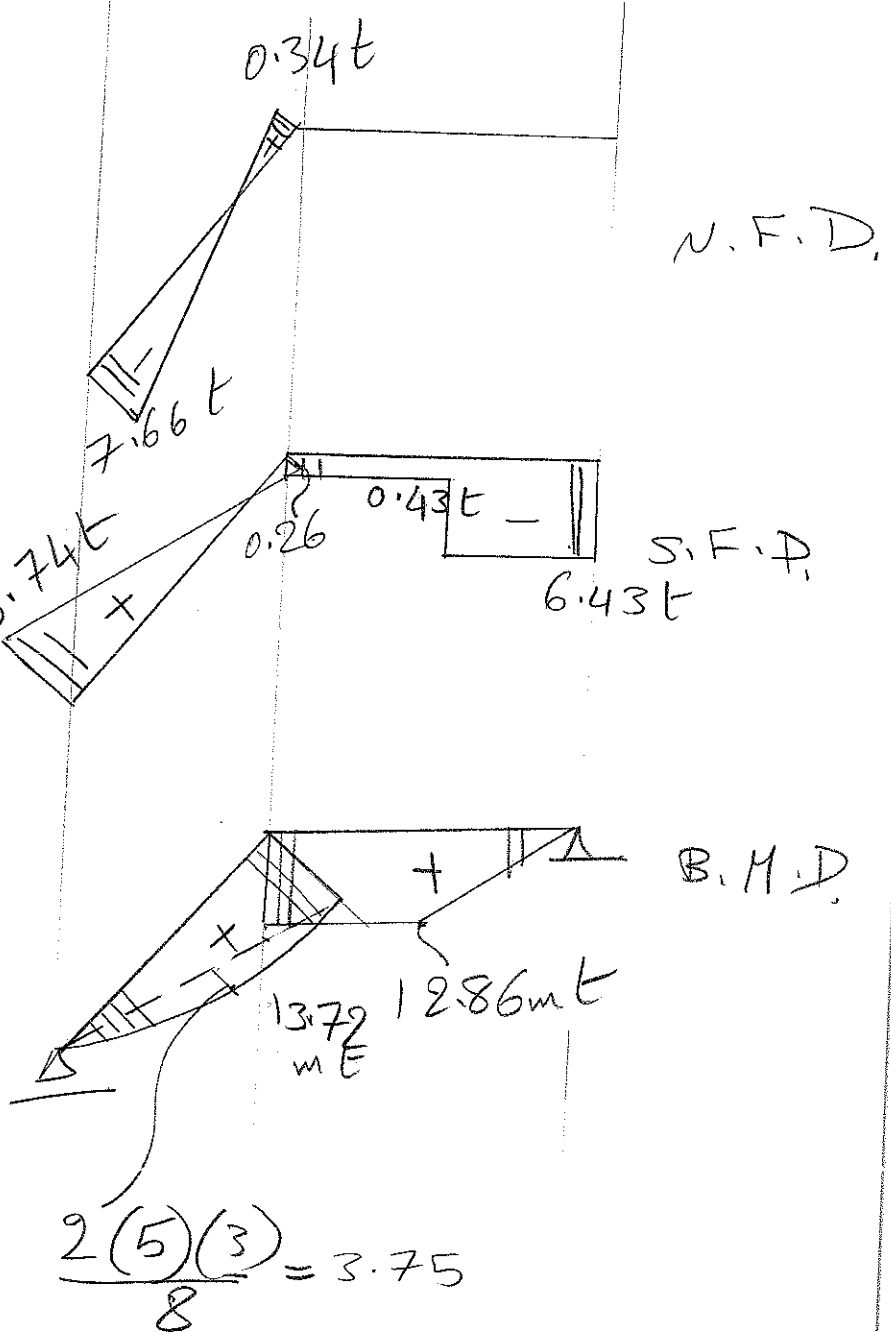
$$\therefore Y_a = 9.57t$$



$$Y_a = 9.57t$$



$$M_c = 6.43 \times 4 - 6 \times 2$$



$$\frac{2(5)(3)}{8} = 3.75$$

Q3

$$\sum M @ b = 0$$

$$5 \times 14 + 6 \times 12 \times 6 - 12 Y_a - 8 \times 2 = 0$$

$$\therefore Y_a = 41 t$$

$$\sum M @ c_{right} = 0$$

$$6 \times 8 \times 4 + 5 \times 10 + 6 X_b - 41 \times 8 = 0$$

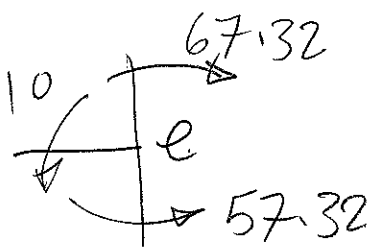
$$\therefore X_b = 14.33 t$$

check

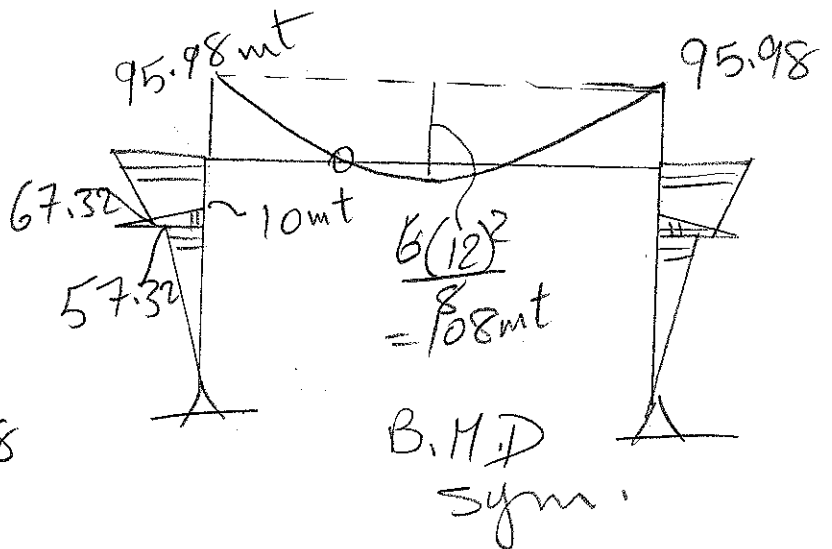
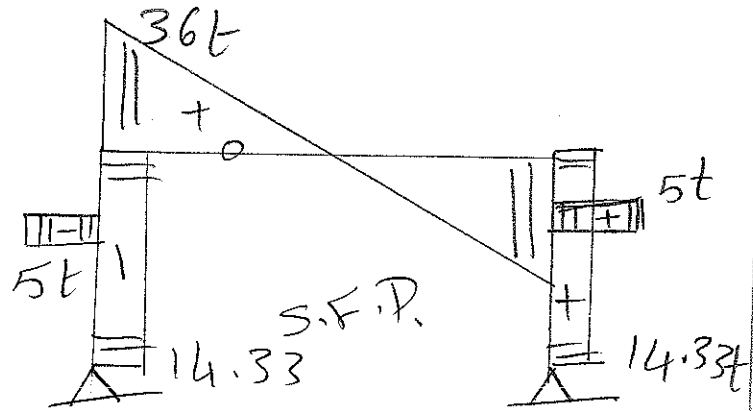
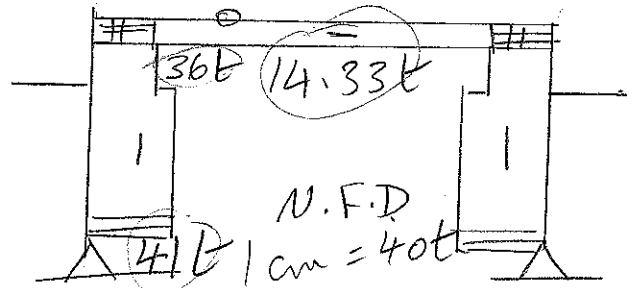
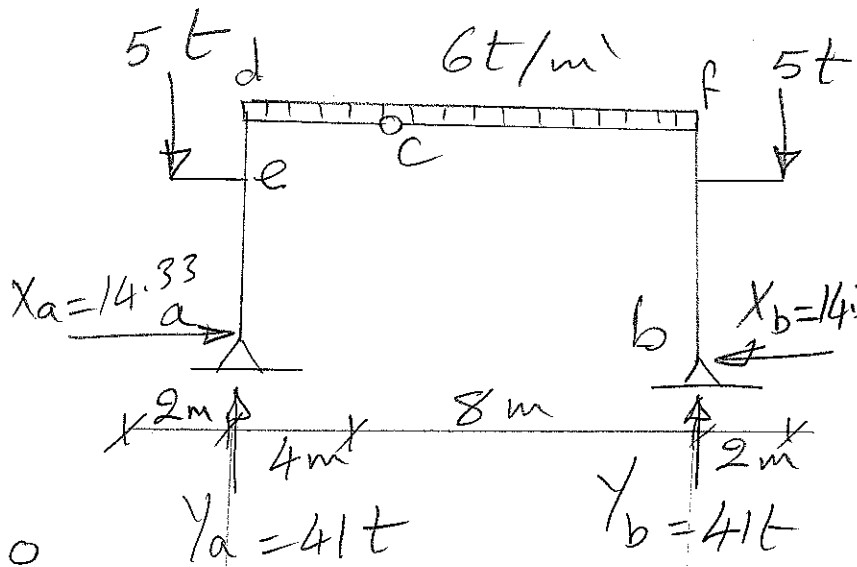
$$\sum M @ c_{left} = 0$$

$$6 \times 4 \times 2 + 5 \times 6 + 6 X_a - 41 \times 4 = 0$$

$$\therefore X_a = 14.33 t$$



$$M_f = 14.33 \times 6 + 5 \times 2 = 95.98$$

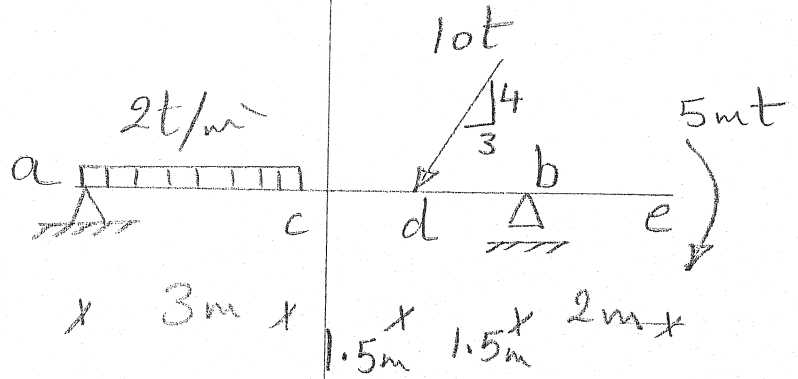


Mid Term Exam

Question 1 [a2,b3,c2] {10 Marks}

For the shown beam:

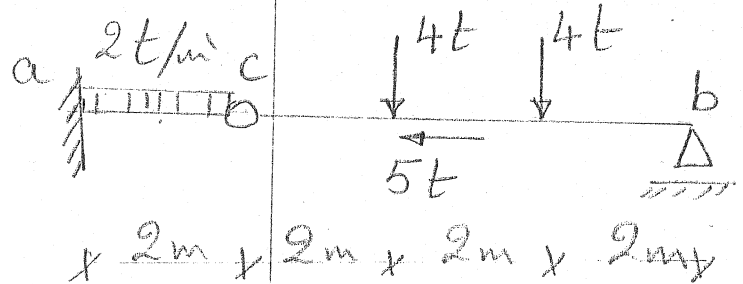
1. Find the reactions. {3 M}
2. Draw the N.F.D., Q.F.D. {4 M}
3. Draw the B.M.D. {3 M}



Question 2 [a2,b3,c2] {10 Marks}

For the shown beam:

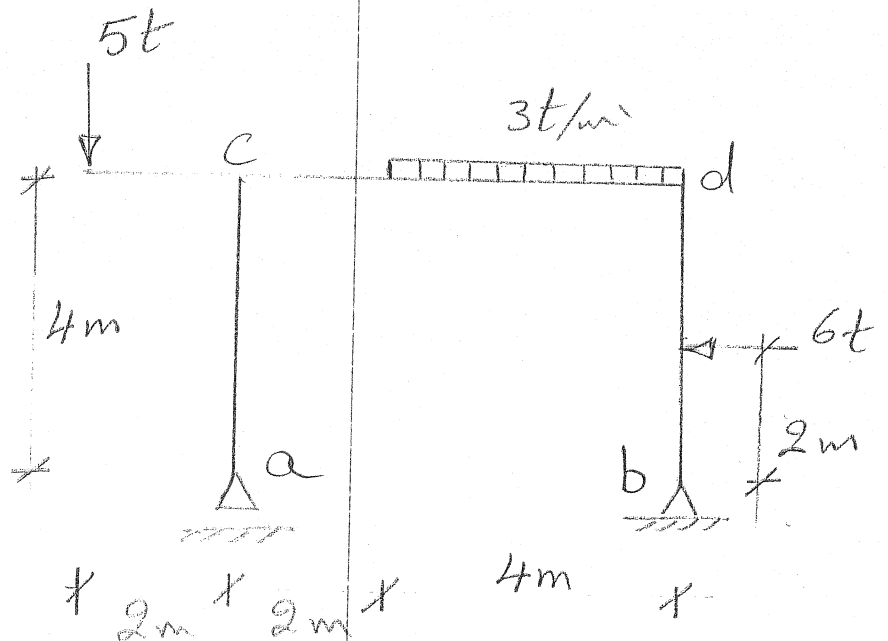
1. Separate at C. {1 M}
2. Find the reactions. {2 M}
3. Draw the N.F.D., Q.F.D. {4 M}
4. Draw the B.M.D. {3 M}



Question 3 [a2,b3,c2] {10 Marks}

For the shown Frame:

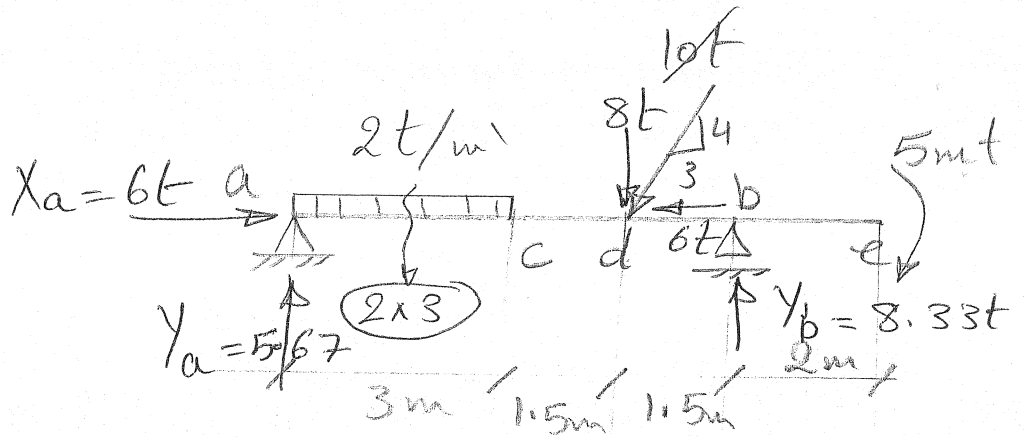
1. Find the reactions. {3 M}
2. Draw the N.F.D., Q.F.D. {4 M}
3. Draw B.M.D. {3 M}



Examination committee: 1-Name
2-Name

Signature
Signature

Q1



① $\sum M @ a = 0$

$$2 \times 3 \times 1.5 + 8 \times 4.5 - 6 Y_b + 5 = 0$$

$$\Rightarrow Y_b = 8.33t$$

② $\sum F_y = 0$

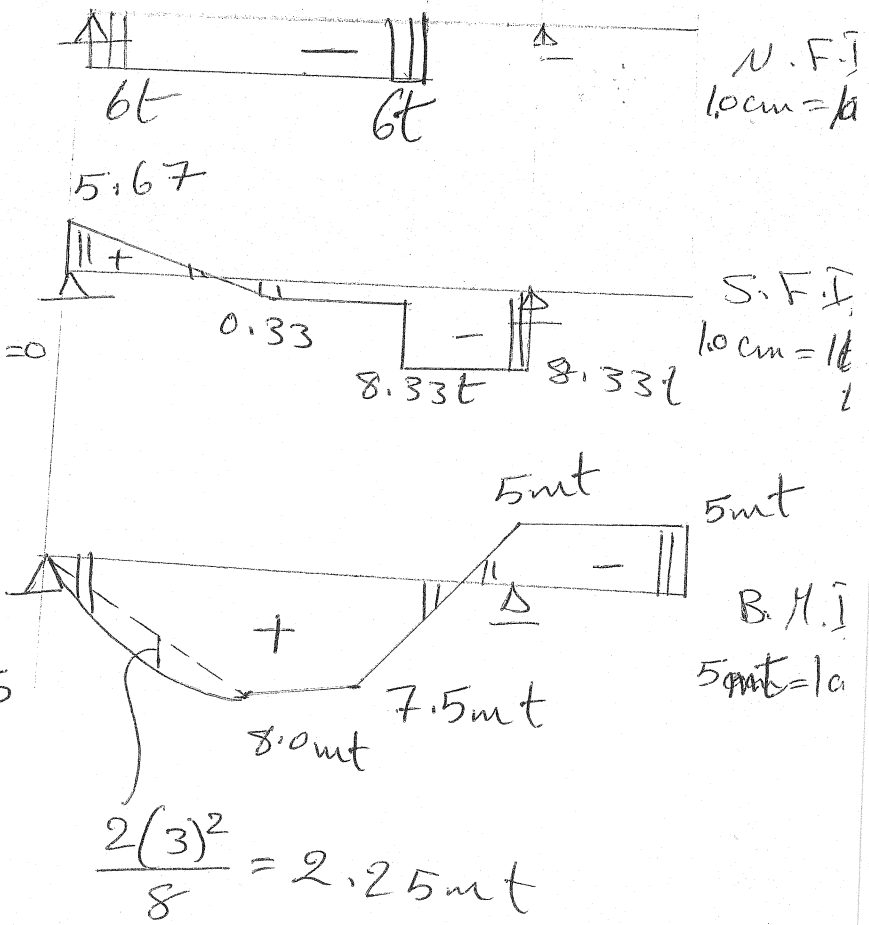
$$Y_a - 2 \times 3 - 8 + 8.33 = 0$$

$$\Rightarrow Y_a = 5.67t$$

$$M_c = 5.67 \times 3 - 2 \times 3 \times 1.5 = 8.01 \text{ mt}$$

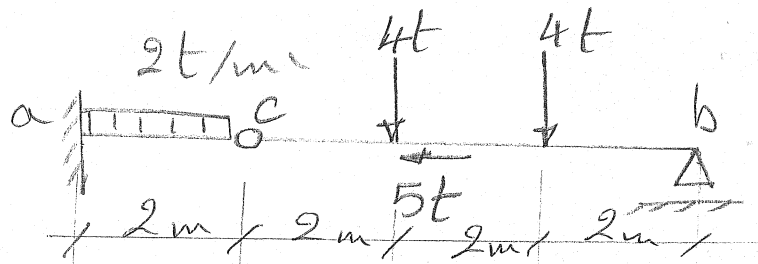
$$M_d = -5 + 8.33 \times 1.5$$

$$M_d = 7.5 \text{ mt}$$



$$\frac{2(3)^2}{8} = 2.25 \text{ mt}$$

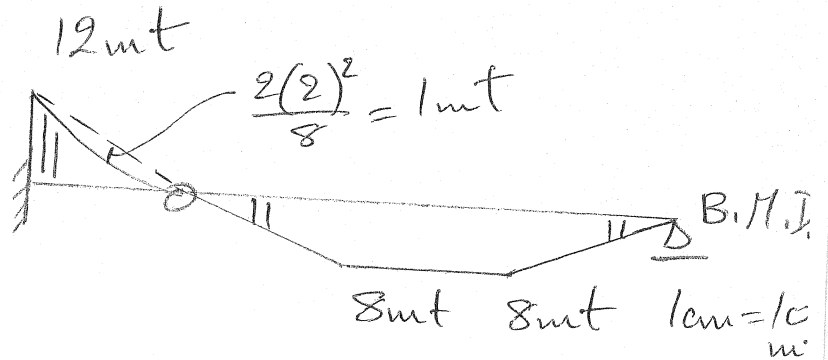
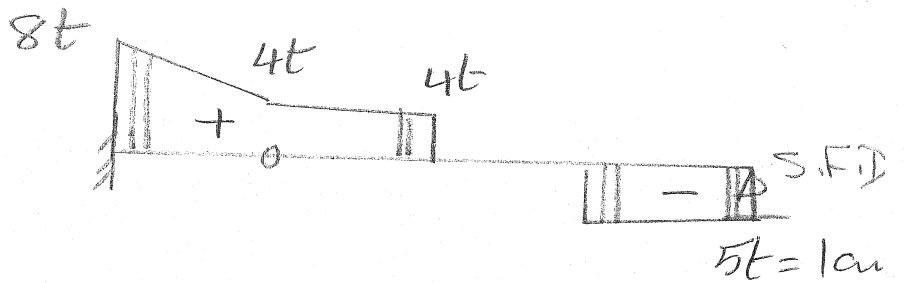
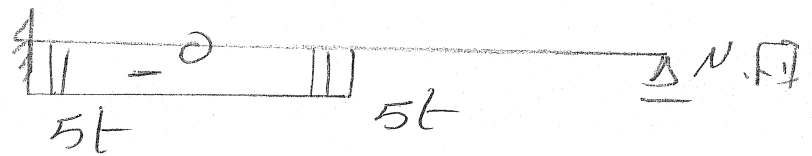
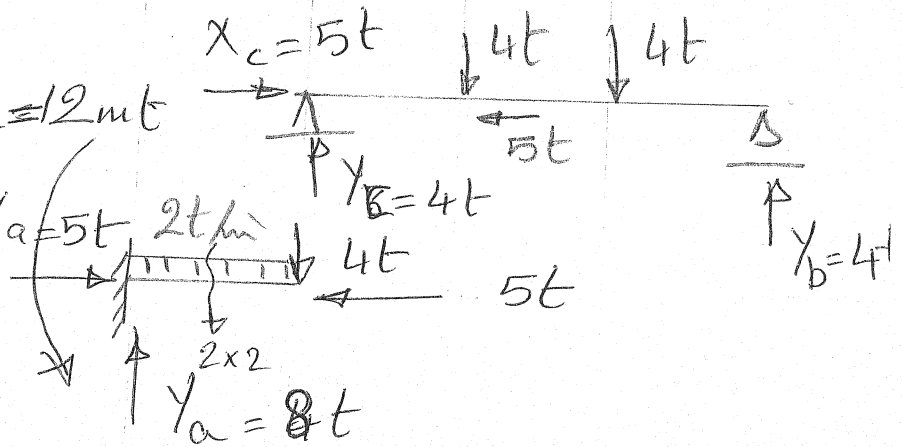
Q2



$\sum M @ a = 0$

$2 \times 2 \times 1 + 4 \times 2 - M_a = 0$
 $\therefore M_a = 12mt$

$M_a = 12mt$



Q3

① $\sum M @ b = 0$

$$5 \times 8 + 3 \times 4 \times 2 + 6 \times 2 - 6Y_a = 0$$

$\Rightarrow Y_a = 12.67t$

② $\sum F_y = 0$

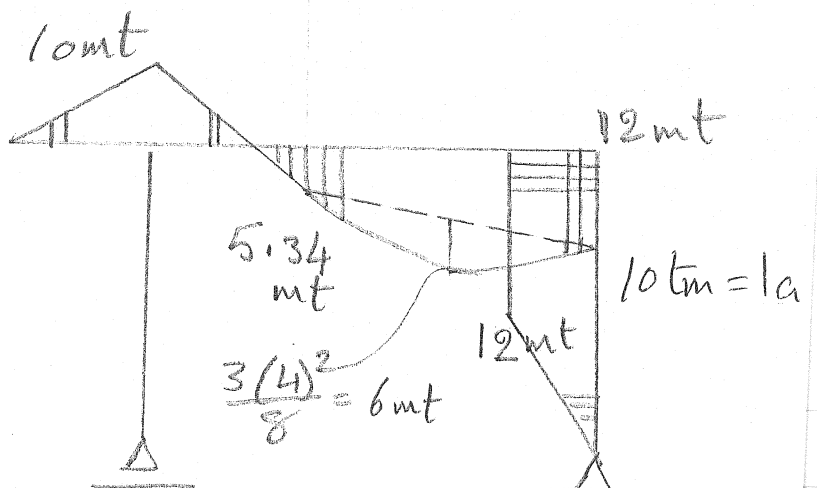
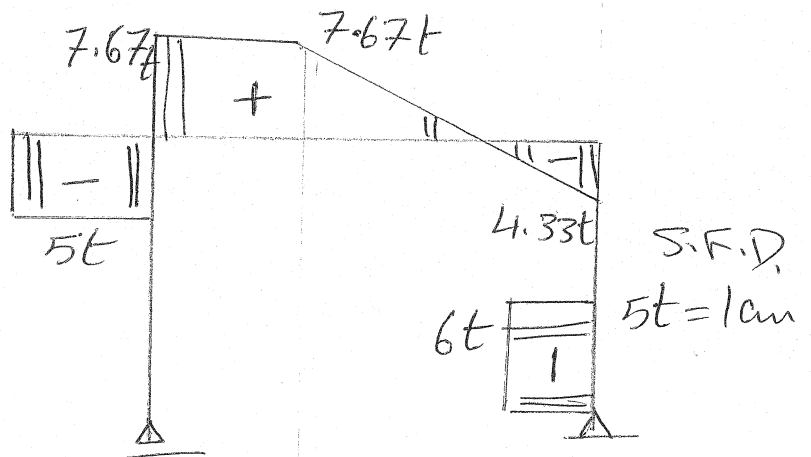
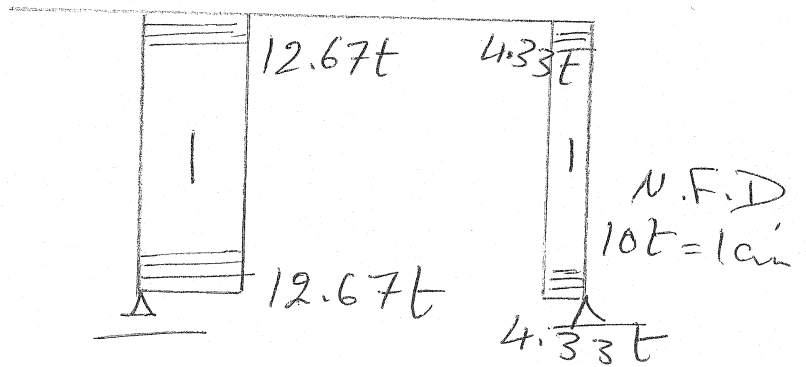
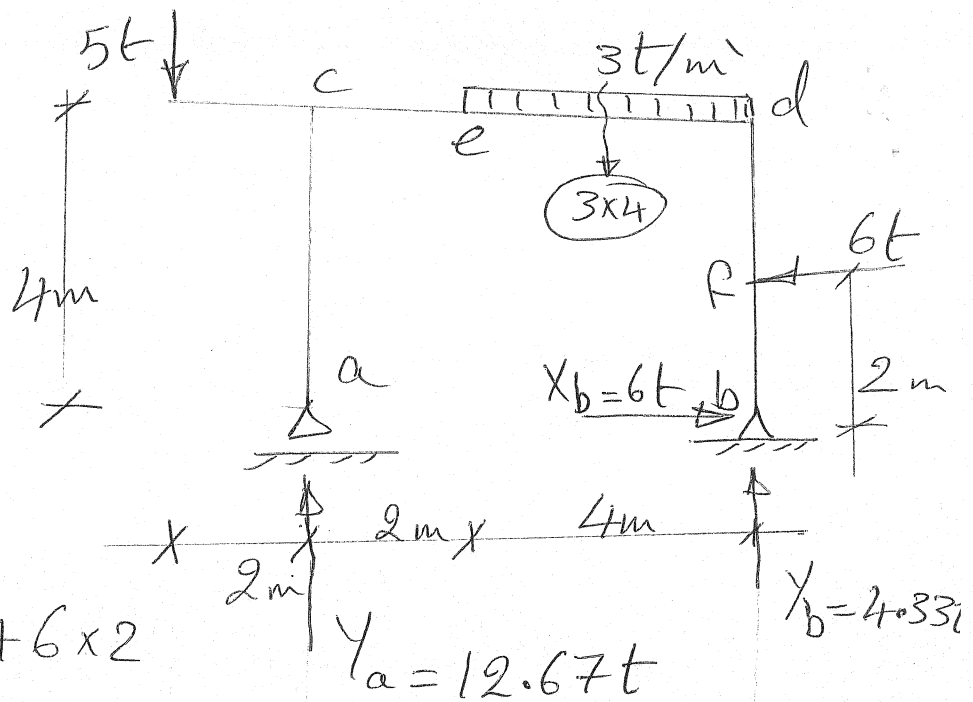
$$12.67 - 5 - 3 \times 4 + Y_b = 0$$

$\Rightarrow Y_b = 4.33t$

$$M_e = 12.67 \times 2 - 5 \times 4 = 5.34 \text{ mt}$$

$$M_d = 6 \times 4 - 6 \times 2 = 12 \text{ mt}$$

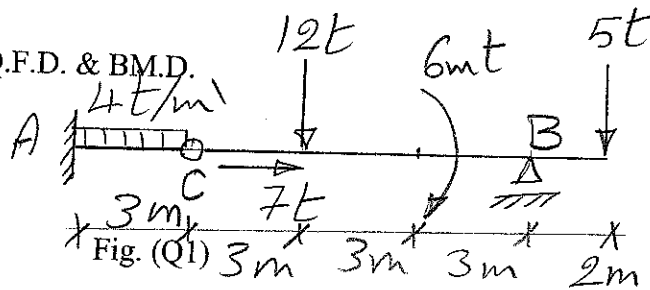
$$M_f = 6 \times 2 = 12 \text{ mt}$$



Q1

For the shown beam:

1. Separate at C.
2. Find the reactions.
3. Draw the N.F.D., Q.F.D. & B.M.D.



ILO's

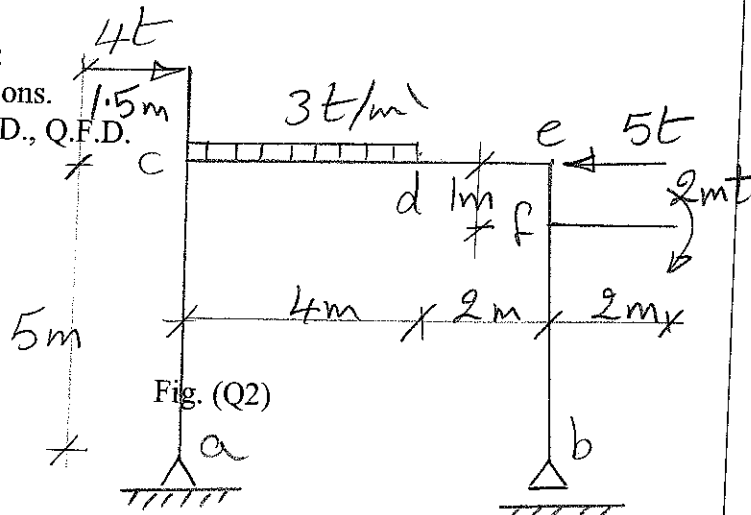
- [a2] [2 marks]
- [a2] [2 marks]
- [a2] [4 marks]

[Total 8]

Q2

For the shown Frame:

1. Find the reactions.
2. Draw the N.F.D., Q.F.D.
3. Draw B.M.D.



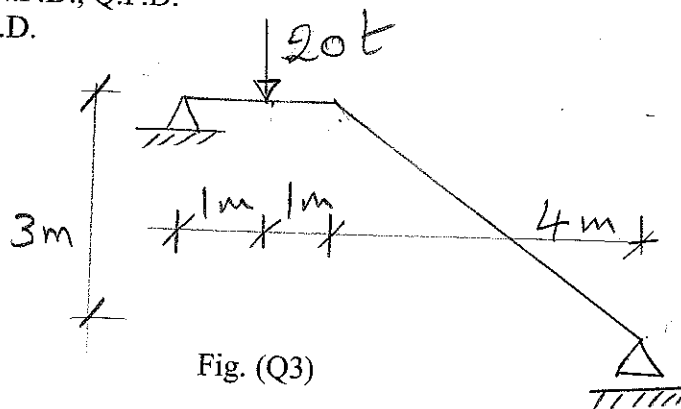
- [a1] [3 marks]
- [a2] [3 marks]
- [a2] [4 marks]

[Total 10]

Q3

For the shown Frame:

4. Find the reactions.
5. Draw the N.F.D., Q.F.D.
6. Draw B.M.D.

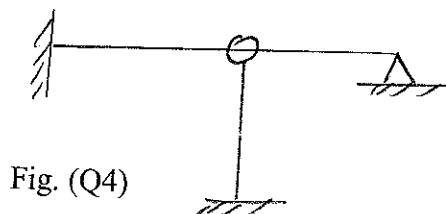


- [a1] [2 marks]
- [a2] [4 marks]
- [a2] [4 marks]

[Total 10]

Q4

Discuss the stability and determinacy of the shown structure:



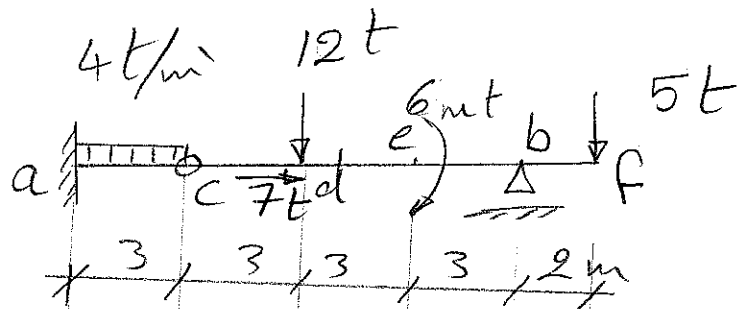
[d1]

[2 marks]

[Total 2]

[Total 30]

Q1



$$\sum M @ c = 0$$

$$12 \times 3 + 6 - 9Y_b + 5 \times 11 = 0$$

$$\therefore Y_b = 10.78 \text{ t}$$

$$\therefore Y_c = 6.22 \text{ t}$$

$$Y_a = 4 \times 3 + 6.22 = 18.22$$

$$\sum M @ a = 0$$

$$\therefore M_a - 4 \times 3 \times 1.5 - 6.22 \times 3 = 0 \quad 18.22 \text{ t}$$

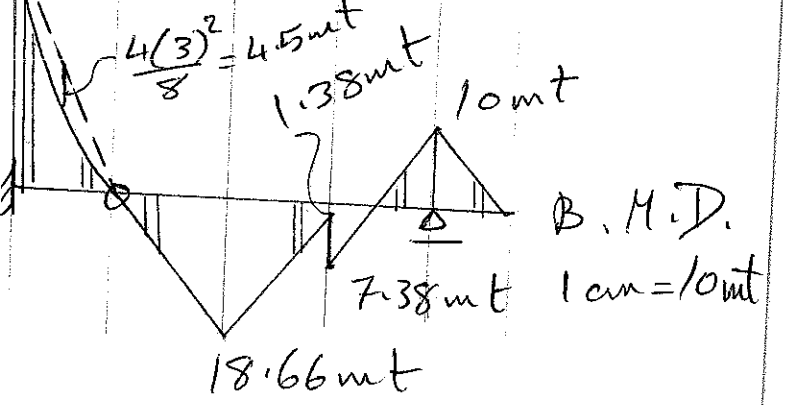
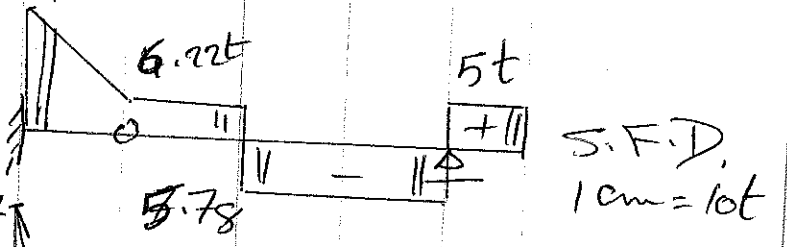
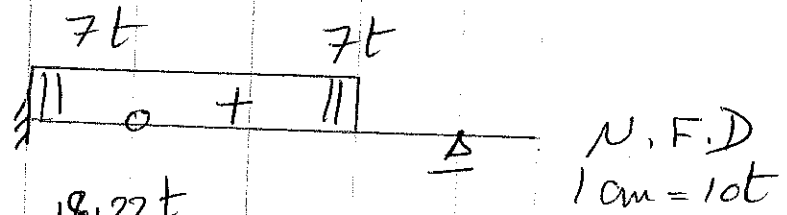
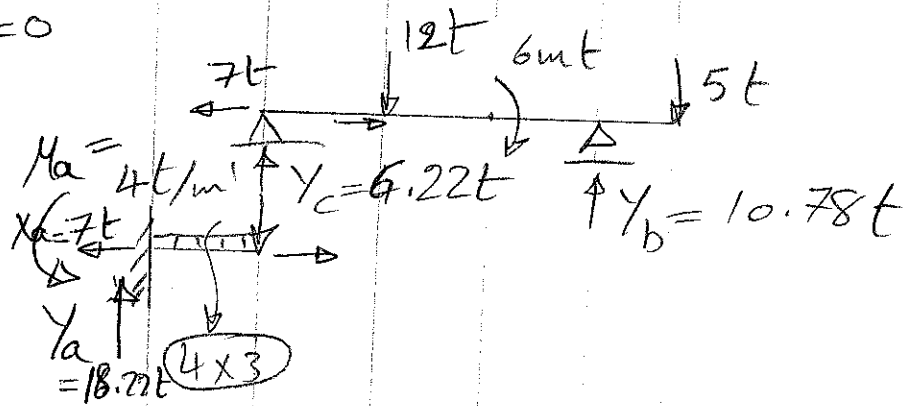
$$\therefore M_a = 36.67 \text{ mt}$$

$$M_b = -5 \times 2 = -10 \text{ mt}$$

$$M_{\text{right}} = -5 \times 5 + 10.78 \times 3 = +7.38$$

$$M_{\text{left}} = +7.38 - 6 = 1.38 \text{ mt}$$

$$M_d = 6.22 \times 3 = 18.66 \text{ mt}$$



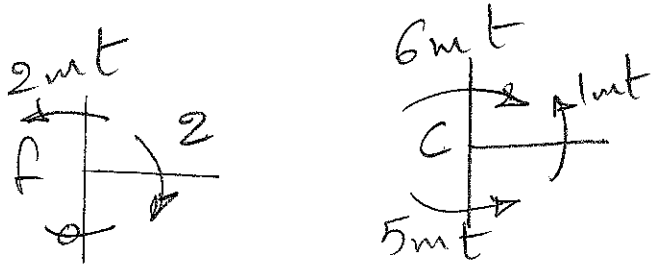
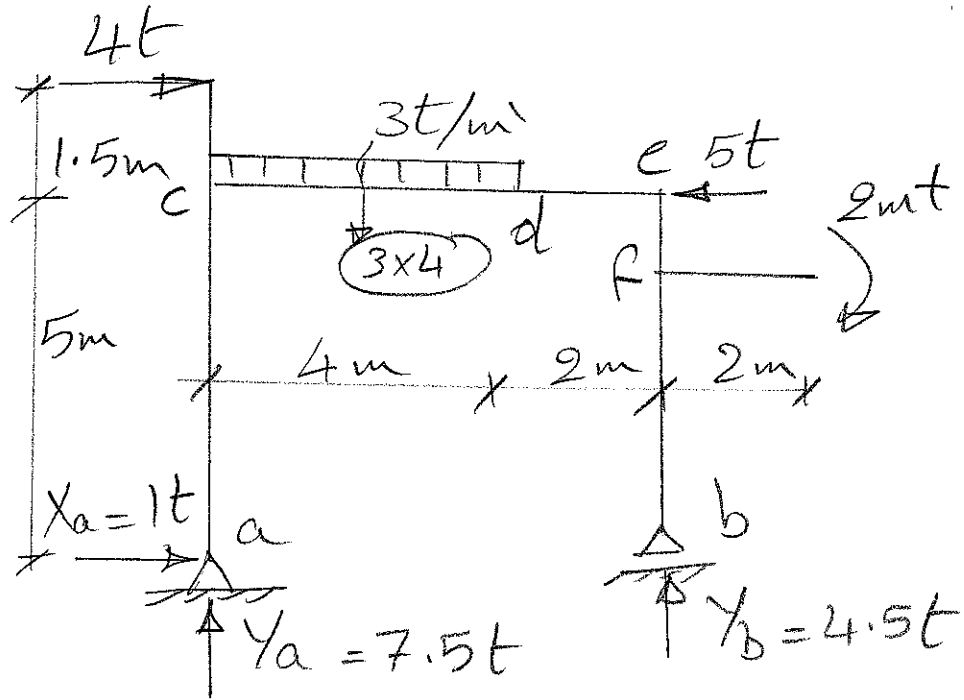
Q2

$$\sum M @ a = 0$$

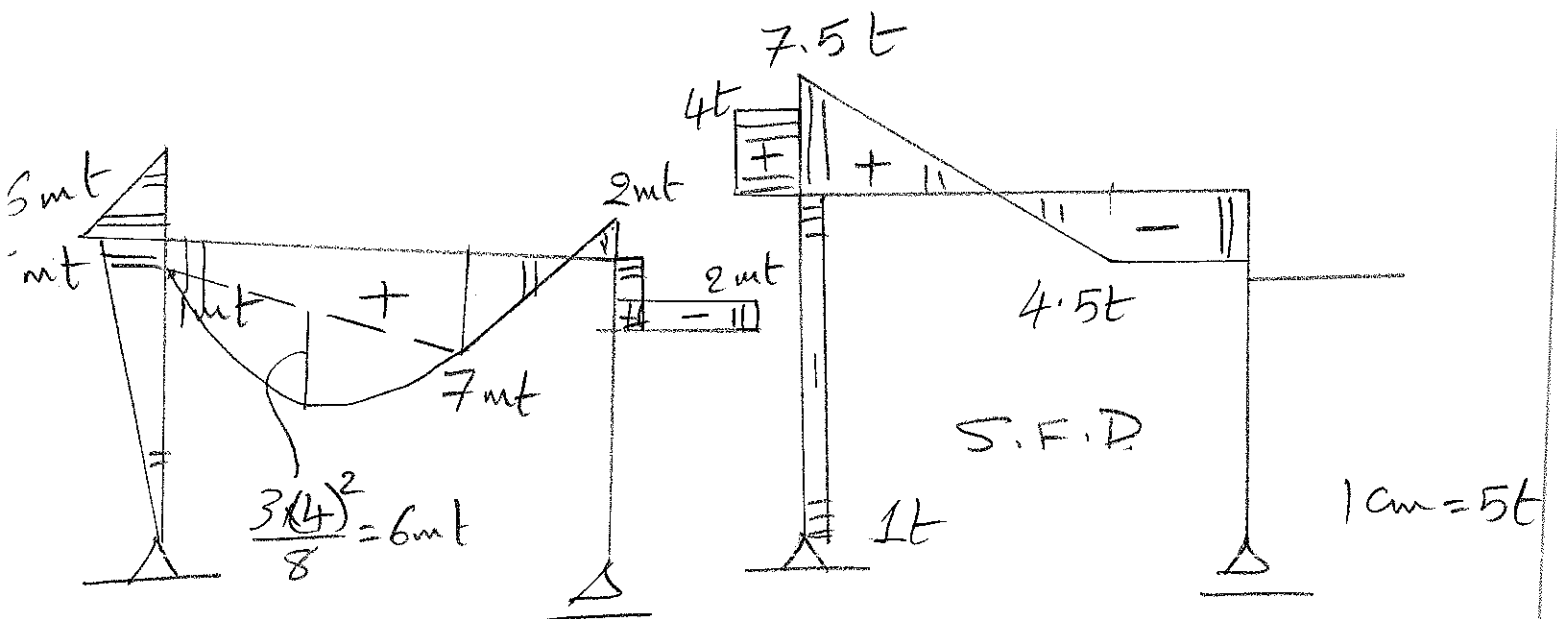
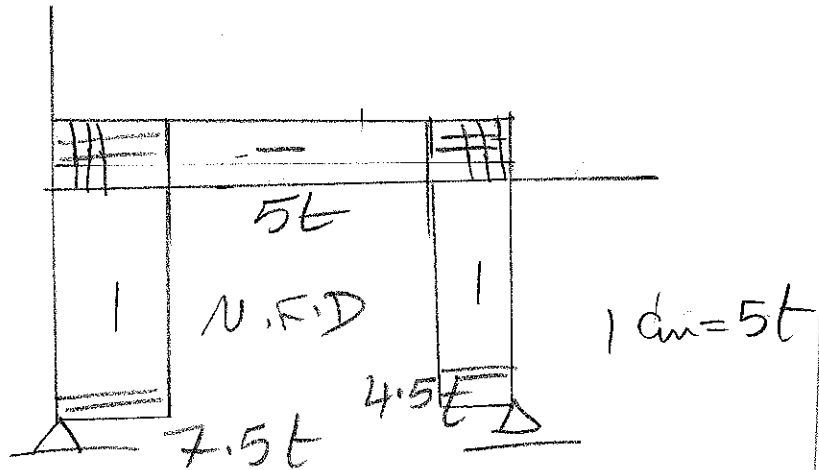
$$4 \times 6 \times 5 + 3 \times 4 \times 2 + 2 - 5 \times 5 - 6 \frac{y_b}{8} = 0$$

$$\Rightarrow y_b = 4.5t$$

$$\Rightarrow y_a = 7.5t$$



$$M_d = 4.5 \times 2 - 2 = 7mt$$



B.M.D
1cm = 5mt

Q3

$\textcircled{1} \sum M @ a = 0$

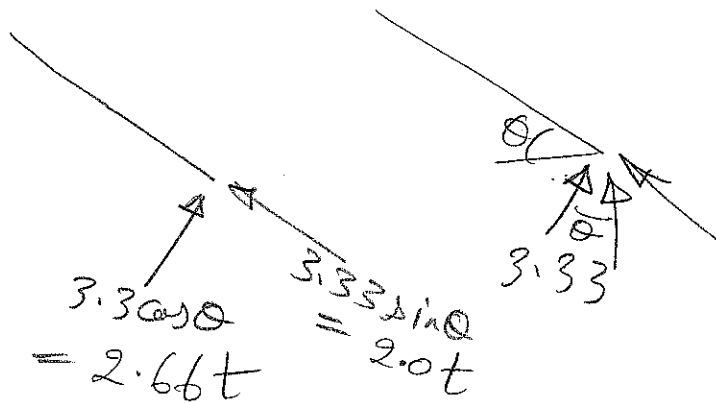
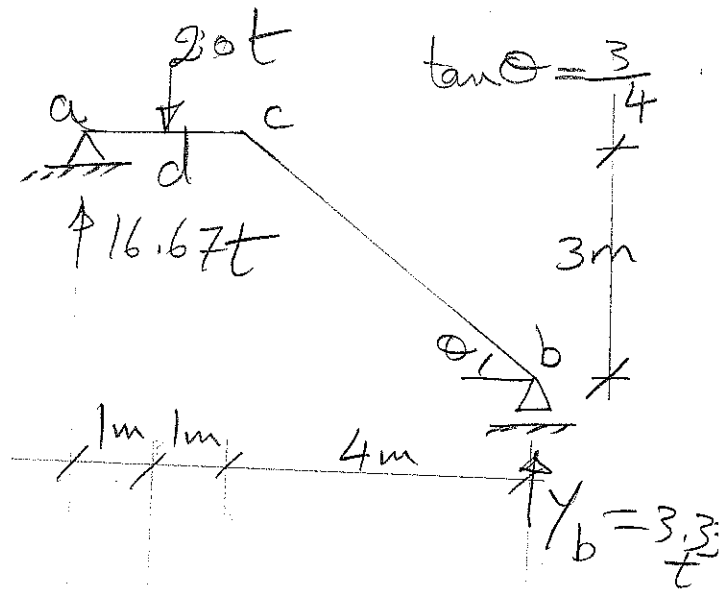
$20 \times 1 - 6Y_b = 0$

$\Rightarrow Y_b = 3.33t$

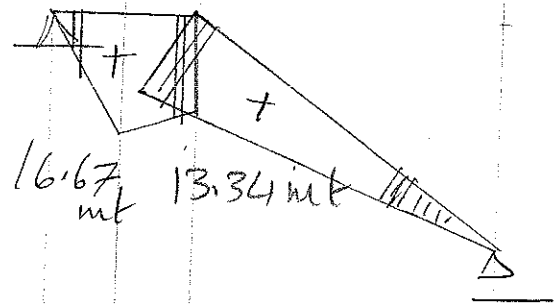
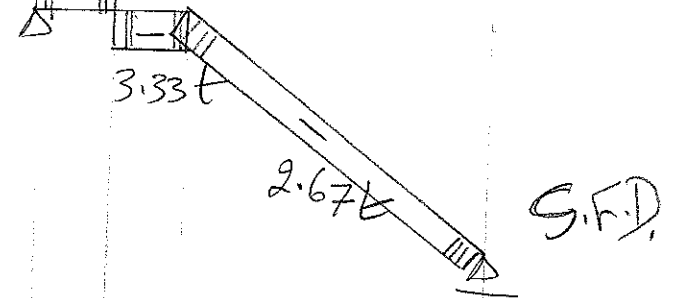
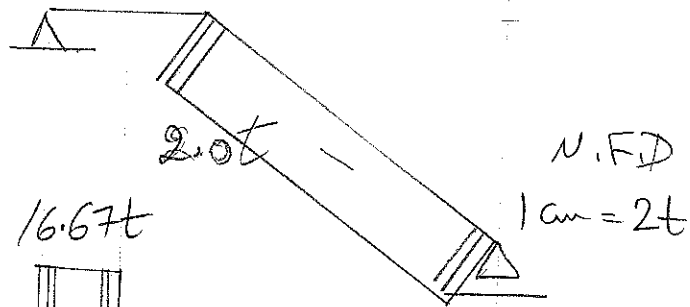
$\textcircled{2} \sum F_y = 0$

$Y_a + Y_b - 20 = 0$

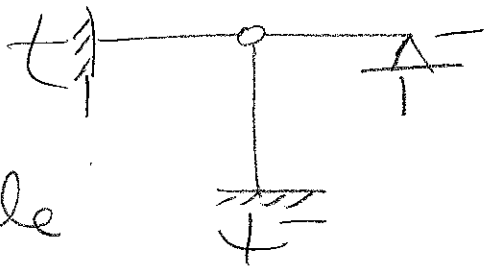
$\Rightarrow Y_a = 16.67t$



$M_c = 16.67 \times 2 - 20 \times 1 = +13.34$



Q4



Stable

$U = 8$

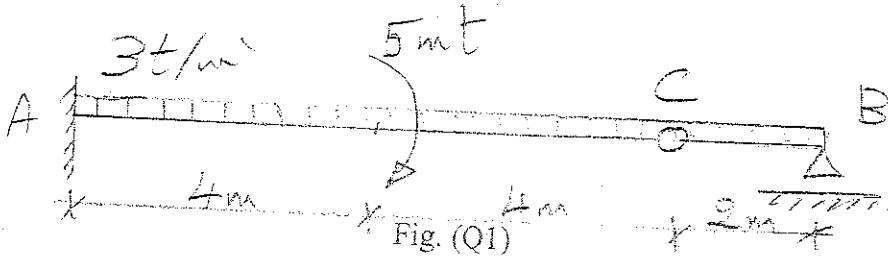
$E = 3 + (3 - 1) = 5$

\therefore 3 times st. indeterminate

Q1

For the shown beam:

1. Separate at C.
2. Find the reactions.
3. Draw the N.F.D., Q.F.D. & B.M.D.



ILO's

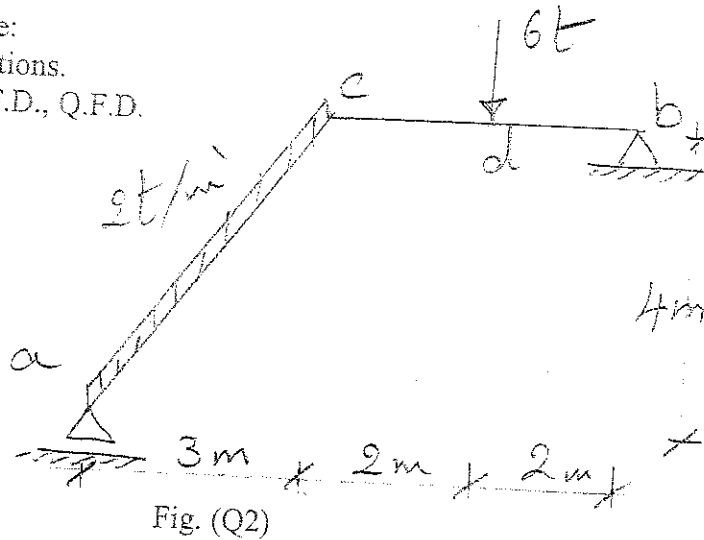
- | | |
|------|-----------|
| [a2] | [2 marks] |
| [a2] | [2 marks] |
| [a2] | [4 marks] |

[Total 8]

Q2

For the shown Frame:

1. Find the reactions.
2. Draw the N.F.D., Q.F.D.
3. Draw B.M.D.



- | | |
|------|-----------|
| [a1] | [3 marks] |
| [a2] | [3 marks] |
| [a2] | [4 marks] |

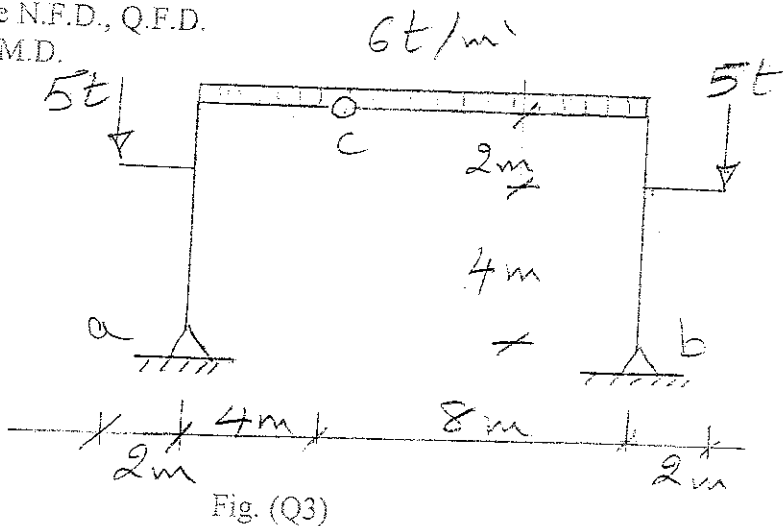
3

[Total 10]

Q3

For the shown Frame:

4. Find the reactions.
5. Draw the N.F.D., Q.F.D.
6. Draw B.M.D.

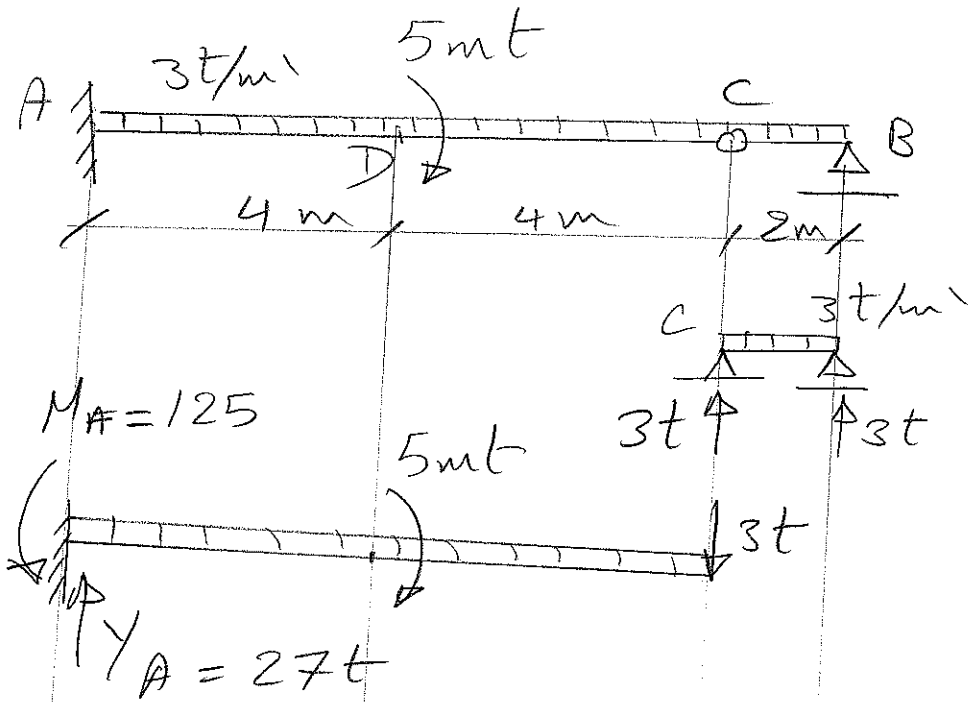


- | | |
|------|-----------|
| [a1] | [4 marks] |
| [a2] | [4 marks] |
| [a2] | [4 marks] |

[Total 12]

[Total 30]

Q1



$$\sum F_y = 0$$

$$Y_A = 3 + 3 \times 8 = 27t$$

$$\sum M @ A = 0$$

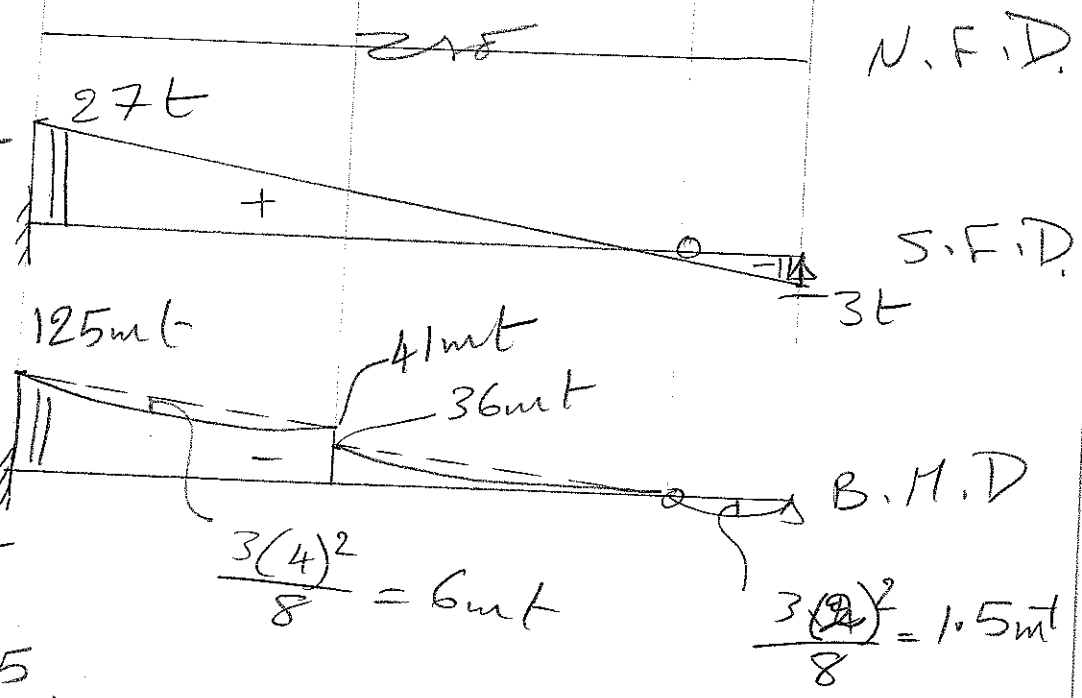
$$-M_A - 3 \times 8 \times 4$$

$$-5 - 3 \times 8 = 0$$

$$\therefore M_A = 125mt$$

$$M_D \text{ right} = 3 \times 4 + 3 \times 4 \times 2 = 36mt$$

$$M_D \text{ left} = 36 + 5 = 41mt$$



Q2

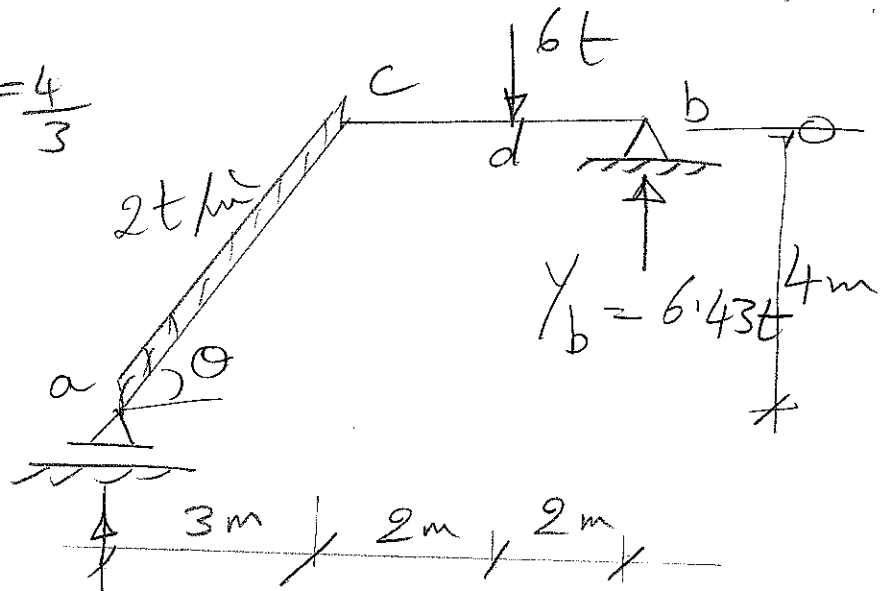
$$\tan \theta = \frac{4}{3}$$

$$\sum M @ b = 0$$

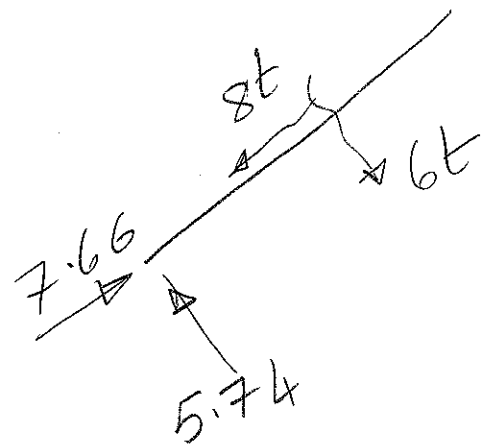
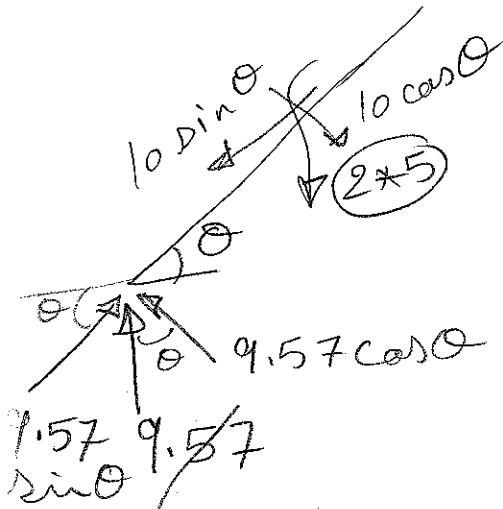
$$6 \times 2 + 2 \times 5 \times 5.5$$

$$- 7 Y_a = 0$$

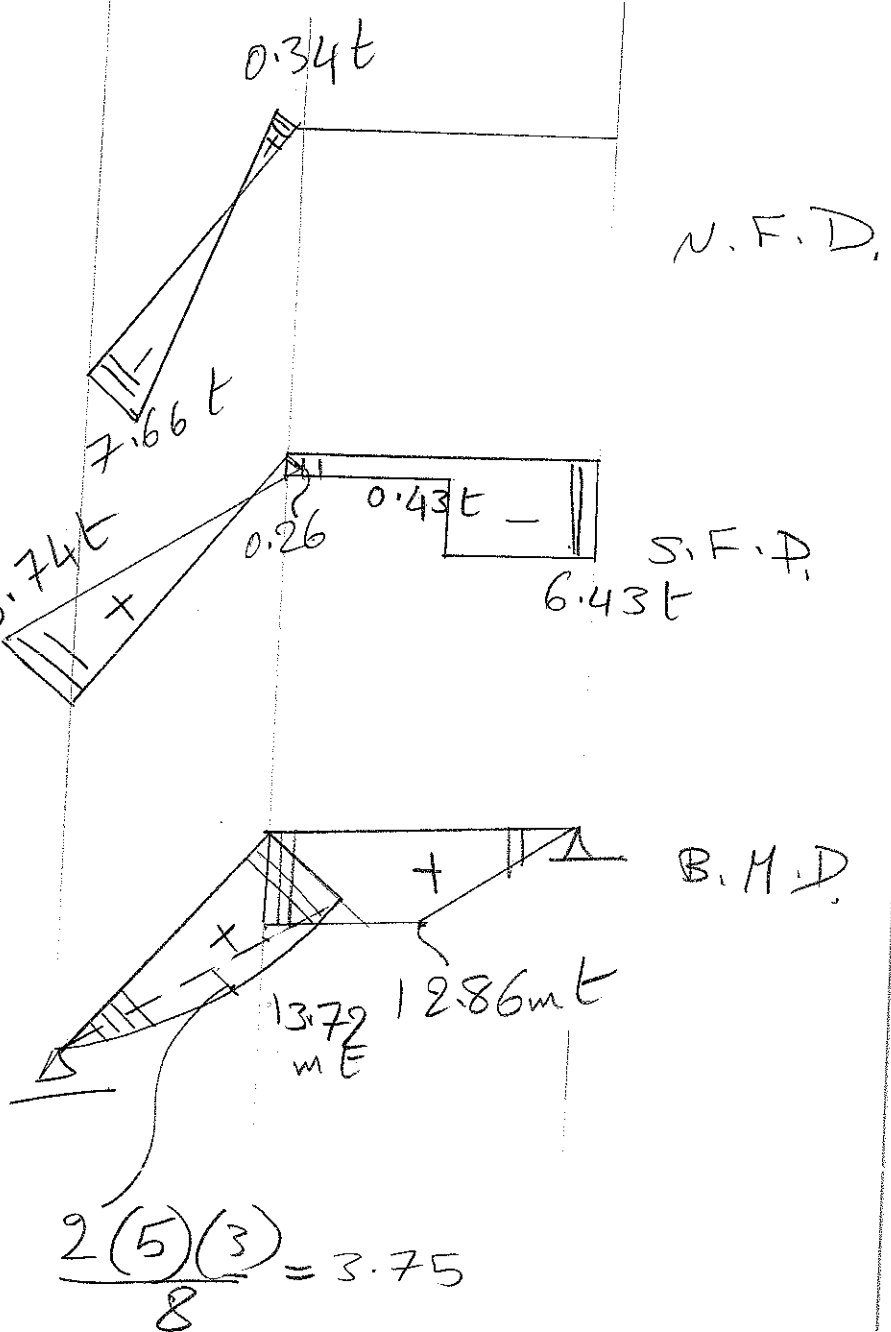
$$\therefore Y_a = 9.57t$$



$$Y_a = 9.57t$$



$$M_c = 6.43 \times 4 - 6 \times 2$$



$$\frac{2(5)(3)}{8} = 3.75$$

Q3

$$\sum M @ b = 0$$

$$5 \times 14 + 6 \times 12 \times 6$$

$$- 12 Y_a - 8 \times 2 = 0$$

$$\therefore Y_a = 41 t$$

$$\sum M @ c_{right} = 0$$

$$6 \times 8 \times 4 + 5 \times 10$$

$$+ 6 X_b - 41 \times 8 = 0$$

$$\therefore X_b = 14.33 t$$

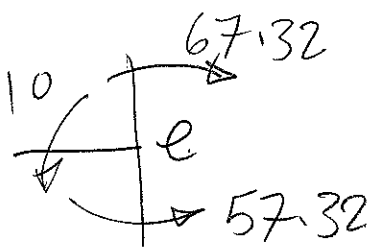
check

$$\sum M @ c_{left} = 0$$

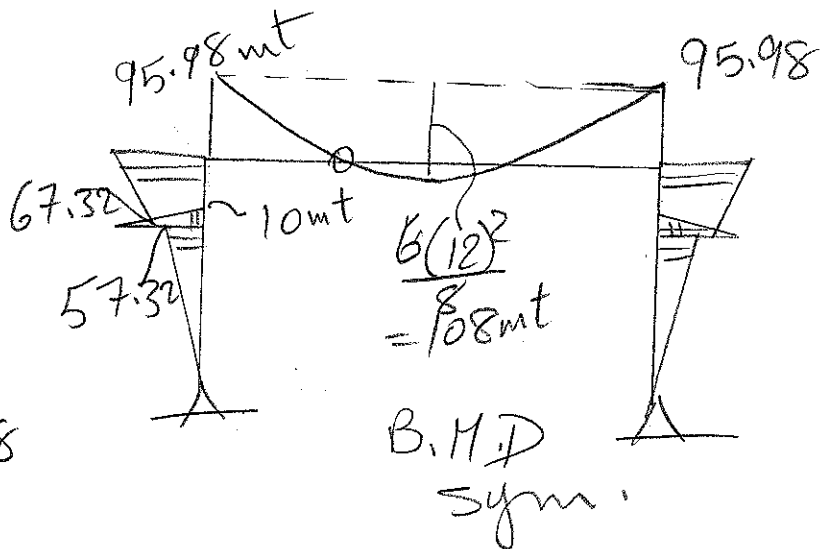
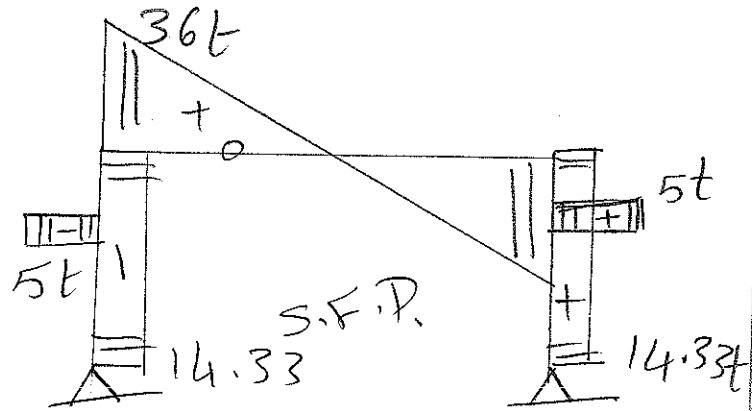
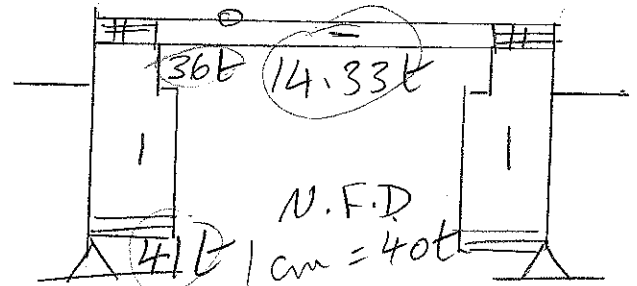
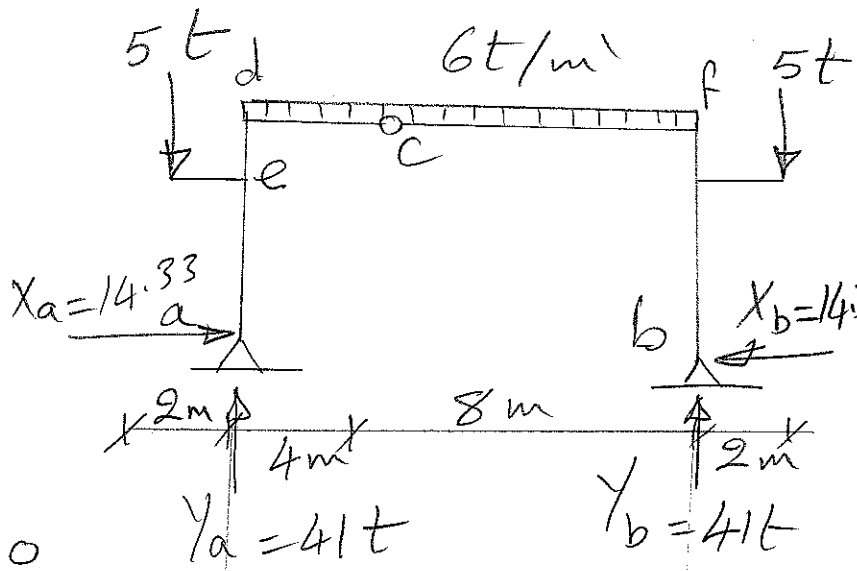
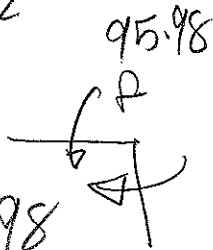
$$6 \times 4 \times 2 + 5 \times 6 + 6 X_a$$

$$- 41 \times 4 = 0$$

$$\therefore X_a = 14.33 t$$



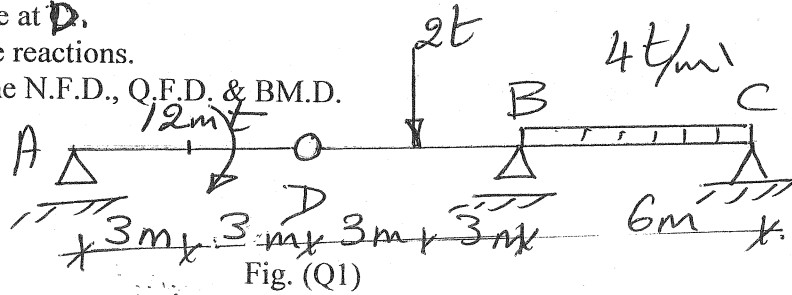
$$MF = 14.33 \times 6 + 5 \times 2 = 95.98$$



Q1

For the shown beam:

1. Separate at D.
2. Find the reactions.
3. Draw the N.F.D., Q.F.D. & B.M.D.



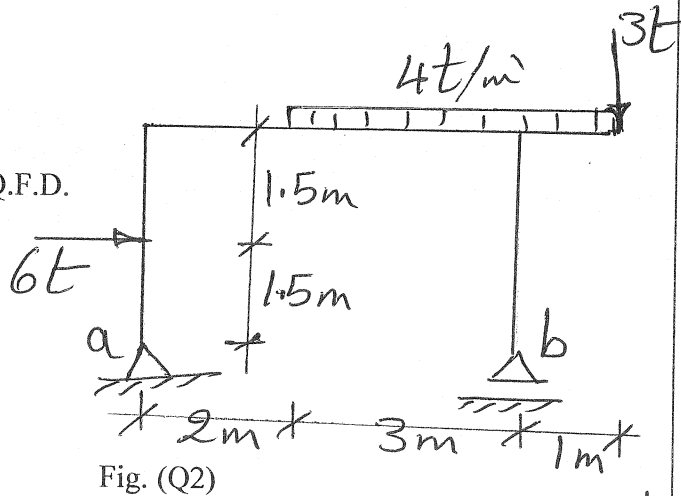
ILO's

- [a2] [2 marks]
- [a2] [2 marks]
- [a2,b3,c2] [4 marks]

Q2

For the shown Frame:

1. Find the reactions.
2. Draw the N.F.D., Q.F.D.
3. Draw B.M.D.



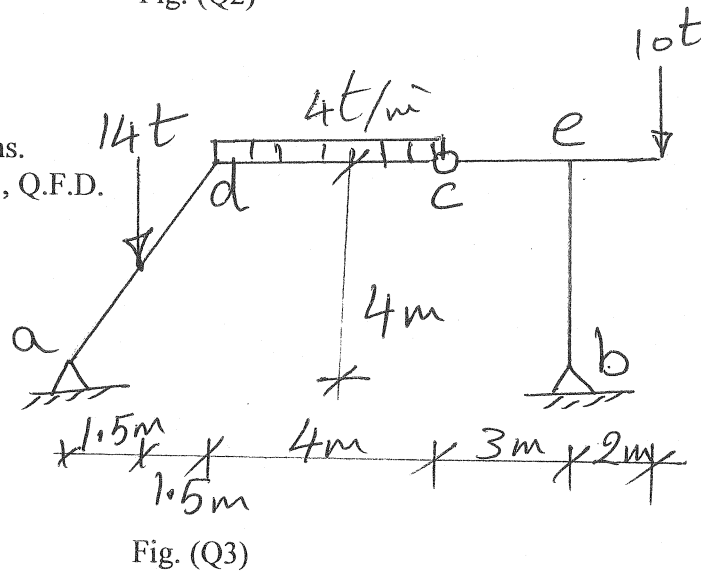
[Total 8]

- [a2] [2 marks]
- [a2,b3,c2] [4 marks]
- [a2,b3,c2] [4 marks]

Q3

For the shown Frame:

4. Find the reactions.
5. Draw the N.F.D., Q.F.D.
6. Draw B.M.D.

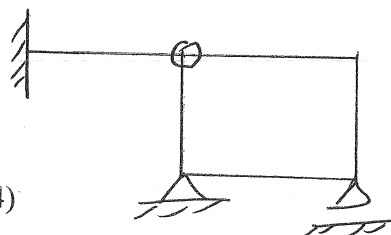


[Total 10]

- [a1] [2 marks]
- [a2,b3,c2] [4 marks]
- [a2,b3,c2] [4 marks]

Q4

Discuss the stability and determinacy of the shown structure:



[b1,c1]

[2 marks]

[Total 2]

[Total 30]

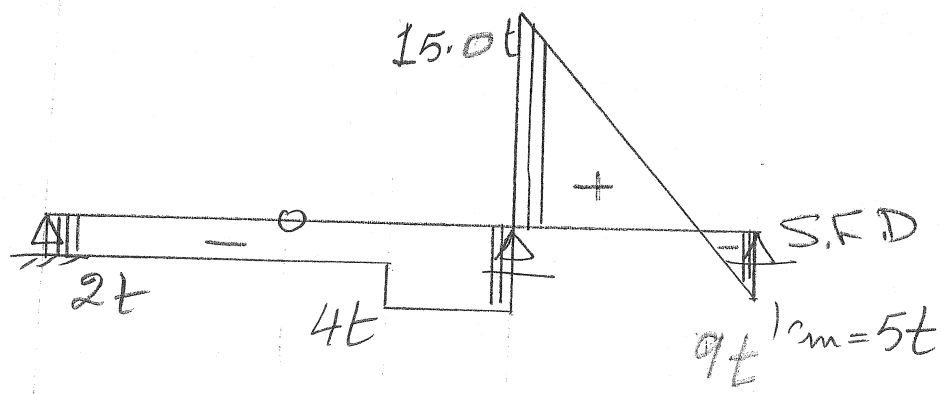
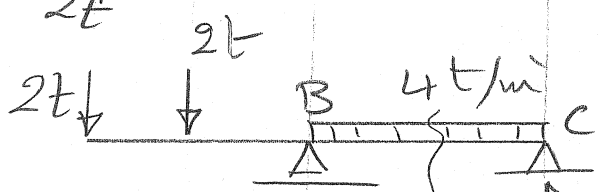
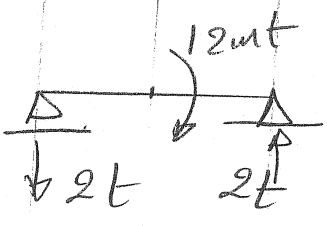
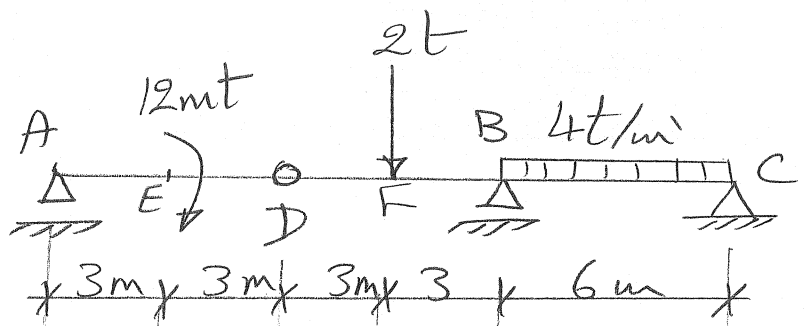
Q1

① $\sum M @ C = 0$

$2 \times 12 + 2 \times 9$
 $+ 4 \times 6 \times 3 - 6 Y_B = 0$
 $\Rightarrow Y_B = 19.0 t$

② $\sum F_y = 0$

$2 + 2 + 4 \times 6 - 19.0 - Y_C = 0$
 $\Rightarrow Y_C = 9.0 t$

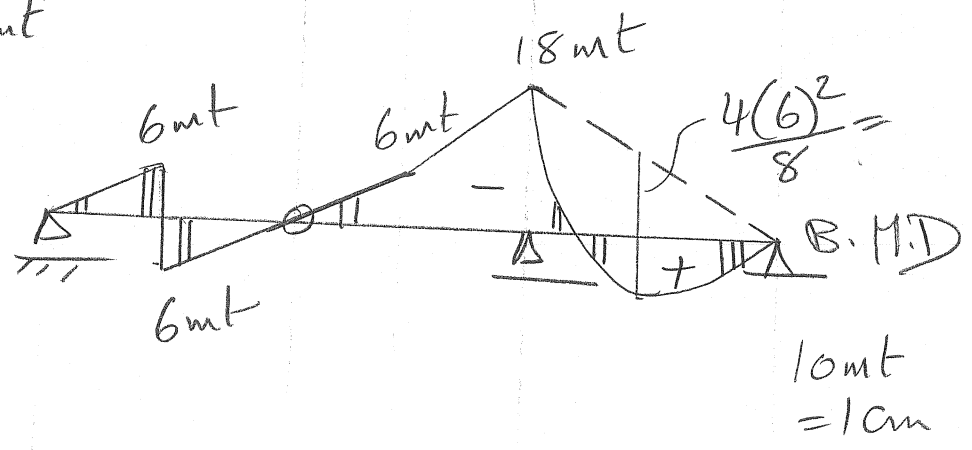


$M_E = -2 \times 3 = -6 tm$
 6ft

$M_{ER} = -6 + 12 = +6 mt$

$M_F = -2 \times 3 = -6 mt$

$M_B = -2 \times 6 - 2 \times 3$
 $= -18 mt$



Q2

$\sum M @ a = 0$

$$6 \times 1.5 + 4 \times 4 \times 4 + 3 \times 6 - 5 Y_b = 0$$

$$\therefore Y_b = 18.2 t$$

$\sum F_y = 0$

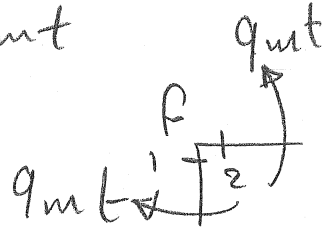
$$\therefore Y_a + 18.2 - 4 \times 4 - 3 = 0$$

$$\therefore Y_a = 0.8 t$$

$M_c = 6 \times 1.5 = 9 mt$

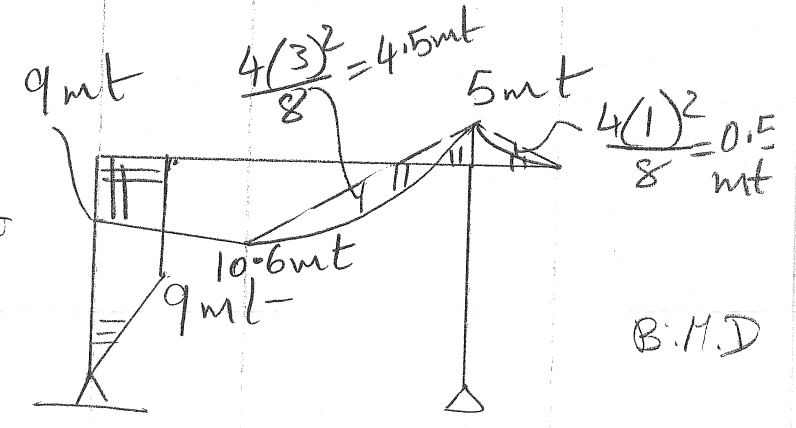
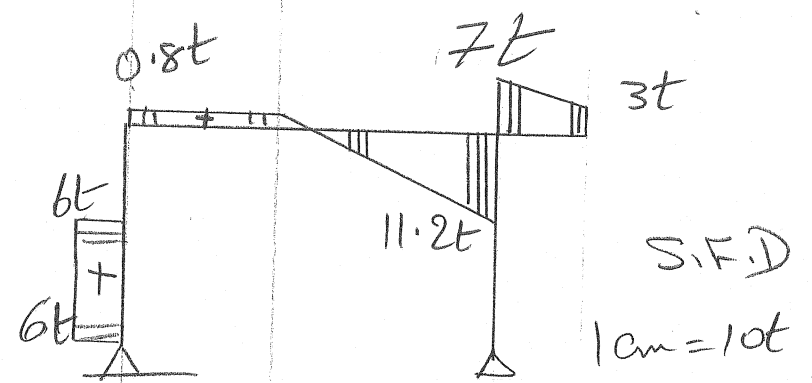
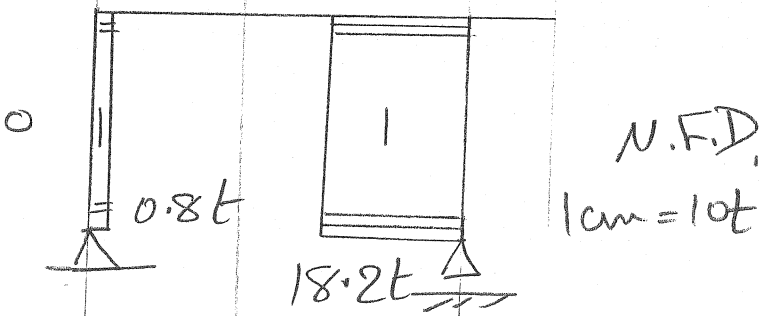
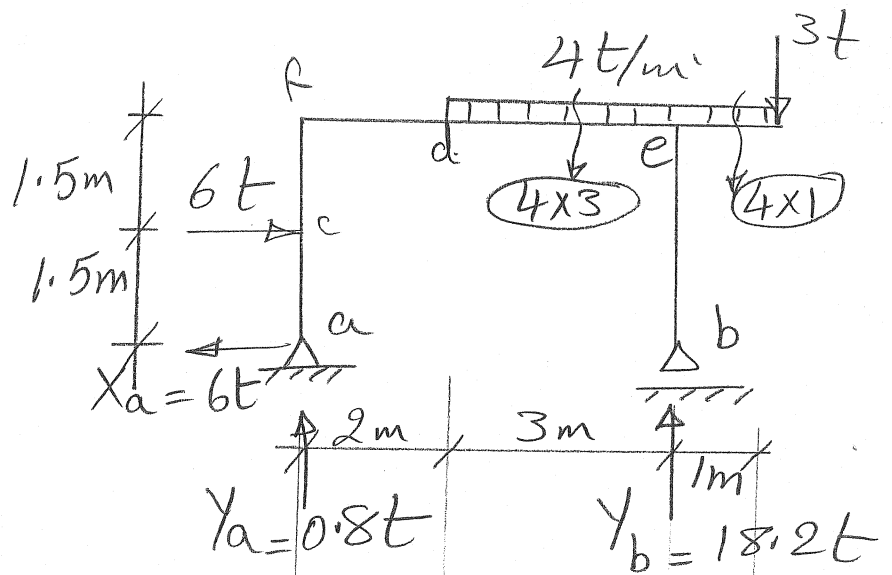
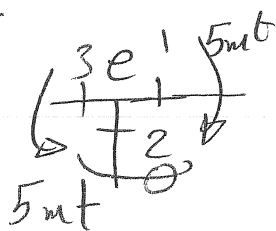
$M_{F_1} = 6 \times 3 - 6 \times 1.5 = 9 mt$

$M_d = 0.8 \times 2 + 6 \times 3 - 6 \times 1.5 = 10.6 mt$



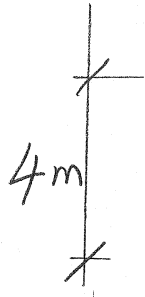
$M_{e_1} = -3 \times 1 - 4 \times 1 \times 0.5$

$M_{e_1} = -5 mt$



Q3

$\tan \theta = \frac{4}{3}$
 $\sin \theta = 0.8$
 $\cos \theta = 0.6$



$X_a = 4.08t$
 $Y_a = 17.9t$

$X_b = 4.08$
 $Y_b = 22.1$

① $\sum M @ a = 0$

$14 \times 1.5 + 4 \times 4 \times 5$
 $- 10 Y_b + 10 \times 12 = 0$

$\Rightarrow Y_b = 22.1$

② $\sum F_y = 0$

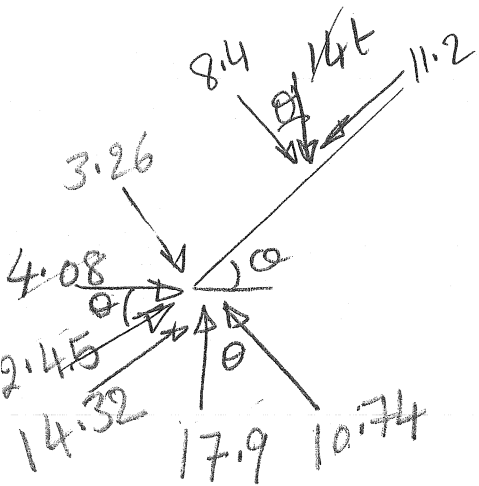
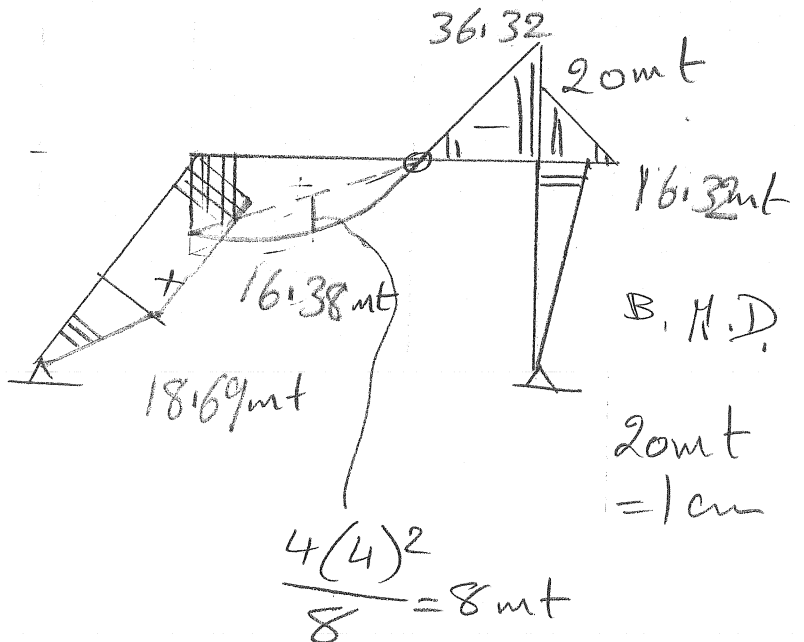
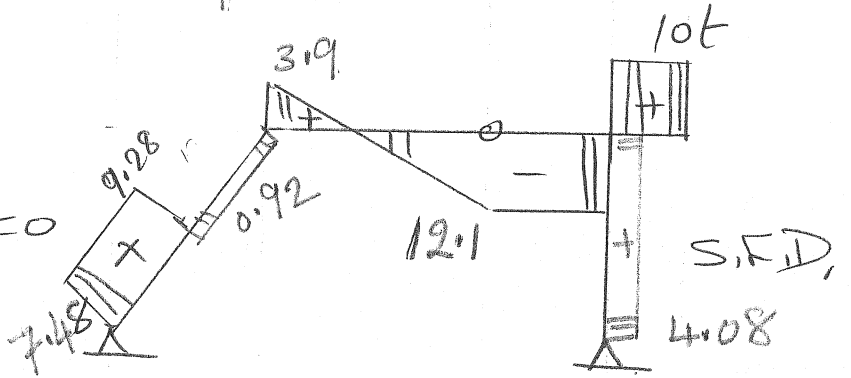
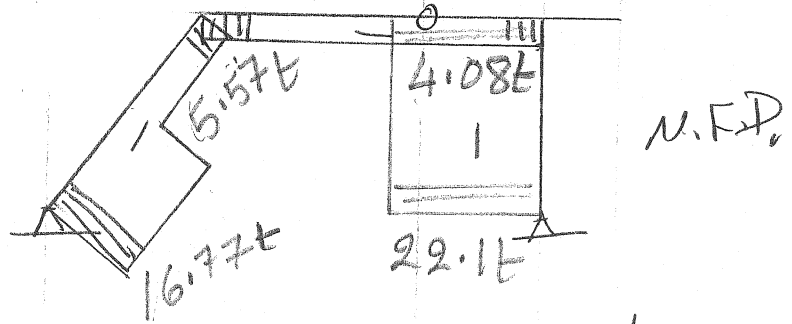
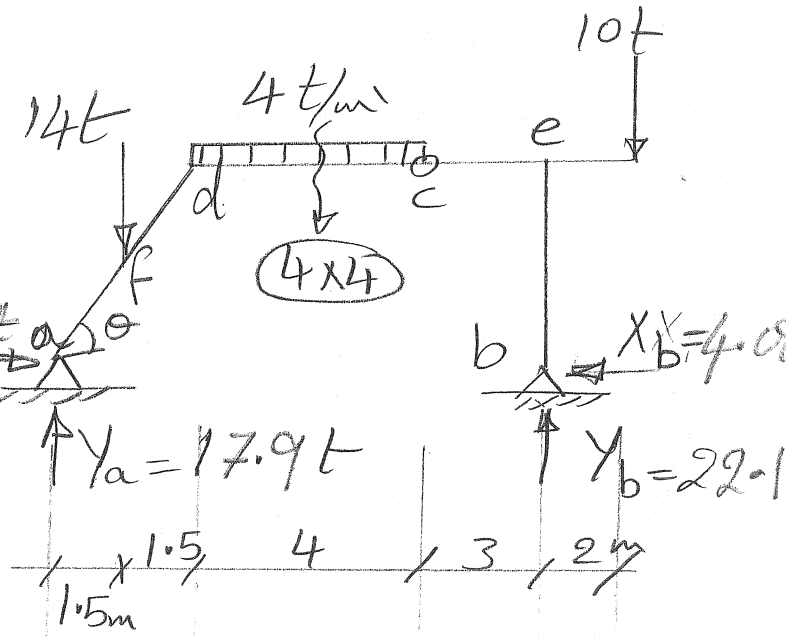
$-14 - 4 \times 4 - 10 + Y_a + Y_b = 0$

$\Rightarrow Y_a = 17.9t$

③ $\sum M_{CR} = 0$

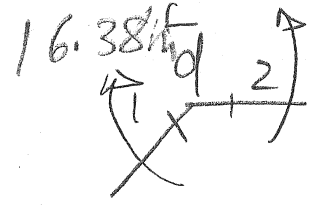
$10 \times 5 + 4 X_b - 22.1 \times 3 = 0$

$\Rightarrow X_b = 4.08$



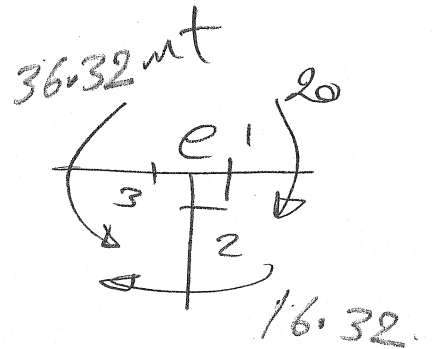
$$M_f = 17.9 \times 1.5 - 4.08 \times 2$$

$$= 18.69 \text{ mt}$$



$$M_{e_1} = -10 \times 2 = -20 \text{ mt}$$

$$M_{e_2} = -4.08 \times 4 = -16.32 \text{ mt}$$



$$M_{d_1} = -4.08 \times 4 - 14 \times 1.5 + 17.9 \times 3$$

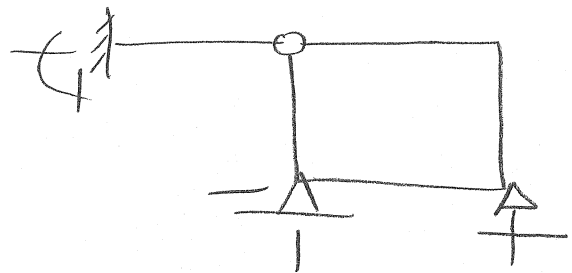
$$= 16.38 \text{ mt}$$

Q4

$$u = 6 + 3 = 9$$

$$E = 3 + (3 - 1) = 5$$

\therefore Stable & 4 times st. indep.



Higher Technological Institute
10th Ramadan City
(6th October Branch)
Department of Civil Engineering

Course : Theory of Structures(2) (CT 112)
 Examiner: Dr.Manal Kamal Zaki

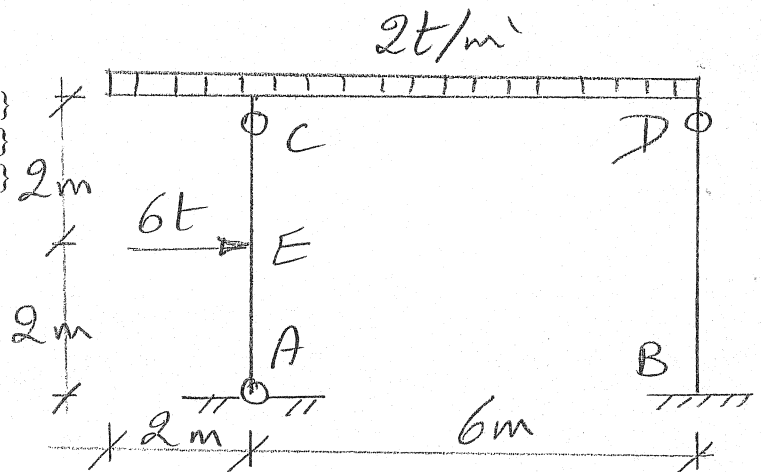
Term : Jan.-May 2018
 Time : 90 min

Final Exam

Question 1 {16 Marks}

For the shown frame:

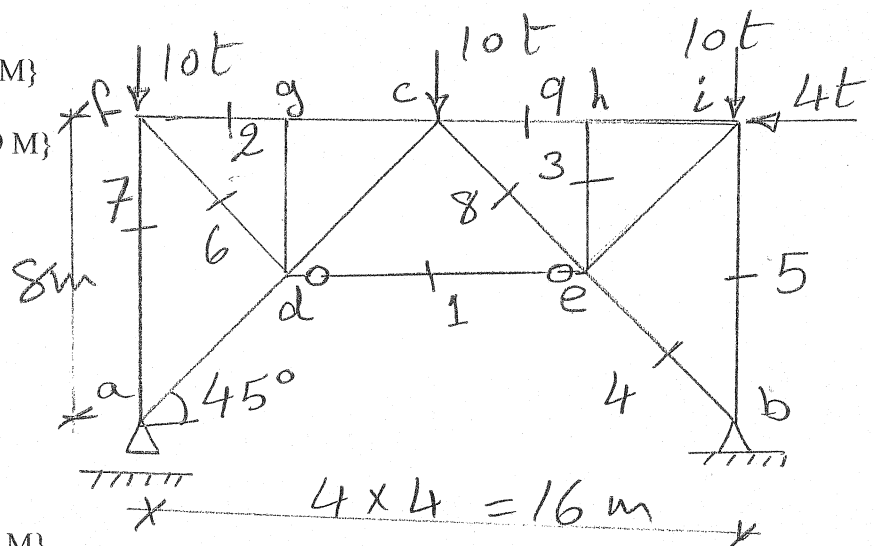
1. Find the reactions. [a2] {4 M}
2. Draw the N.F.D., Q.F.D. [a2,b3,c2] {8 M}
3. Draw the B.M.D. [a2,b3,c2] {4 M}



Question 2 {12 Marks}

For the shown truss:

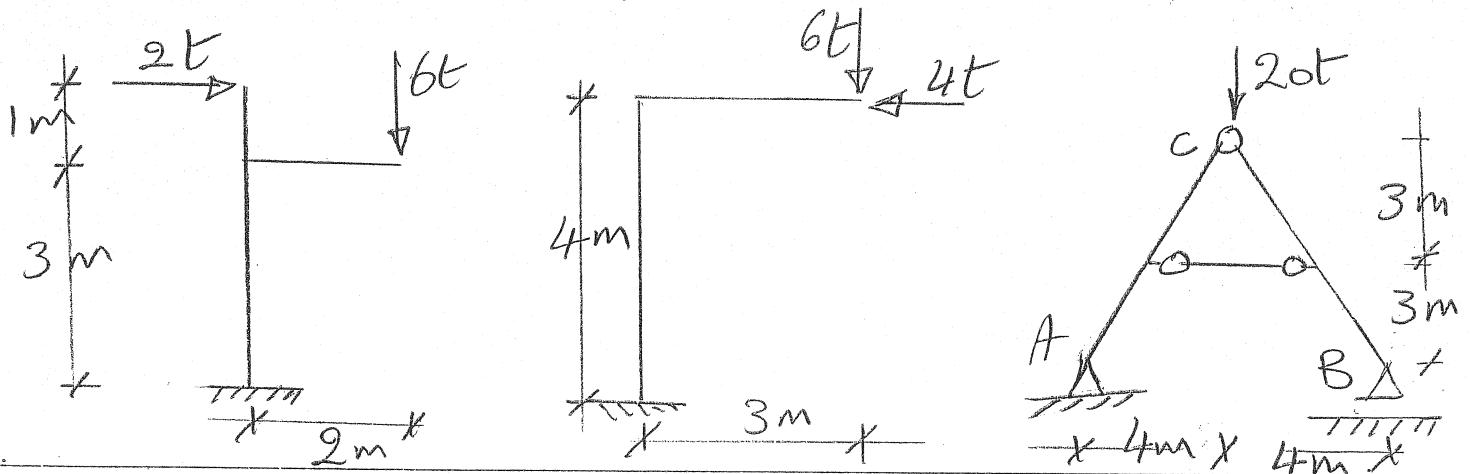
1. Find the reactions. [a2] {3M}
2. Find the normal forces in the marked members [a3,b3,c3] {9 M}



Question 3 {12 Marks}

For the shown structures:

1. Find the forces in the link members.
2. Draw the B.M.D. only [a2,a4,c4] {12 M}



Examination committee: 1-Name
 2-Name

Signature
 Signature

Q1

① $\sum M @ C = 0$
lower

$6 \times 2 - X_a \times 4 = 0$

$\therefore X_a = 3t$

② $\sum F_x = 0$

$\therefore 6 - 3 - X_B = 0$

$\therefore X_B = 3t$

③ $\sum M @ D_{lower} = 0$

$3 \times 4 - M_B = 0$

$\therefore M_B = 12mt$

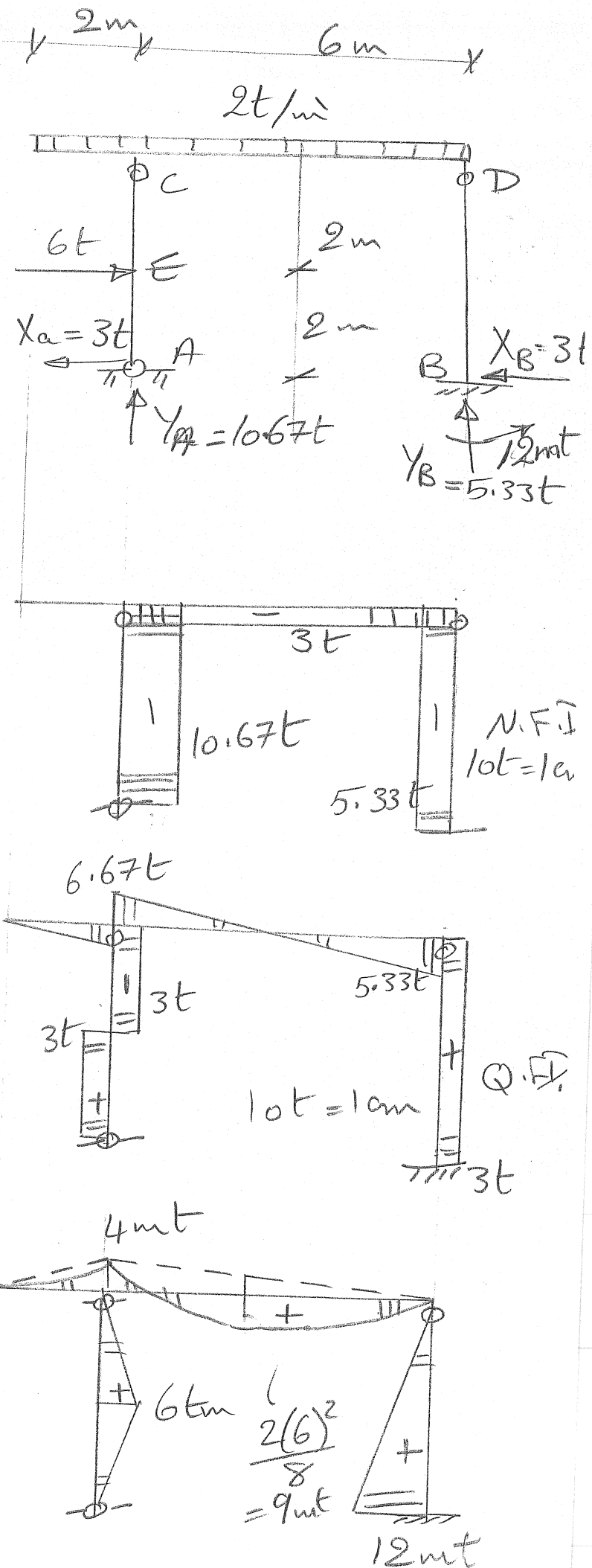
④ $\sum M @ A = 0$

$6 \times 2 + 2 \times 8 \times 2$

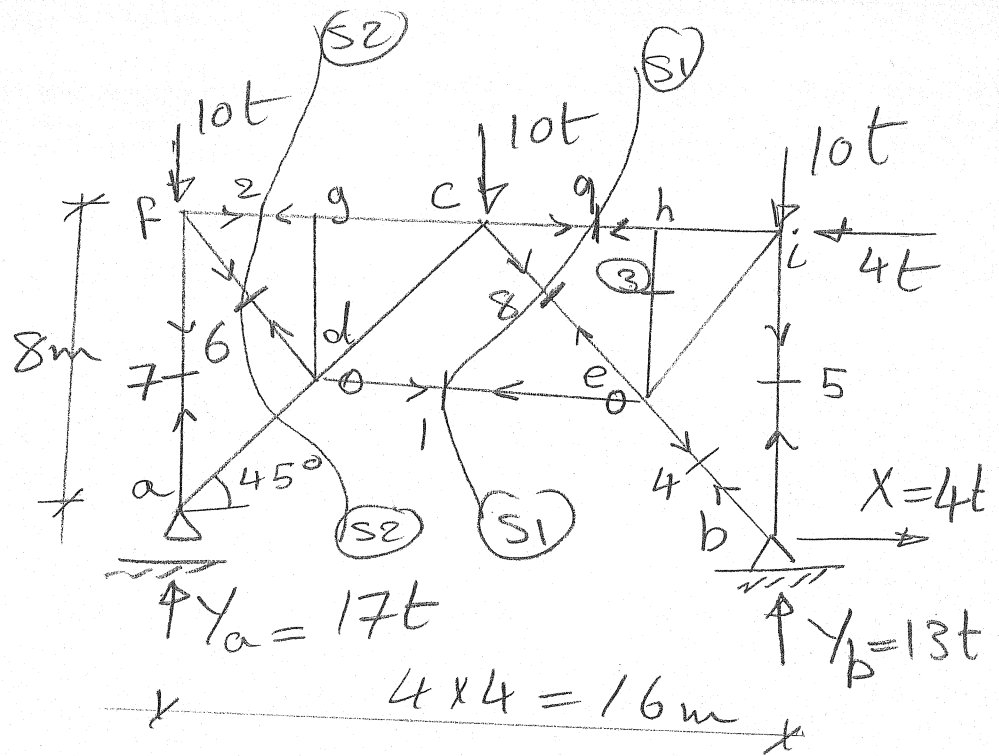
$- 12 - 6 Y_B = 0$

$\therefore Y_B = 5.33t$

$M_E = 3 \times 2 = 6mt$



Q2



$$\sum M @ a = 0$$

$$10 \times 8 + 10 \times 16 - 4 \times 8 - 16 Y_b = 0$$

$$Y_b = 13t$$

Sec S1-S1 $\sum M @ c_{left} = 0$

$$(17 - 10) \times 8 - F_1 \times 4 = 0 \quad \therefore \boxed{F_1 = +14t}$$

tens.

Sec S2-S2 $\sum M @ d_{left} = 0$

$$(17 - 10) \times 4 - F_2 \times 4 = 0 \quad \therefore \boxed{F_2 = -7t}$$

Joint h $\sum F_y = 0 \quad \therefore \boxed{F_3 = 0}$

comp.

Joint b $\sum F_{xc} = 0$

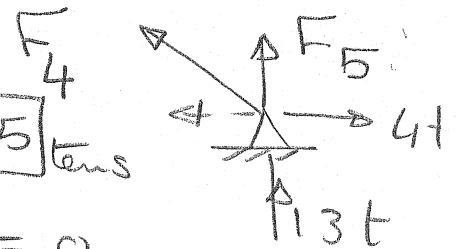
$$\therefore F_4 \cos 45 - 4 = 0 \quad \therefore \boxed{F_4 = +5.65}$$

tens

$$\sum F_y = 0 \quad \therefore F_4 \sin 45 + F_5 + 13 = 0$$

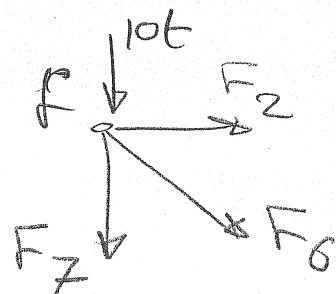
$$\therefore \boxed{F_5 = -17t}$$

comp



Joint P : $\Sigma F_x = 0$

$$F_2 + F_6 \cos 45 = 0$$
$$\therefore F_2 = -7t$$



$$\therefore \boxed{F_6 = +9.9t} \text{ tens}$$

$$\Sigma F_y = 0$$

$$\therefore 10 + F_7 + F_6 \sin 45 = 0$$

$$10 + F_7 + 9.9 \sin 45 = 0$$

$$\therefore \boxed{F_7 = -17t} \text{ comp.}$$

Sec S1-S1' $\Sigma F_{y,t} = 0$

$$13 - 10 + F_8 \sin 45 = 0$$

$$\therefore \boxed{F_8 = -4.24t} \text{ comp}$$

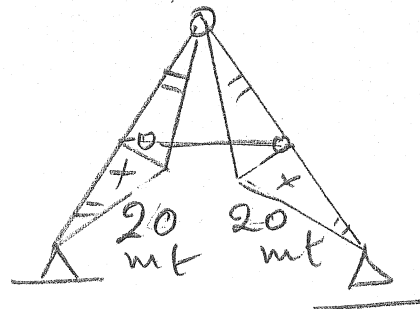
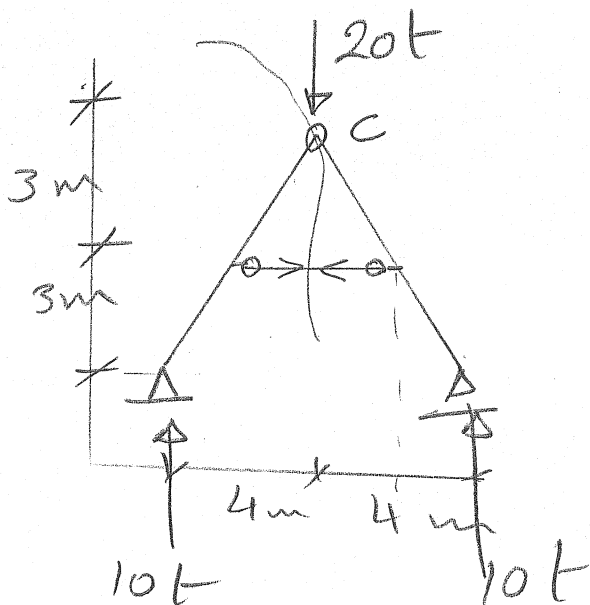
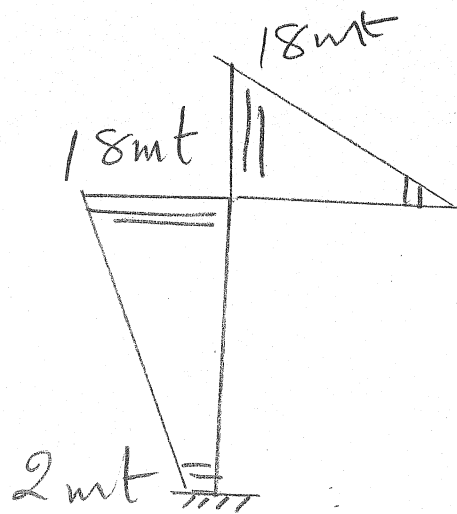
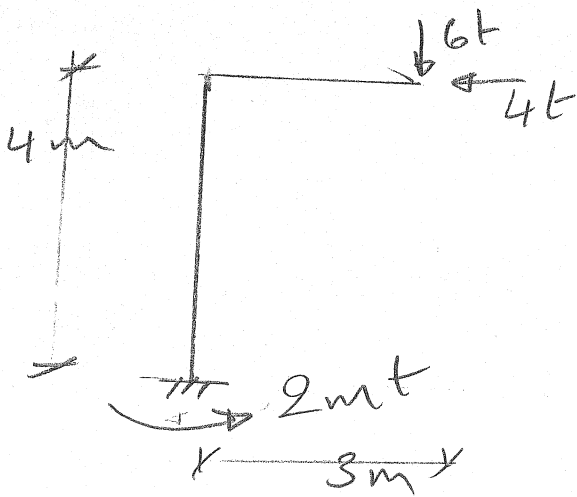
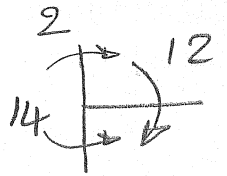
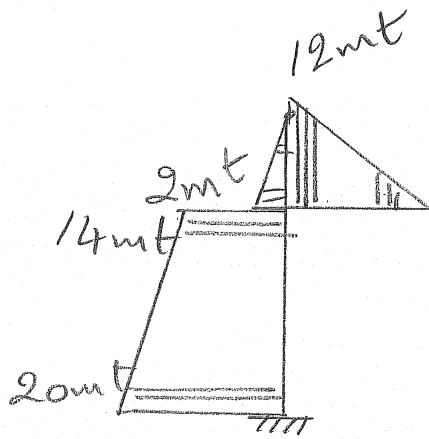
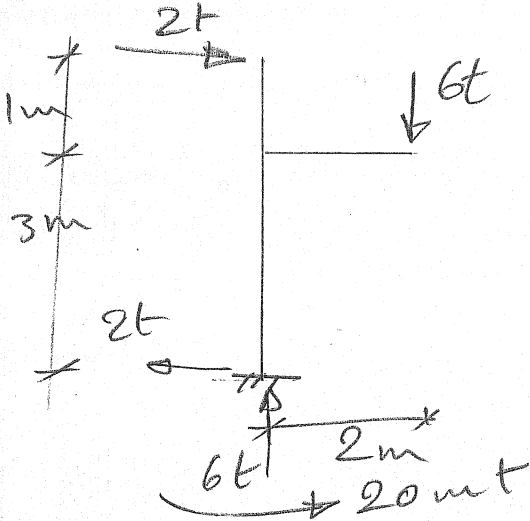
$$\Sigma F_{x,t} = 0$$

$$4 - 4 - F_9 - F_1 - F_8 \cos 45 = 0$$

$$\therefore -F_9 - 14 + 4.24 \cos 45 = 0$$

$$\therefore \boxed{F_9 = -11t} \text{ comp}$$

Q3



$\sum M @ c \text{ left} = 0$

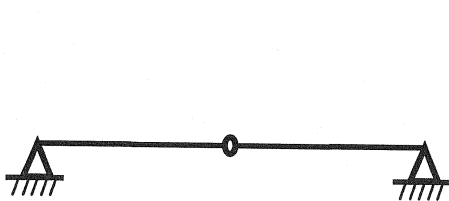
$3F - 10 \times 4 = 0$

$F = 13.33t$

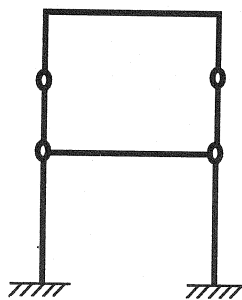


Q1 Marks (12) ILO's(a, b, and c)

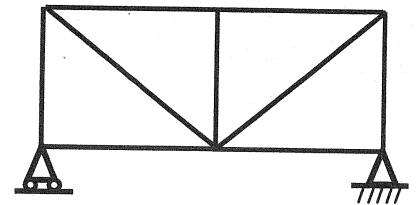
Check stability of the following structures:



Un stable

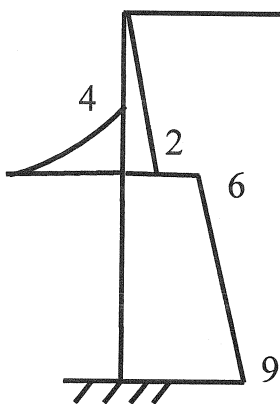


Un stable

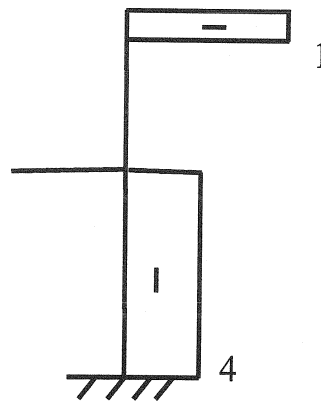


Stable & determinate

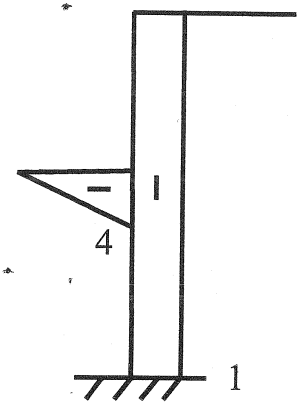
Q2 Marks (18) ILO's(a, b, and c)



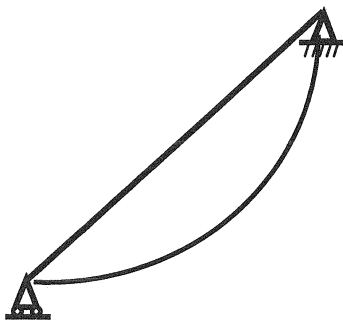
B.M.D



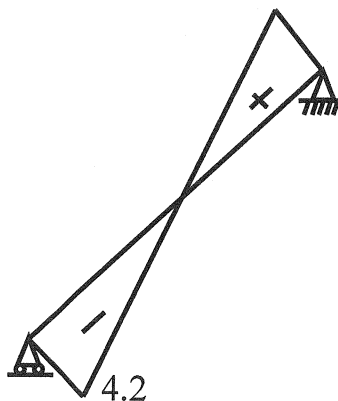
N.F.D



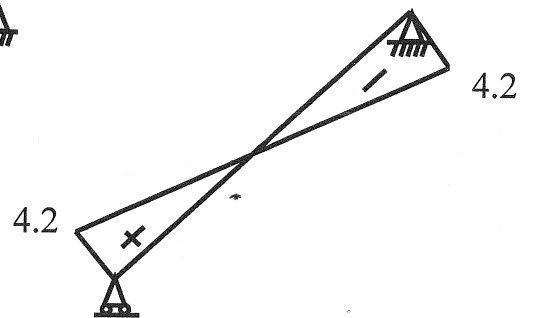
S.F.D



B.M.D



N.F.D



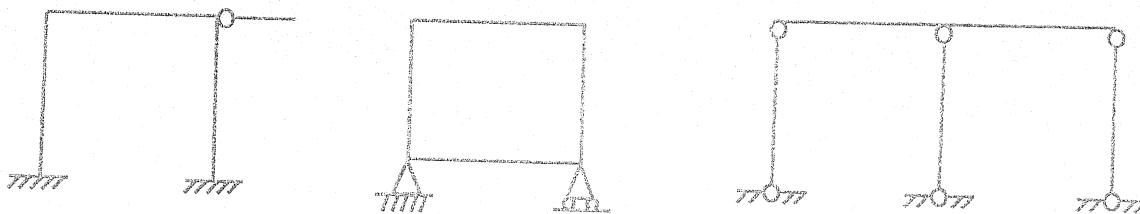
S.F.D

Handwritten signature



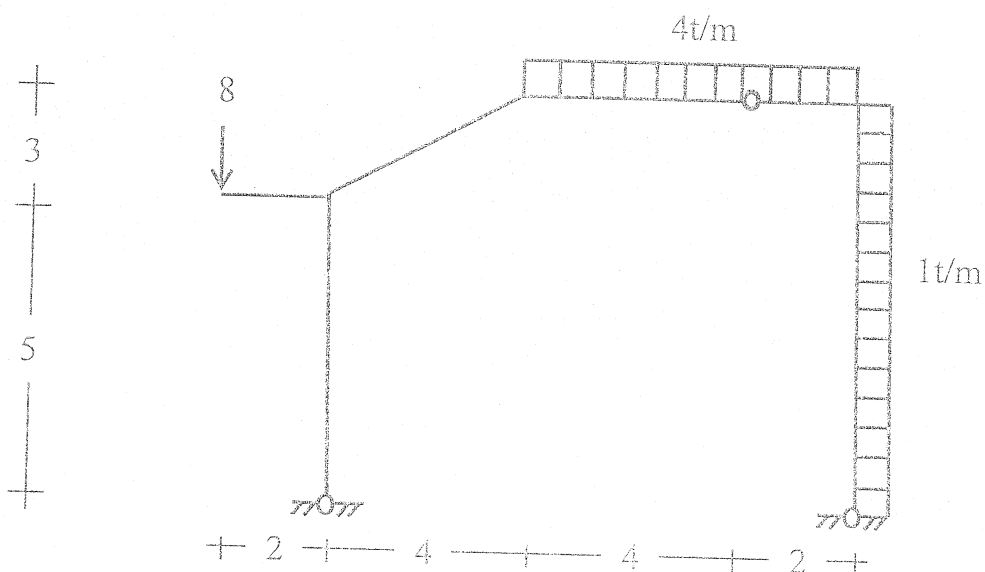
Q1 Marks (12) ILO's(a, b, and c)

Check stability of the following structures:

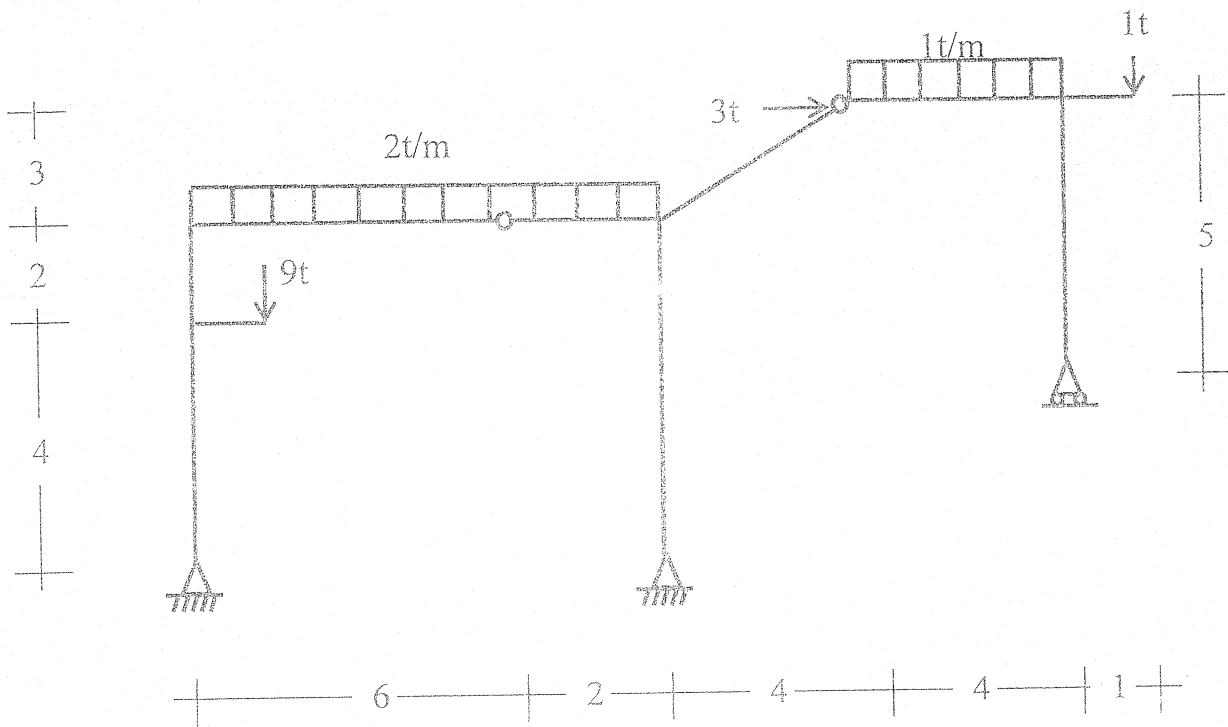


Q2 Marks (20) ILO's(a, b, and c)

Draw N.F.D , S.F.D, B.M.D for the following structures

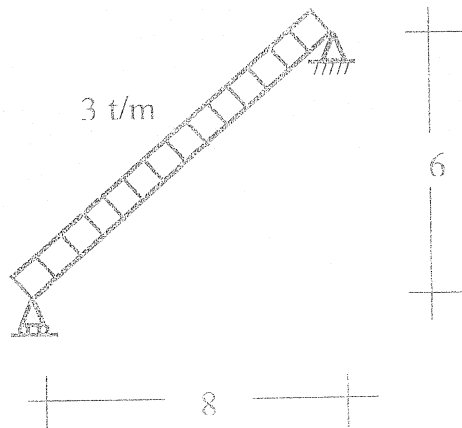


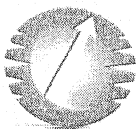
Handwritten signature



Q3Marks (8) ILO's(a, b, and c)

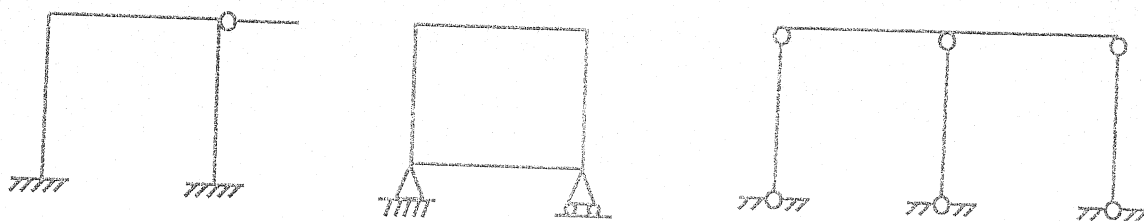
Draw N.F.D , S.F.D, B.M.D for the following structure





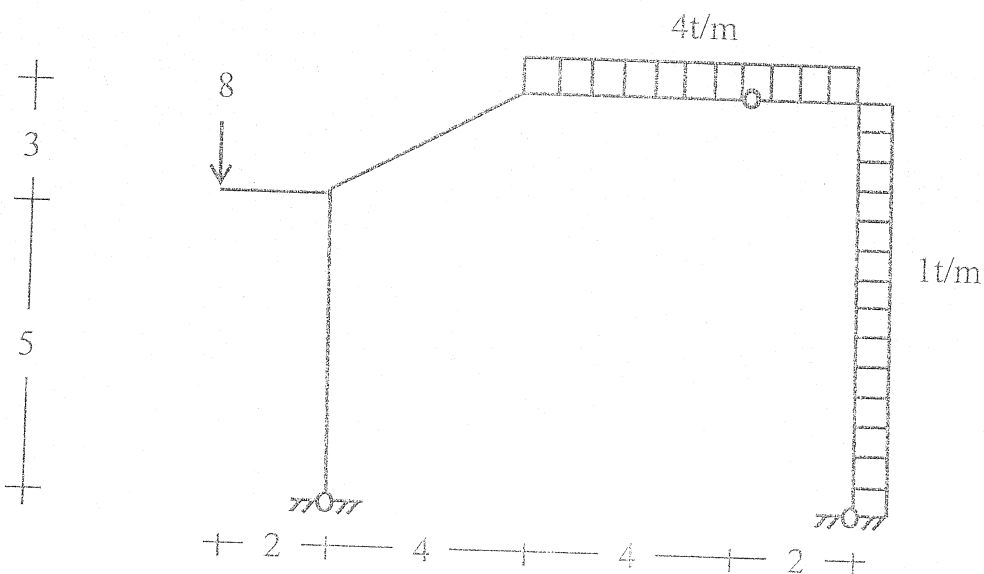
Q1Marks (12) ILO's(a, b, and c)

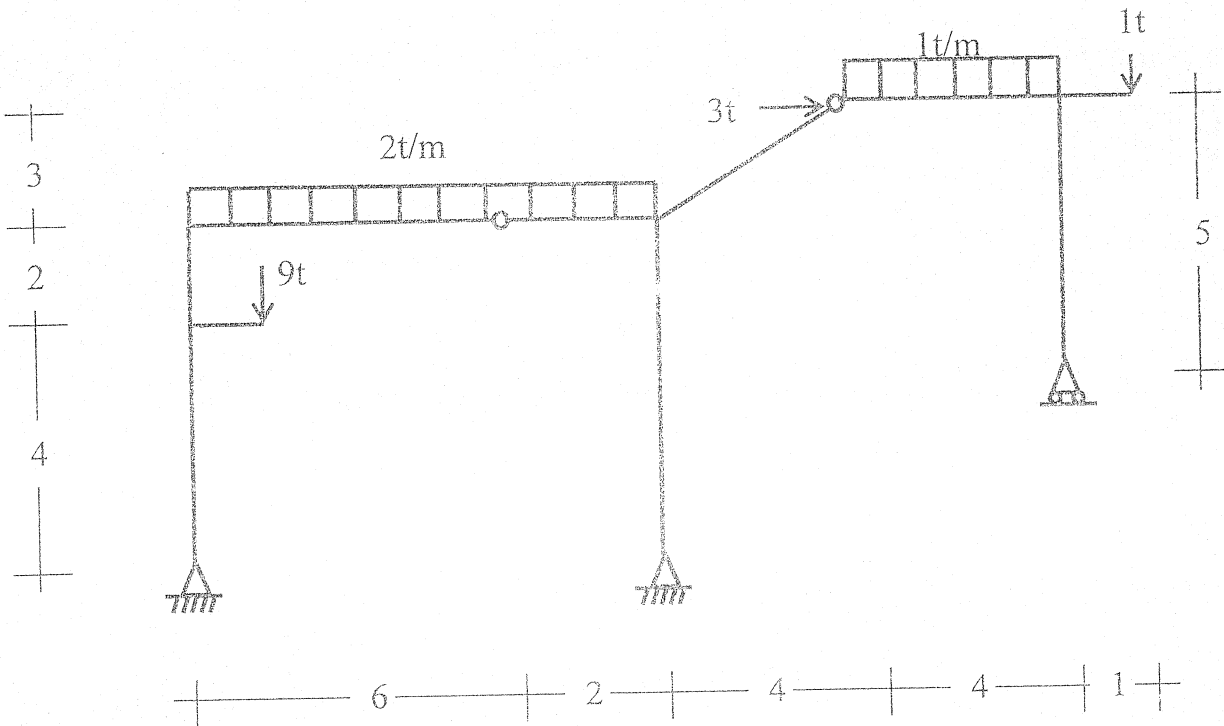
Check stability of the following structures:



Q2Marks (20) ILO's(a, b, and c)

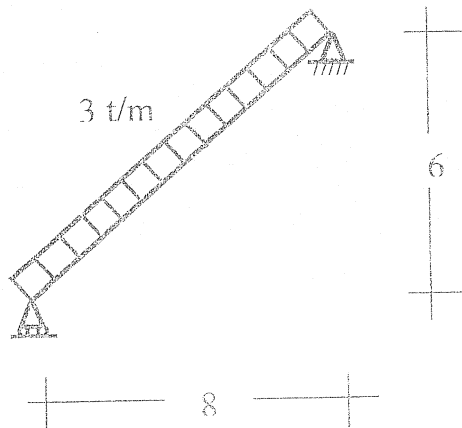
Draw N.F.D , S.F.D, B.M.D for the following structures

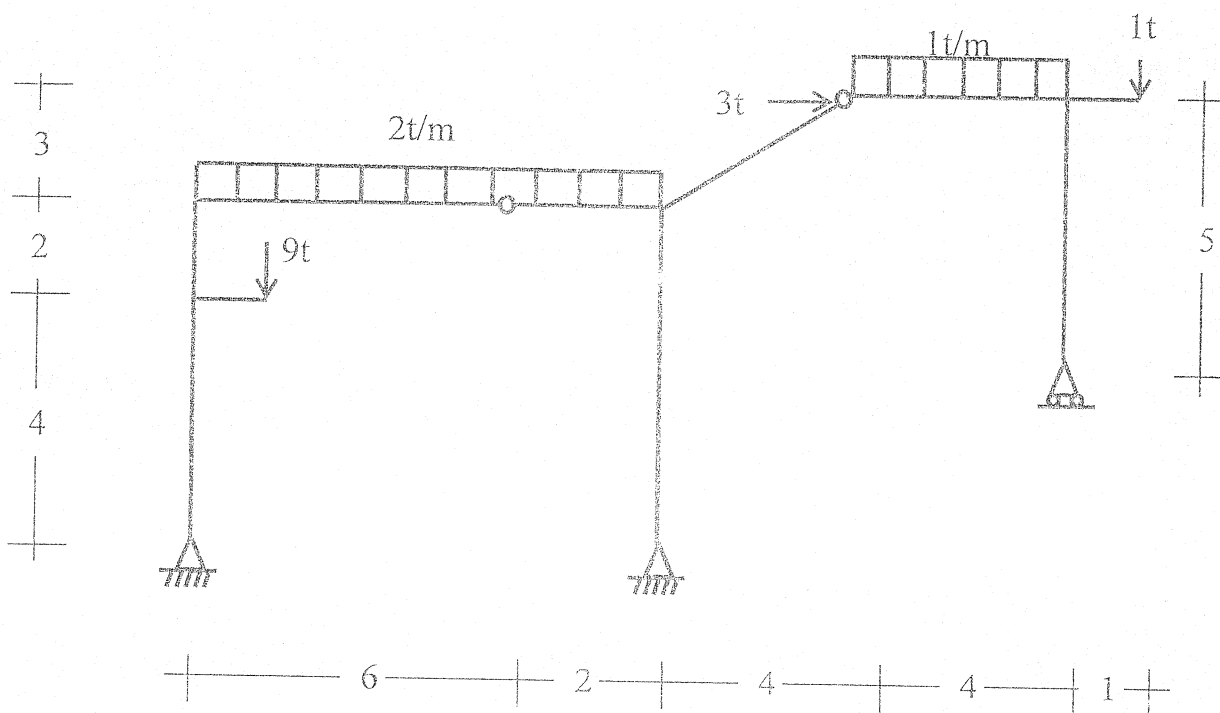




Q3Marks (8) ILO's(a, b, and c)

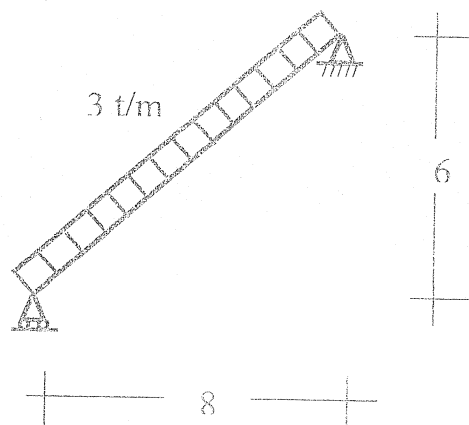
Draw N.F.D , S.F.D, B.M.D for the following structure





Q3 Marks (8) ILO's(a, b, and c)

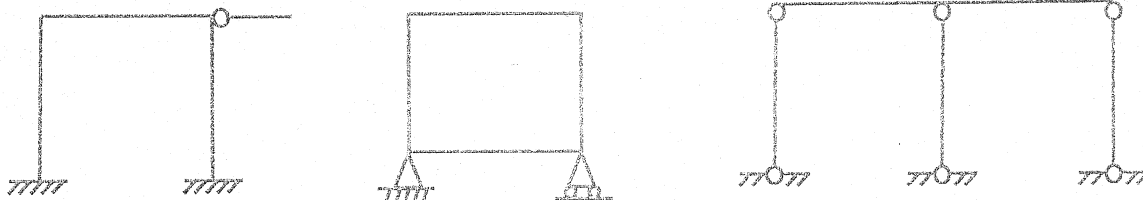
Draw N.F.D , S.F.D, B.M.D for the following structure





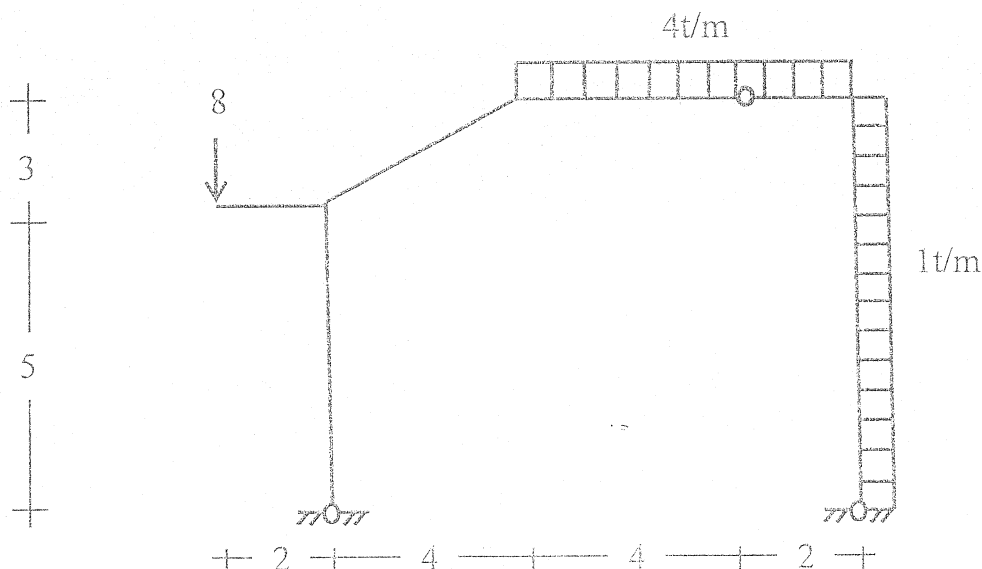
Q1Marks (12) ILO's(a, b, and c)

Check stability of the following structures:



Q2Marks (20) ILO's(a, b, and c)

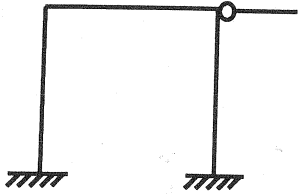
Draw N.F.D , S.F.D, B.M.D for the following structures



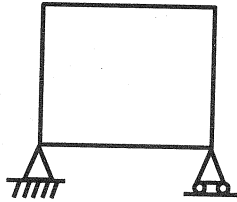


Q1 Marks (12) ILO's(a, b, and c)

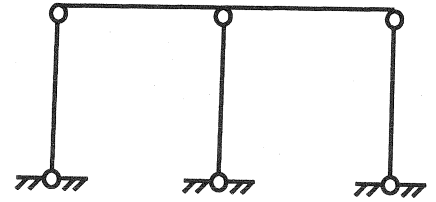
Check stability of the following structures:



Unstable



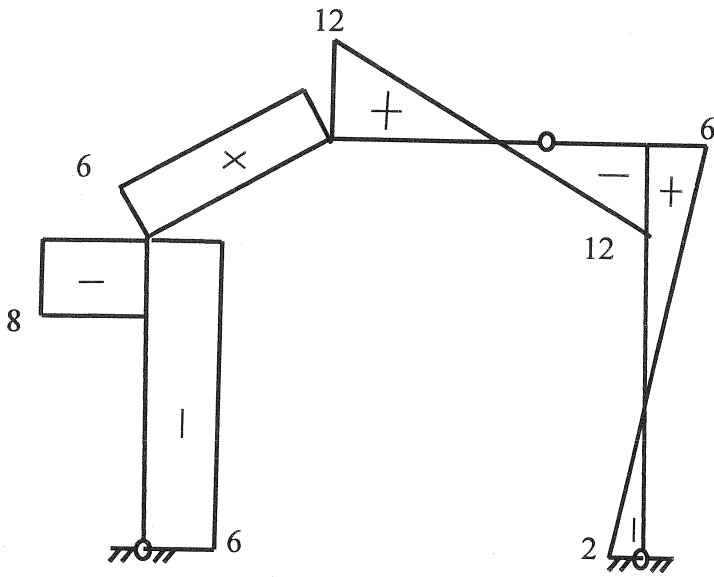
Stable and indeterminate (3 times)



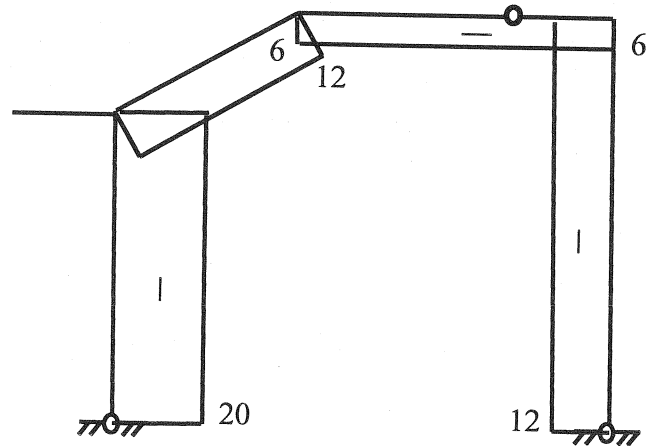
Unstable

Q2 Marks (20) ILO's(a, b, and c)

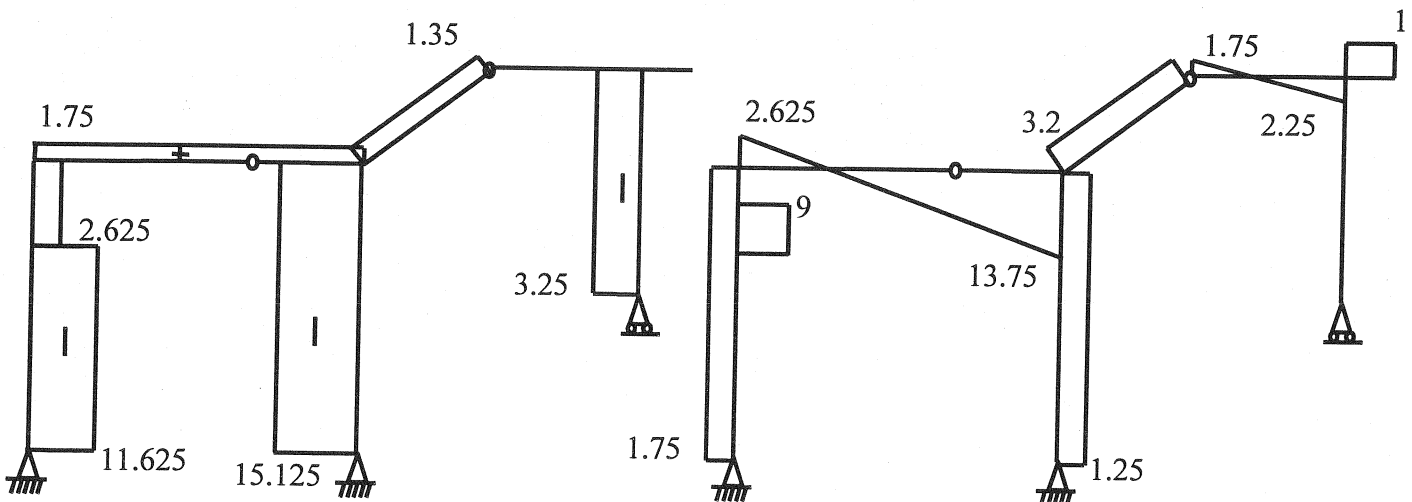
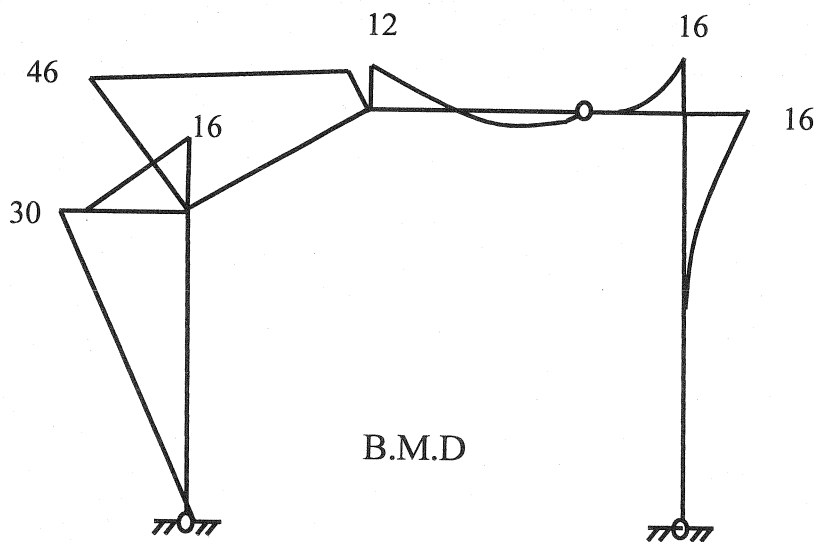
Draw N.F.D , S.F.D, B.M.D for the following structures

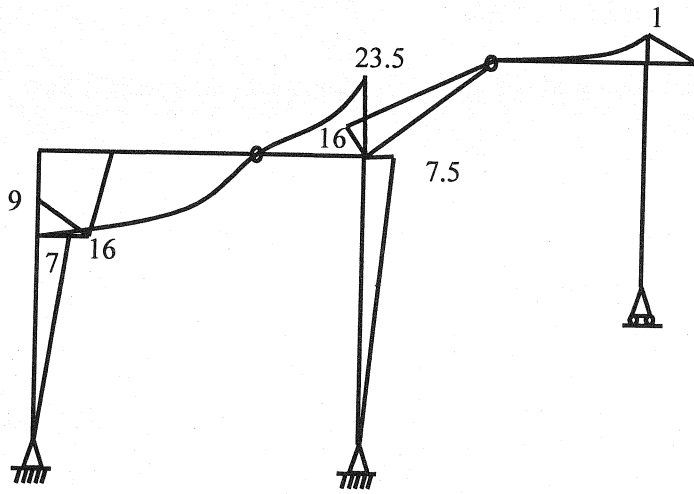


S.F.D



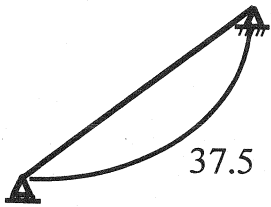
N.F.D



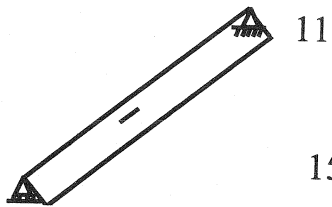



B.M.D

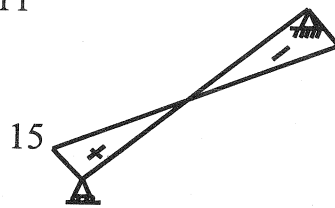
Q3Marks (8) ILO's(a, b, and c)



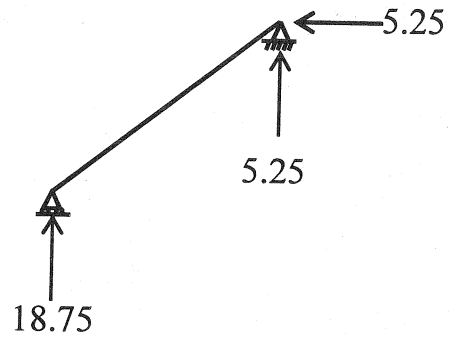
B.M.D



N.F.D



S.F.D



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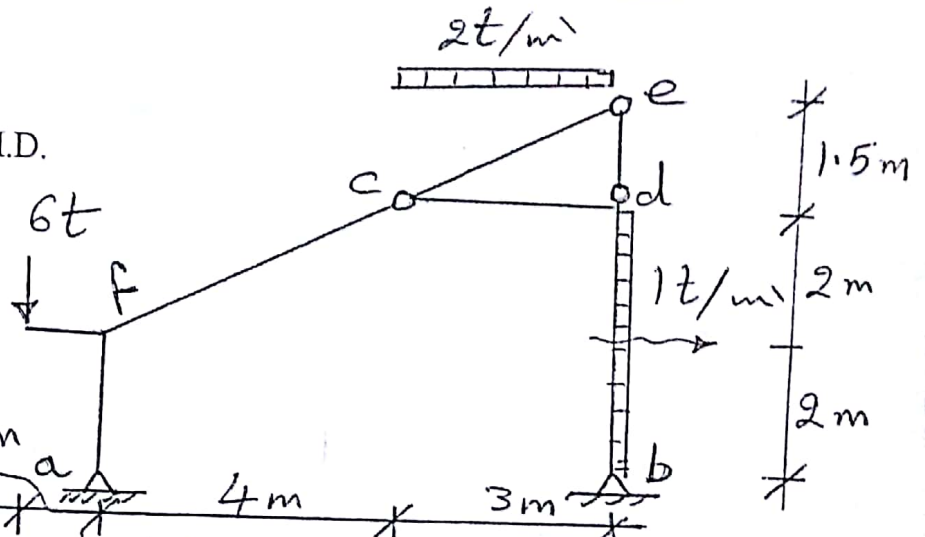
Subject: Structure 2 (CT 112)
Examiner: Examination Committee

Term: Jan.-May 2011
Time: 90 min

Final Examination

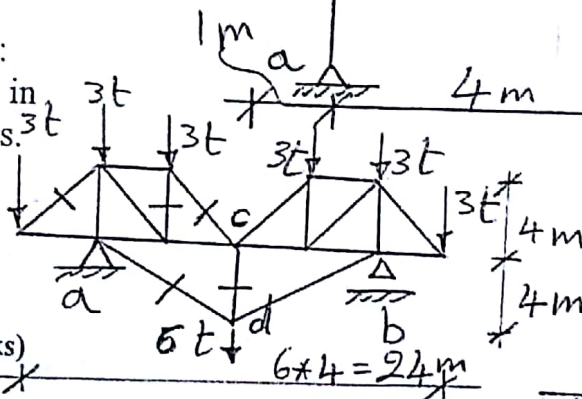
Question (1) (15 marks)

For the shown frame
- Draw the N.F.D., Q.F.D. and B.M.D.



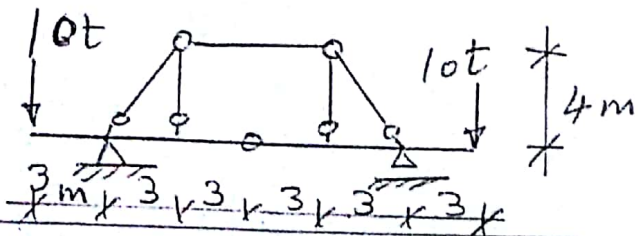
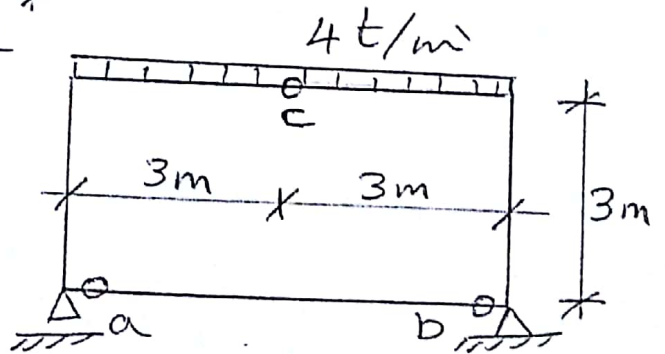
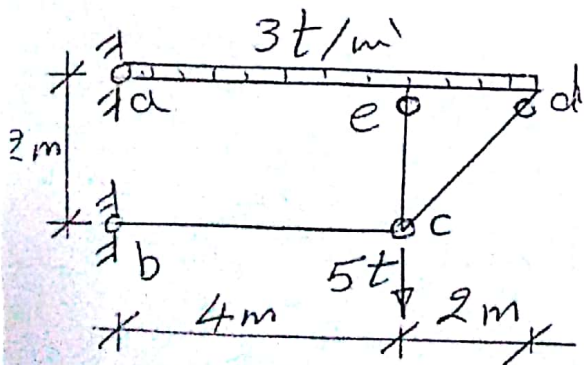
Question (2) (10 marks)

For the shown truss:
- compute the forces in the marked members.



Question (3) (15 marks)

For the shown structures:
- Compute the forces in the link members.
- Draw the B.M.D. only.

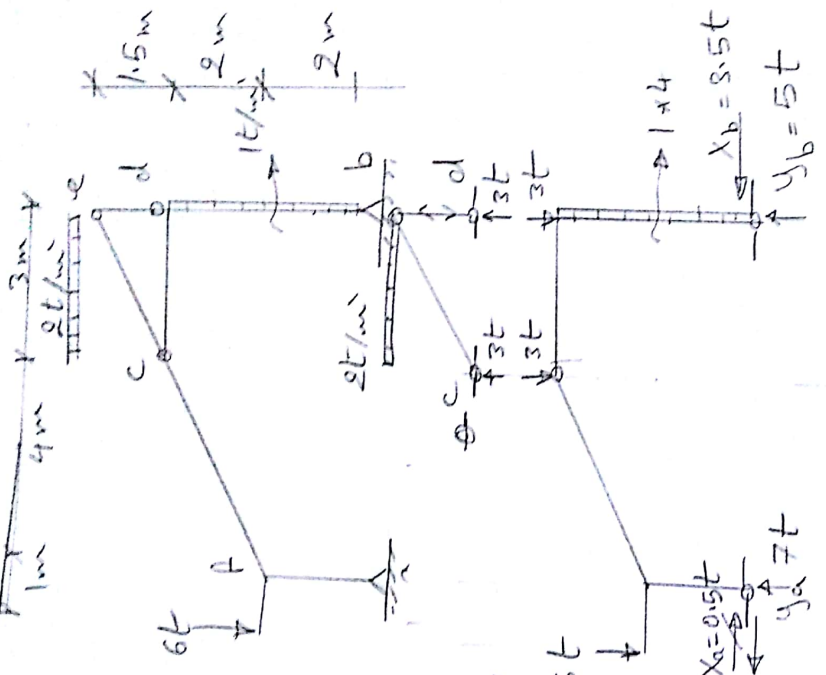


Coarse Examination Committee

Coarse Coordinator

STR 2

Q1



$$\sum H @ A = 0$$

$$1 \times 4 \times 2 + 3 \times 7 + 3 \times 4$$

$$- 6 \times 1 - Y_b \times 7 = 0$$

$$\therefore Y_b = 5t$$

$$\sum Y = 0$$

$$\therefore 6 + 3 + 3 - Y_b - Y_a = 0$$

$$\therefore Y_a = 7t$$

$$X_a = 0.5t$$

$$Y_a = 7t$$

$$X_b = 8.5t$$

$$Y_b = 5t$$

$$\sum H @ C_{left} = 0$$

$$- 6 + 5 + 4 X_a - 4 Y_b = 0$$

$$\therefore X_a = -0.5t$$

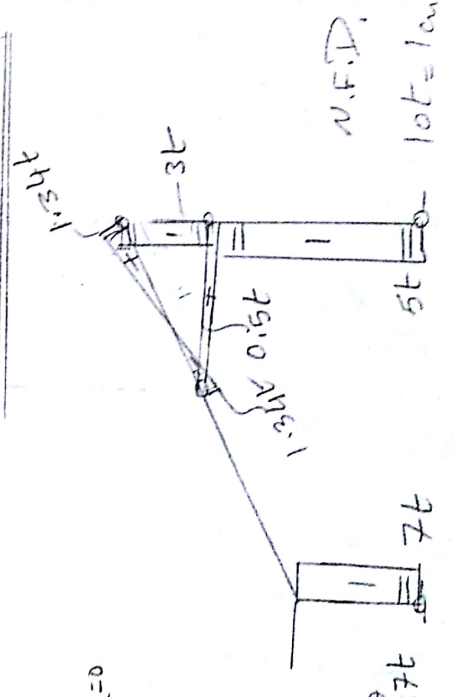
$$\tan \theta = \frac{1}{2}$$

$$\cos \theta = \frac{2}{\sqrt{5}} = 0.8944$$

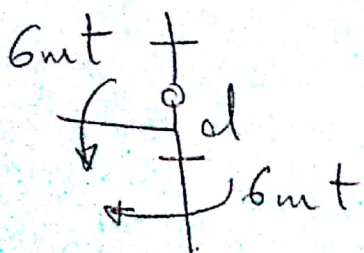
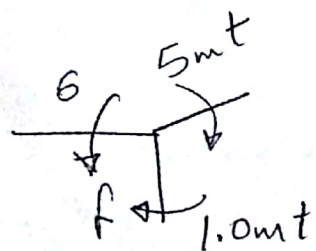
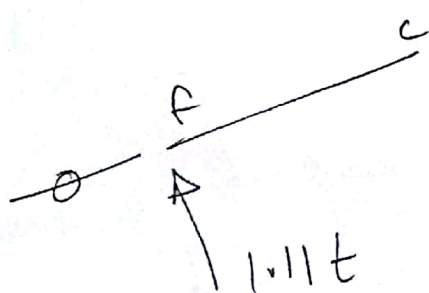
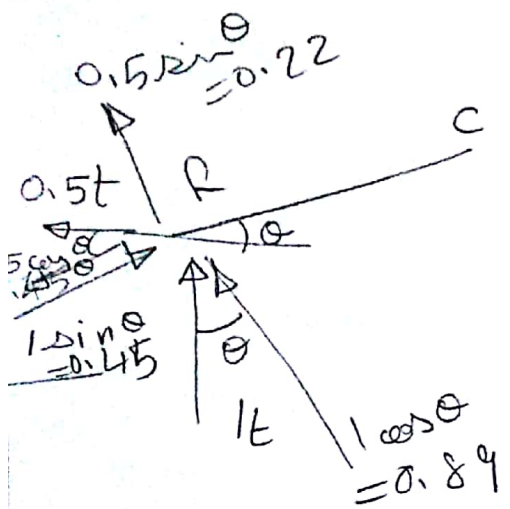
$$\sin \theta = \frac{1}{\sqrt{5}} = 0.4472$$

$$6 \cos \theta = 5.37t$$

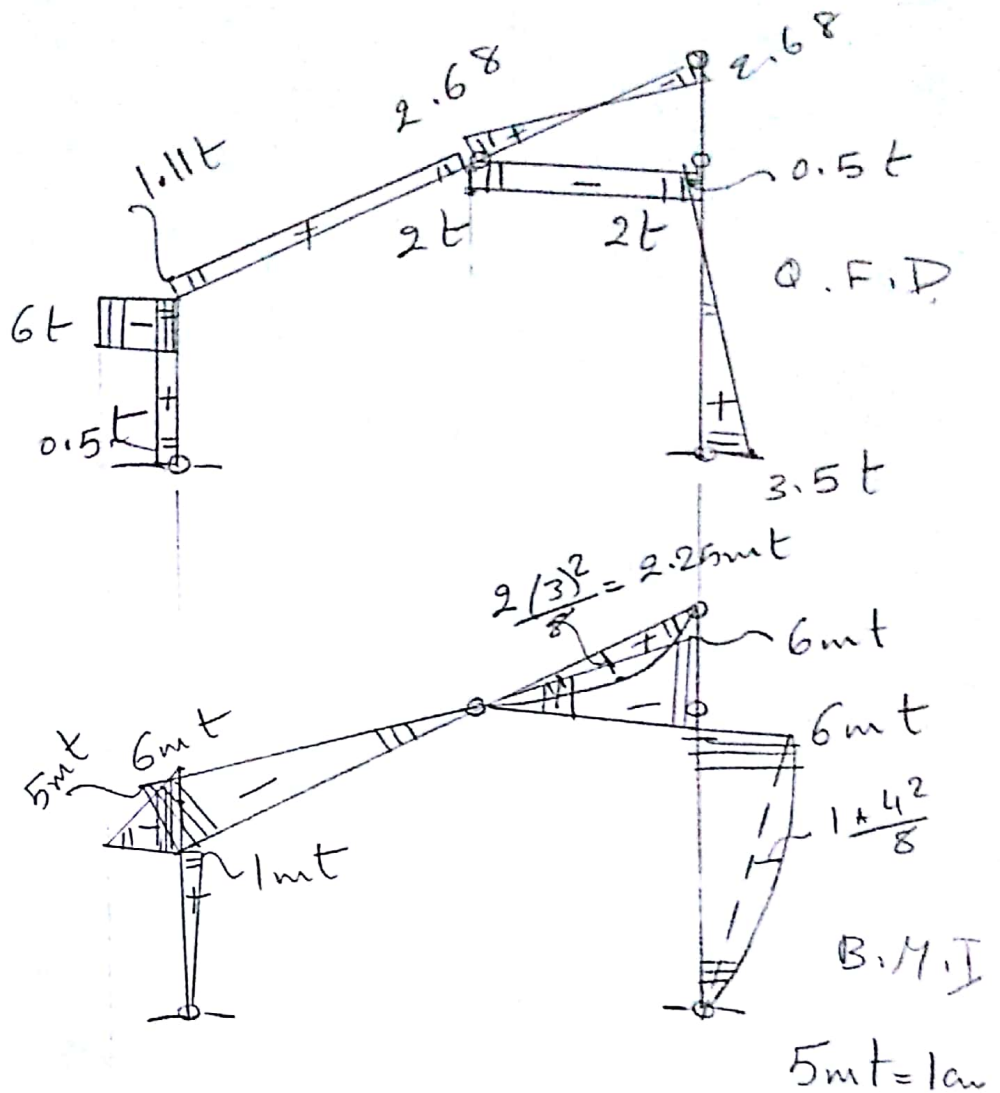
$$6 \sin \theta = 2.68t$$



$$3 \cos \theta = 2.68$$



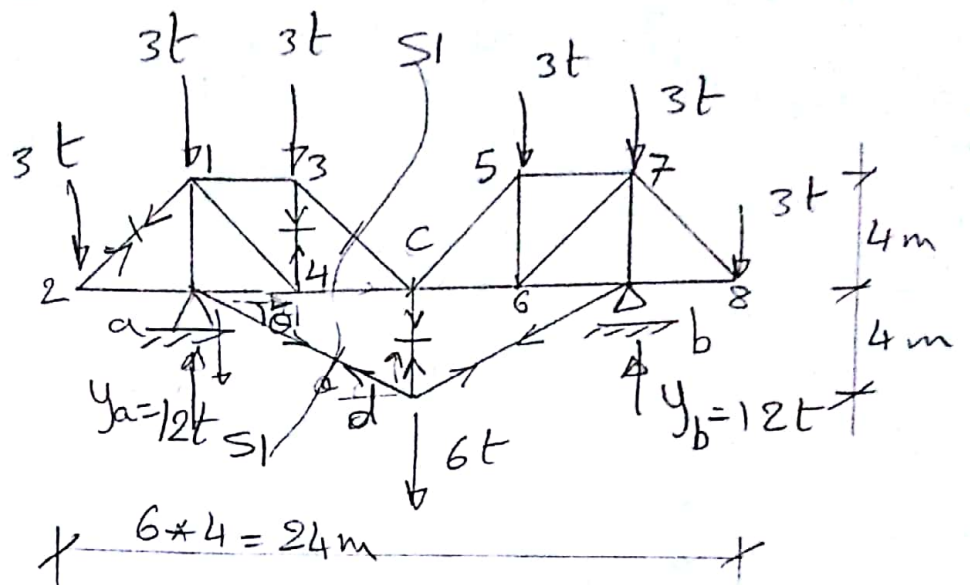
$$M_d = -3.5 \times 4 + 1 \times 4 \times 2 = -6mt \text{ m t}$$



Q 2

$$\tan \theta = \frac{1}{2}$$

$$y_a = y_b = 12t$$



Member a d

Sec SI-SI

$$\sum M @ c \text{ left} = 0$$

$$\therefore 3[12 + 8 + 4] - 12 \times 8 + F_{ad} \sin \theta \times 8 = 0$$

$$\therefore \boxed{F_{ad} = +6.71 t} \text{ tens}$$

Member c-d

Joint d

$$\sum Y = 0$$

$$\therefore 2F_{a-d} \sin \theta + F_{d-c} - 6 = 0$$

$$\therefore \boxed{F_{d-c} = \text{Zero}}$$

Member F3-c

Joint c, $\sum Y = 0$

$$\boxed{F_{3-c} = 0}$$

Member 3-4

Joint 3, $\sum Y = 0$

$$\boxed{F_{3-4} = -3t}$$

Member 1-2

Joint 2, $\sum Y = 0$

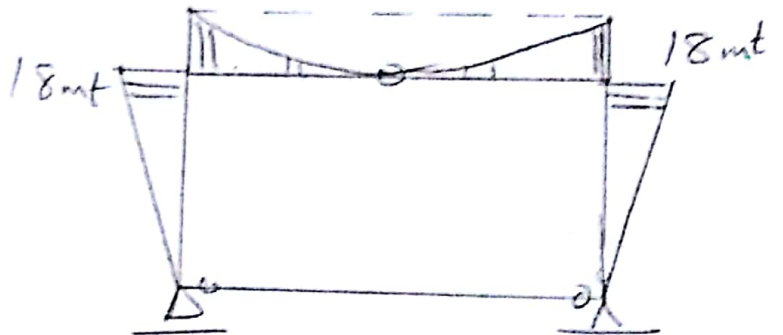
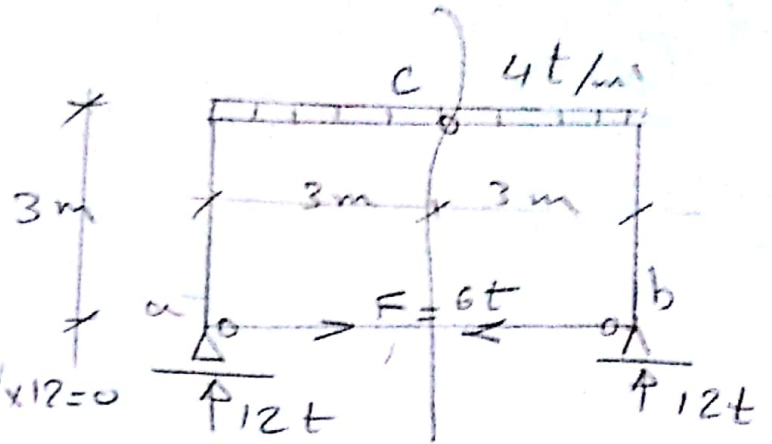
$$\therefore F_{1-2} = \frac{3}{\cos 45} = \boxed{4.24 t = F_{1-2}}$$

Q3

$$\sum M @ C = 0$$

$$\therefore 4 \times 3 \times 1.5 + F \times 3 - 3 \times 12 = 0$$

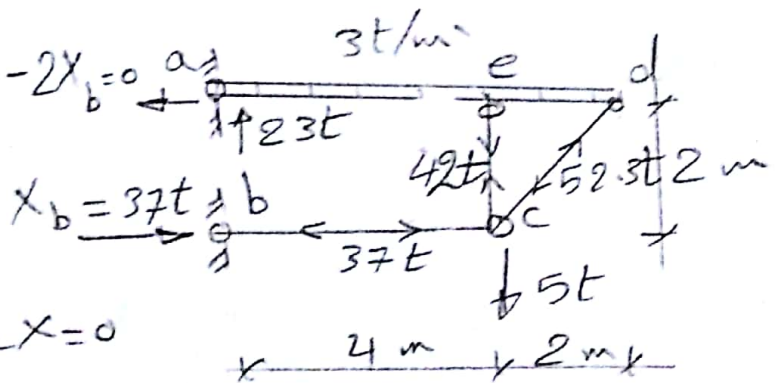
$$\therefore F = +6t$$



$$\sum M @ a = 0$$

$$\therefore -3 + 6 \times 3 + 5 \times 4 - 2X_b = 0$$

$$\therefore X_b = 37t$$



$$\frac{F_{c-d}}{\sum X = 0}$$

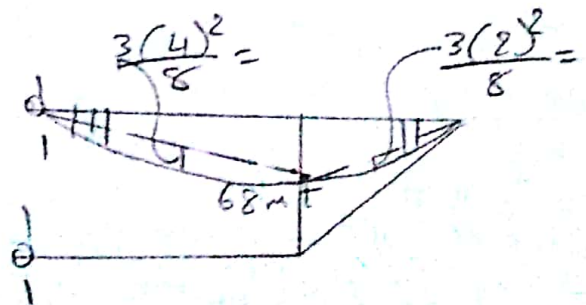
$$\therefore F_{c-d} = 52.3t$$

$$\sum Y = 0 \text{ at jt } c \rightarrow F_{ce} = 49t$$

$$F_{c-e} - F_{c-d} \cos 45 = 0$$

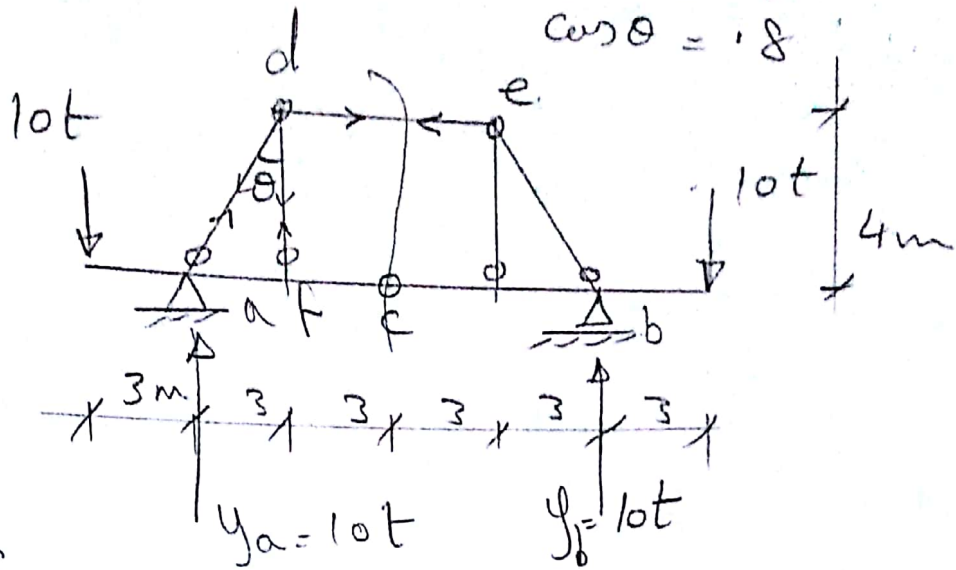
$$M_e = 23 \times 4 - 3 \times 4 \times 2$$

$$= 68 \text{ mt}$$



$\odot a = 0$

$\sin \theta = .6$
 $\cos \theta = .8$



- d-e

Sec s-s

$\sum M @ c \text{ left} = 0$

$F_{d-e} \times 4 + Y_a \times 6 - 10 \times 9 = 0$

$\therefore \boxed{F_{d-e} = 7.5t} \text{ Comp}$

Member a-d

Joint d : $\sum X = 0$

$\therefore F_{d-e} - F_{ad} \sin \theta = 0$

$\therefore \boxed{F_{ad} = +12.5} \text{ Tens.}$

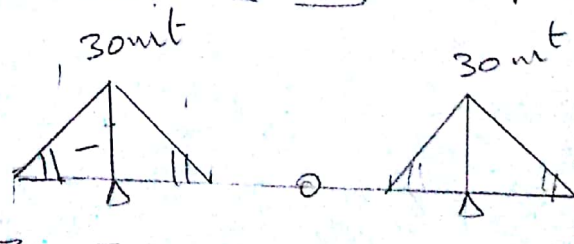
Member d-f, Joint d, $\sum Y = 0$

$\therefore F_{d-f} + F_{ad} \cos \theta = 0$

$\therefore \boxed{F_{d-f} = -10t} \text{ Comp}$

$M_f = -10 \times 6$
 $+ 10 \times 3$

$+ F_{ad} \cos \theta \times 3 = \text{zero}$



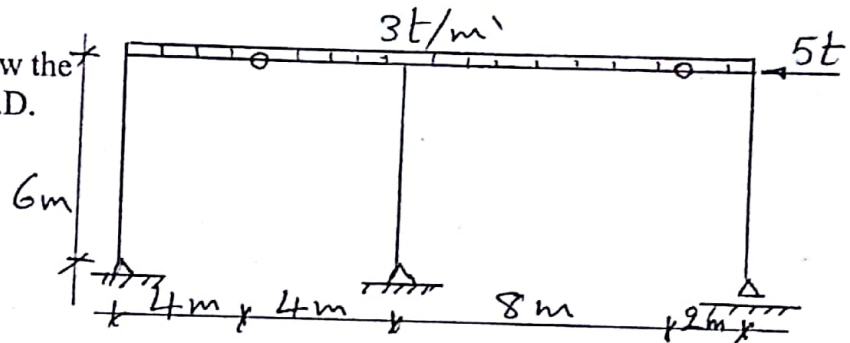
Higher Technological Institute
10th of Ramadan City
 Department of Civil Engineering

Subject: Structures (CT 112)
 Examiner: Dr. Manal K. Zaki
 Exam: Final

Term: Jan-May 2008
 Time: 2 hours

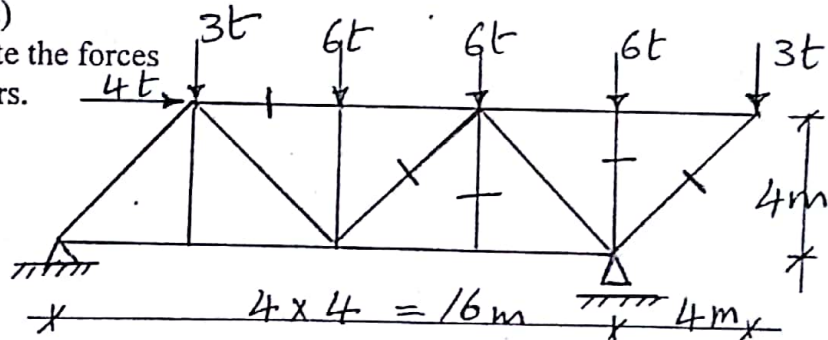
Question 1 (15 marks)

For the shown frame draw the N.F.D., Q.F.D. and B.M.D. under the given loads



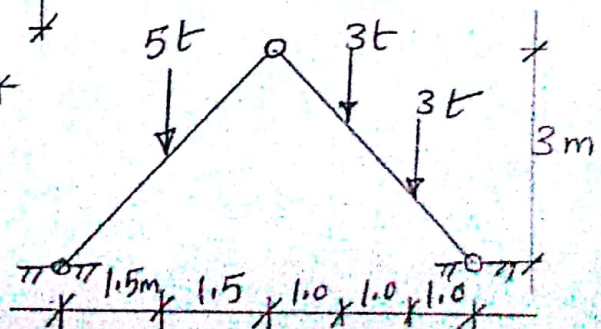
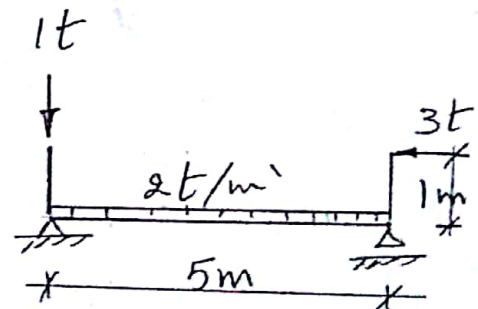
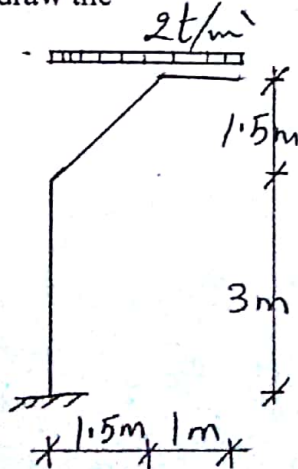
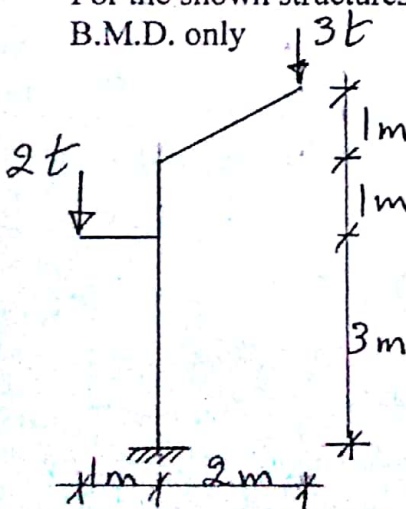
Question 2 (15 marks)

For the shown compute the forces in the marked members. Check graphically

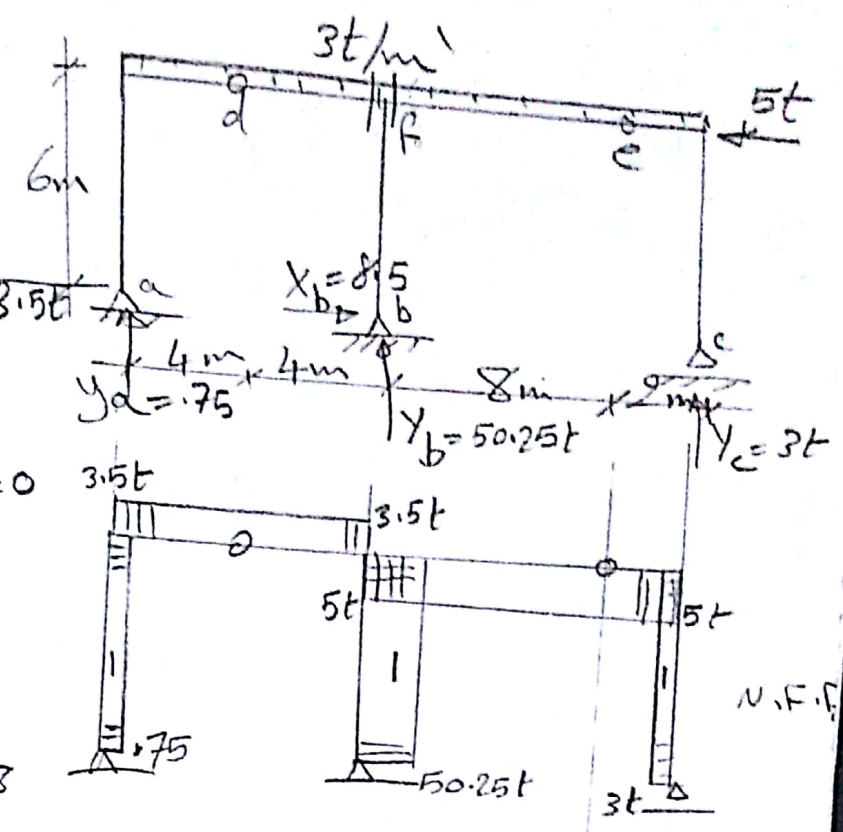


Question 3 (10 marks)

For the shown structures draw the B.M.D. only



41



$$\sum M_{e \text{ right}} = 0$$

$$\begin{aligned} \therefore 3 \times 2 \times 1 - Y_c \times 2 &= 0 \\ \therefore Y_c &= 3t \end{aligned}$$

$$\sum M_a = 0$$

$$\begin{aligned} \therefore 3 \times 18 \times 9 - Y_b \times 8 \\ - Y_c \times 18 - 5 \times 6 &= 0 \end{aligned}$$

$$\therefore Y_b = 50.25t$$

$$\sum M_b = 0$$

$$\begin{aligned} \therefore 3 \times 18 \times 1 + Y_a \times 18 \\ - 5 \times 6 - Y_c \times 10 &= 0 \end{aligned}$$

$$\therefore Y_a = 0.75t$$

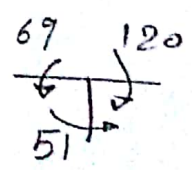
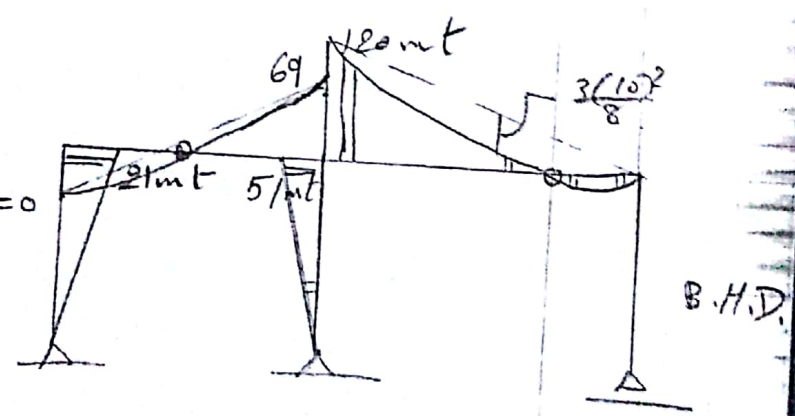
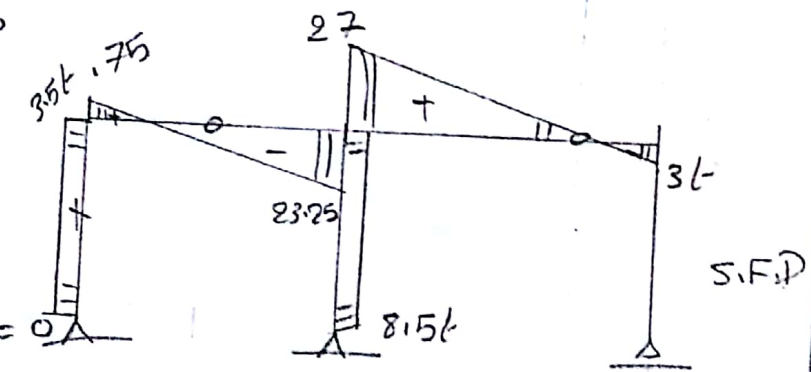
check $\sum Y = 0$

$$\sum M_{d \text{ left}} = 0$$

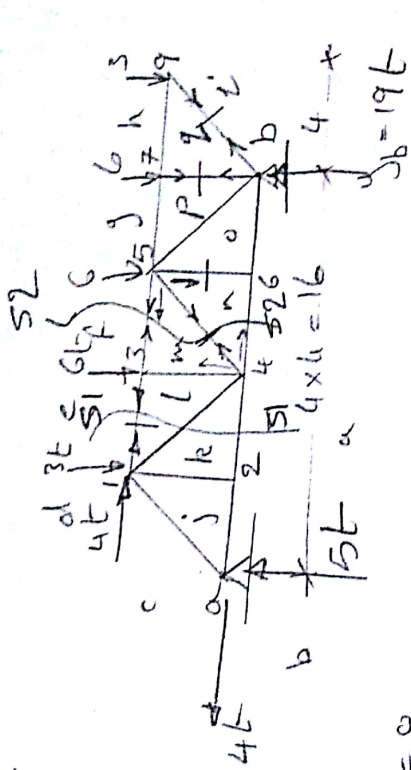
$$3 \times 4 \times 2 - Y_a \times 4 - X_a \times 6 = 0$$

$$\begin{aligned} \therefore X_a &= 3.5t \\ \therefore X_b &= 8.5t \end{aligned}$$

$$\begin{aligned} M_{f \text{ right}} \\ &= 3 \times 10 \times 5 - 3 \times 10 \\ &= 150 - 30 \\ &= 120 \end{aligned}$$



Q2



$$\sum M_a = 0$$

$$\therefore 4 \times 4 + 3 \times 4 + 6(8 + 12 + 16) + 3 \times 20 - Y_b \times 16 = 0$$

$$\therefore Y_b = 19t$$

$$\therefore Y_a = 5t$$

Sec S1-S1

$$\sum M_4 \text{ left} = 0$$

$$\therefore 5 \times 8 + F_{1-3} \times 4 + 4 \times 4 - 3 \times 4 = 0$$

$$\therefore F_{1-3} = -11t \text{ comp.}$$

$$F_{3-5} = -11t \text{ comp.}$$

Sec S2-S2

$$\sum \text{right} = 0$$

$$\therefore F_{5-4} \times 4 + F_{4-5} \cos 45 \times 4 + 19 \times 4 - 6 \times 4 - 3 \times 8 = 0$$

$$\therefore F_{4-5} = 5.66t \text{ Tens}$$

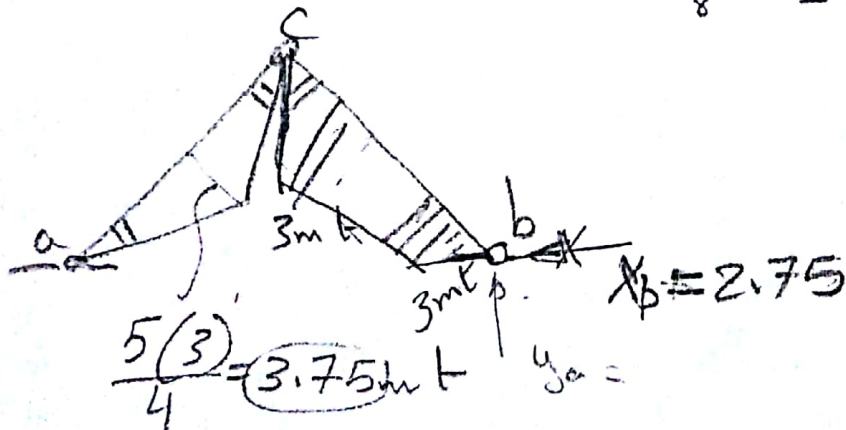
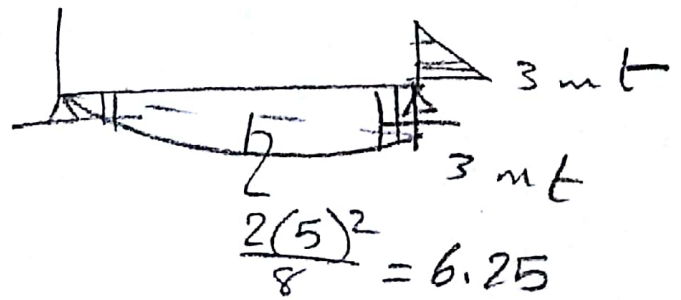
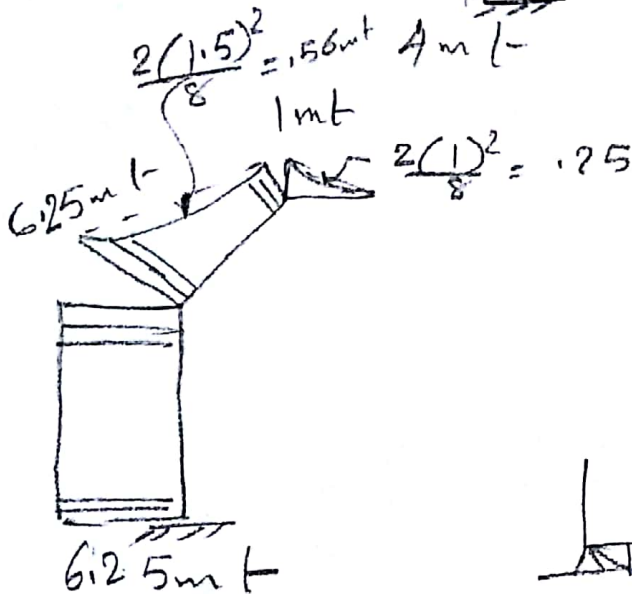
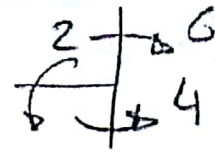
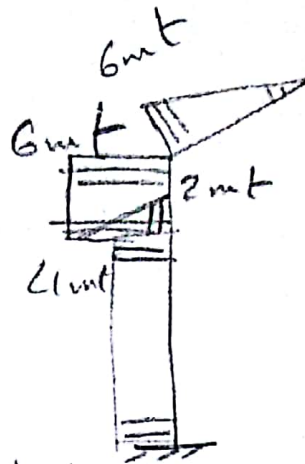
$$\text{Joint: } F_{6-5} = 0$$

$$\text{Joint: } F_{7-4} = -6t \text{ comp.}$$

$$\text{Joint: } 9 \therefore 3 + F_{9-b} \cos 45 = 0$$

$$F_{9-b} = -4.24t \text{ comp}$$

3



$$\sum M_a = 0$$

$$\therefore 5 \times 1.5 + 3 \times 4 + 3 \times 5 - Y_a \times 6 = 0$$

$$\therefore Y_a = 5.75 \text{ t}$$

$$\sum M_{\text{right}} = 0$$

$$3 \times 1 + 3 \times 2 + X_b \times 3 - Y_a \times 3 = 0 \rightarrow X_a = 2.75$$

HIGHER TECHNOLOGICAL INSTITUTE

Civil Engineering Department

Theory of Structures (2)

Time allowed: 1.5 hr.



3rd semester 2016-2017

Mid-term Exam

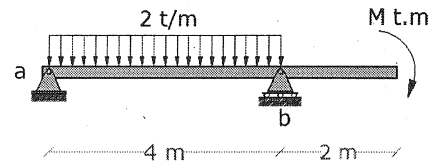
Code : CT112

Examiner: Dr. Ahmed Youssef

*** The exam consists of four questions in four pages attempt all.

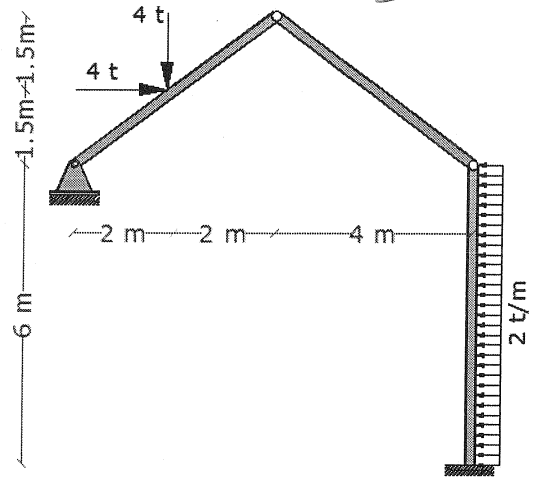
Question (1): (3 Marks) *a2, b2, c2, d1*

For the shown beam find the value of the shown clockwise concentrated moment (M), such that the supports can sustain load up to 2 t (tension) and 6 t (compression).



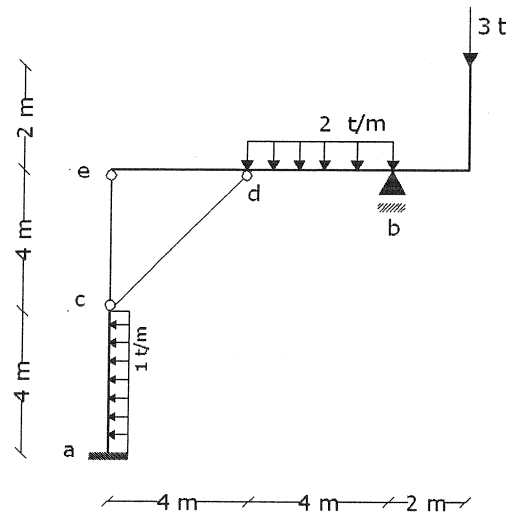
Question (2): (5 Marks) *a, b, c, d*

Find the supports reactions for the shown structure.



Question (3): (6 Marks) *a₂, b₂, c₂, d₁*

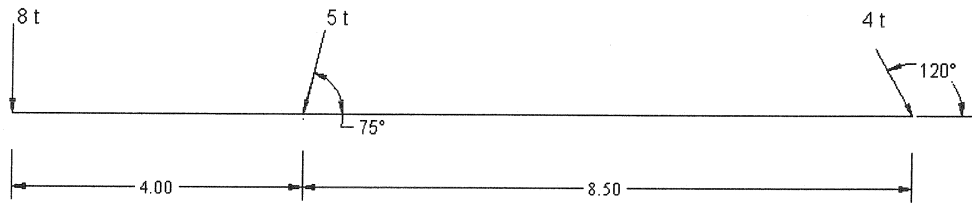
Determine the external reactions and the force in link members for the shown frame.



(Handwritten signature)

Question (4): (6 Marks) *a2, b2, c2, d1*

Determine the magnitude, direction, point of application of the force which make the system in equilibrium for the shown system

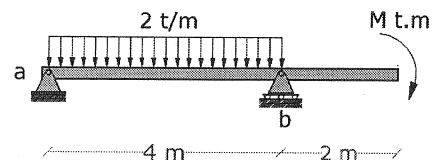




***** The exam consists of four questions in four pages attempt all.**

Question (1): (3 Marks)

For the shown beam find the value of the shown clockwise concentrated moment (M), such that the supports can sustain load up to 2 t (tension) and 6 t (compression).



Only support (a) can expose to tension.

***In first case the vertical reaction (y_a) must not exceed 2t (downward).

- $\sum M_b = 0$

$$2 \cdot 4 \cdot 2 + 2 \cdot 4 - M = 0 \quad M = 24 \text{ t.m} \quad \text{-----}1$$

***In second case the vertical reaction (y_b) must not exceed 6t (upward).

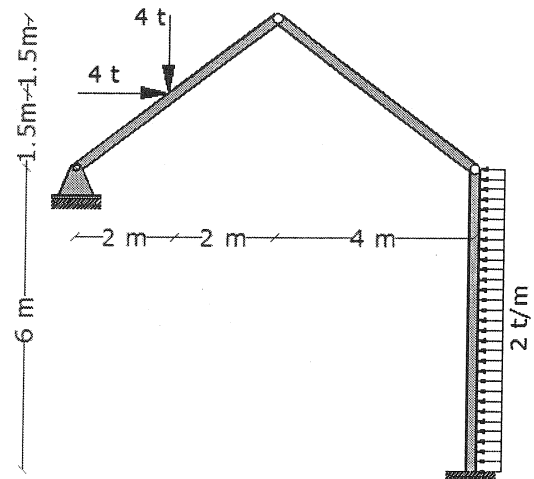
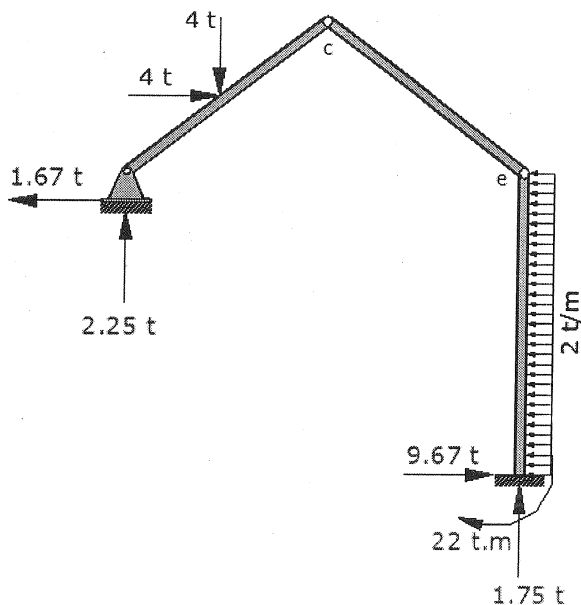
- $\sum M_a = 0$

$$2 \cdot 4 \cdot 2 - 4 \cdot 6 + M = 0 \quad M = 8 \text{ t.m} \quad \text{-----}1$$

We can satisfy the two condition by Moment = 8 t.m -----1

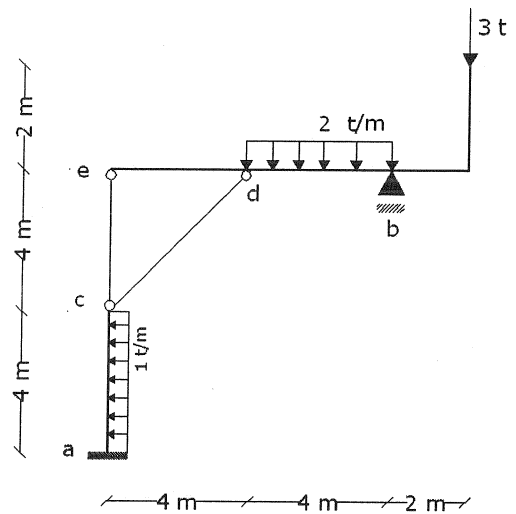
Question (2): (5 Marks)

Find the supports reactions for the shown structure.



Question (3): (6 Marks)

Determine the external reactions and the force in link members for the shown frame.



• $\sum M_c = 0$

$3 \cdot 10 + 2 \cdot 4 \cdot 6 - 8 Y_b = 0 \quad Y_b = 9.75 \text{ t (upward) --1}$

• $\sum Y = 0$

$8 + 3 - Y_a - 9.75 = 0 \quad Y_a = 1.25 \text{ t (upward) -----1}$

• $\sum X = 0$

$X_a = 4 \text{ t (to the right) -----1}$

• $\sum M_a = 0$

$3 \cdot 10 + 2 \cdot 4 \cdot 6 - 8 \cdot 9.75 - 4 \cdot 2 - M_a = 0 \quad M_a = 8 \text{ t.m (clockwise) --1}$

• $\sum M_d = 0$

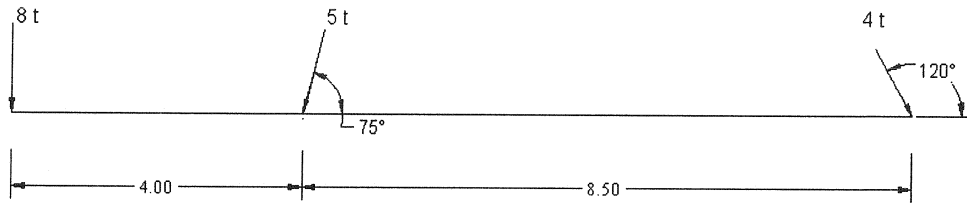
$3 \cdot 6 + 2 \cdot 4 \cdot 2 - 4 F_{ec} = 0 \quad Y_b = 8.5 \text{ t (tension) --1}$

• $\sum Y = 0$

$8 + 3 + 8.5 - F_{ed} \cos 45 = 0 \quad F_{ed} = 27.577 \text{ t (compression) -----1}$

Question (4): (6 Marks)

Determine the magnitude, direction, point of application of the force which make the system in equilibrium for the shown system



Solution:-

-Analytical

$$\sum F_x = R_x$$

$$R_x = -5 \cos (75) + 4 \cos (60) = 0.705 t \text{ (left)}$$

$$\sum F_y = R_y$$

$$R_y = -8 - 5 \sin (7) - 4 \sin (60) = -16.29 t \text{ (upward)}$$

$$R = ((R_x)^2 + (R_y)^2)^{0.5} = 16.30 t$$

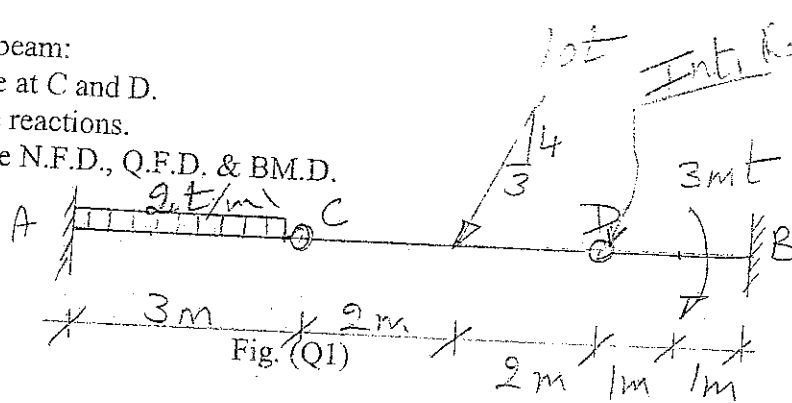
$$\tan \theta = R_y / R_x \Rightarrow \Rightarrow \Rightarrow \Rightarrow \theta = 92.47^\circ$$

$$R * x \sin (87.53) = 5 * 4 \sin (75) + 4 * 12.5 \sin (60) \Rightarrow \Rightarrow X = 3.85 \text{ m}$$

Q1

For the shown beam:

1. Separate at C and D.
2. Find the reactions.
3. Draw the N.F.D., Q.F.D. & B.M.D.

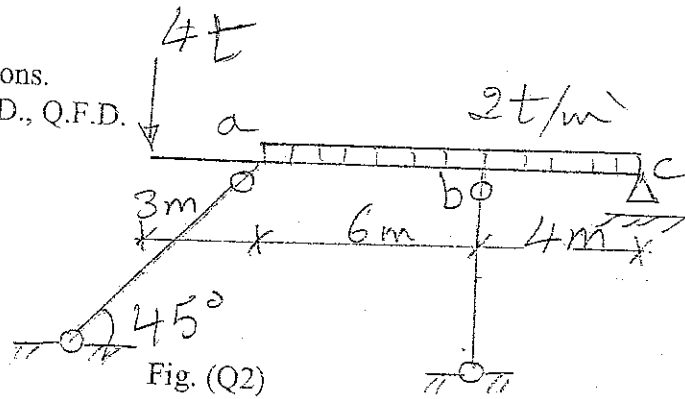


[a2] [2 marks]
[a2] [2 marks]
[a2] [4 marks]

Q2

For the shown beam :

1. Find the reactions.
2. Draw the N.F.D., Q.F.D.
3. Draw B.M.D.

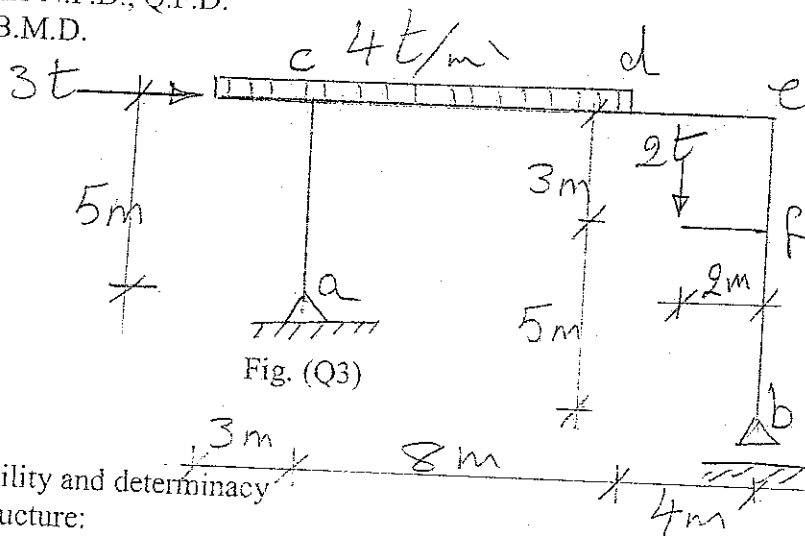


[a1] [3 marks]
[a2] [3 marks]
[a2] [4 marks]

Q3

For the shown Frame:

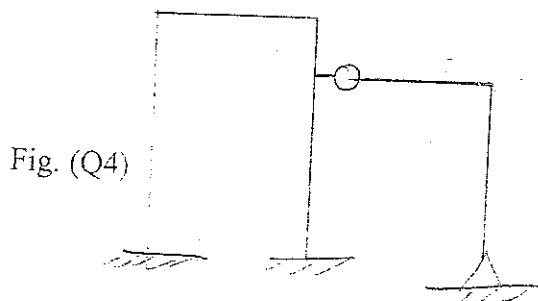
4. Find the reactions.
5. Draw the N.F.D., Q.F.D.
6. Draw B.M.D.



[a1] [2 marks]
[a2] [4 marks]
[a2] [4 marks]

Q4

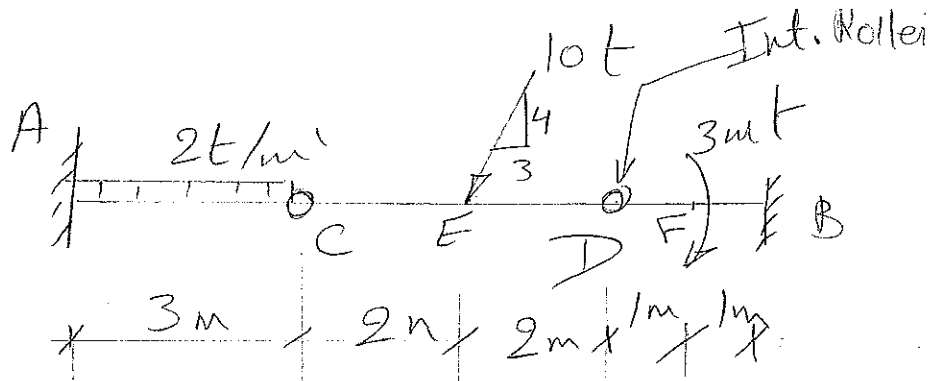
Discuss the stability and determinacy of the shown structure:



[di] [2 marks]

[Total 2]
[Total 30]

Q1



Part AC

$$Y_A = 4 + 2 \times 3 = 10t$$

$$M_A = 21mt$$

$$X_A = 6t$$

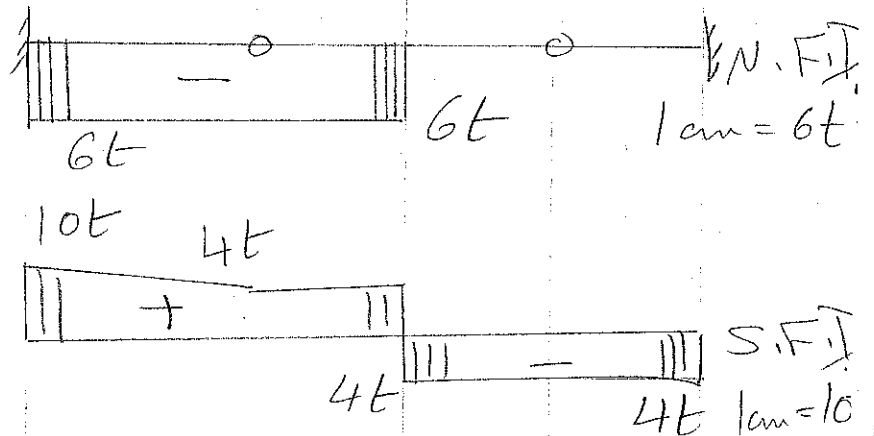
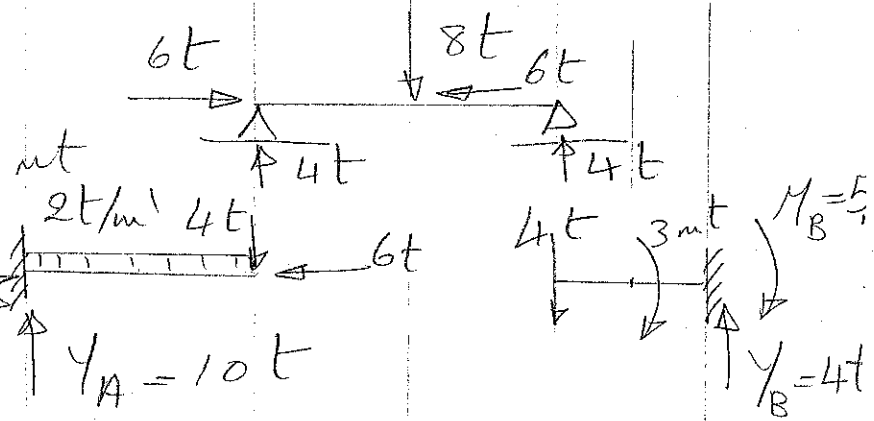
$$M_A = 4 \times 3 + 2 \times 3 \times 1.5 = 21mt$$

Part DB

$$\sum M @ B = 0$$

$$4 \times 2 - 3 - M_B = 0$$

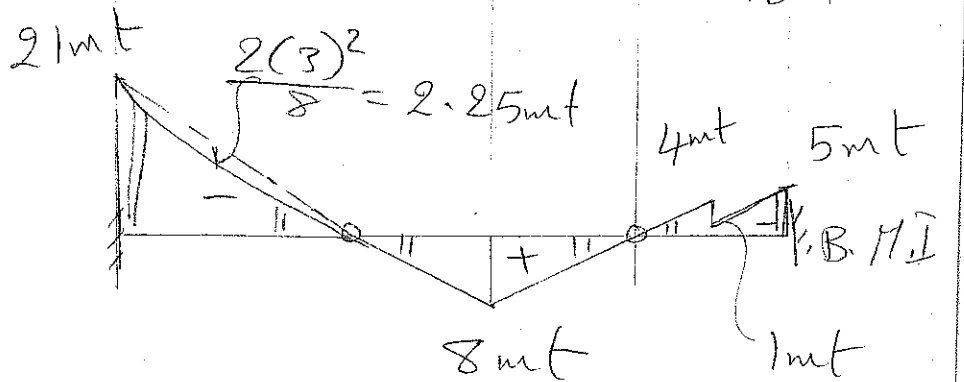
$$\therefore M_B = 5mt$$



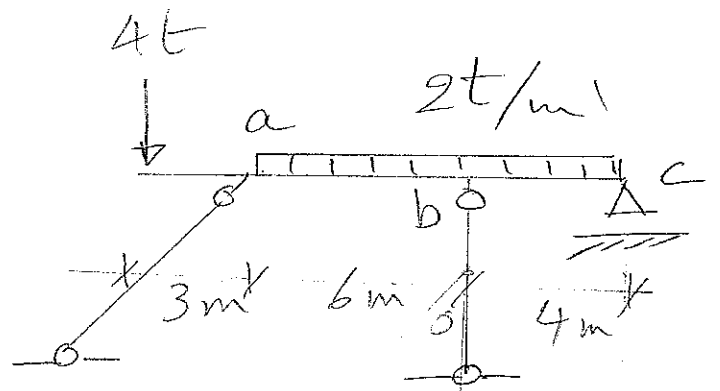
$$M_E = 4 \times 2 = 8mt$$

$$M_E \text{ left} = -4 \times 1 = -4mt$$

$$M_E \text{ right} = -4 + 3 = -1mt$$



Q2



$$\sum M @ a = 0$$

$$4 \times 9 + 2 \times 10 \times 1 + 4R_c = 0$$

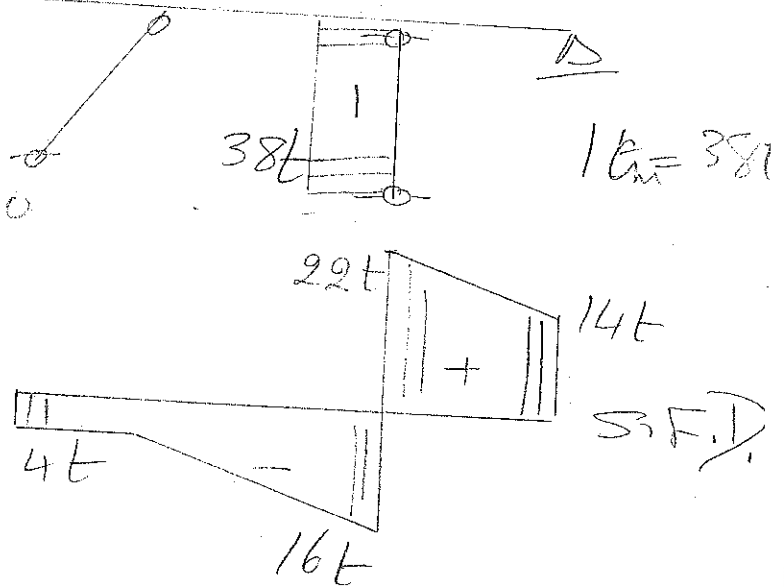
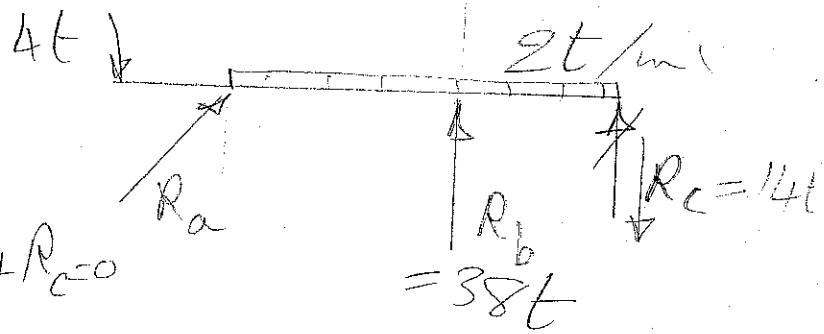
$$\therefore R_c = -14t$$

$$\sum F_x = 0 \rightarrow R_a = 0$$

$$\sum F_y = 0$$

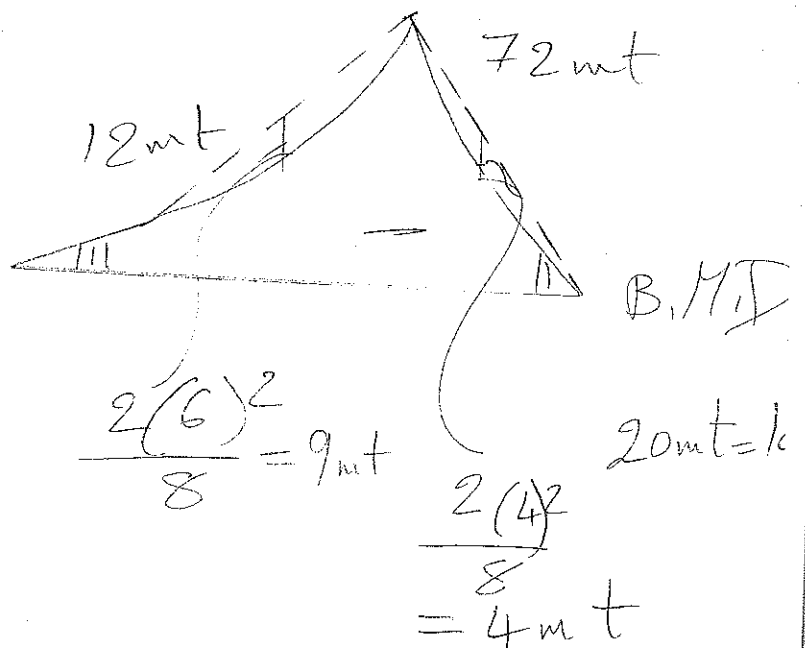
$$\therefore 4 + 2 \times 10 + 14 - R_b = 0$$

$$\therefore R_b = 38t$$



$$M_a = -4 \times 3 = -12mt$$

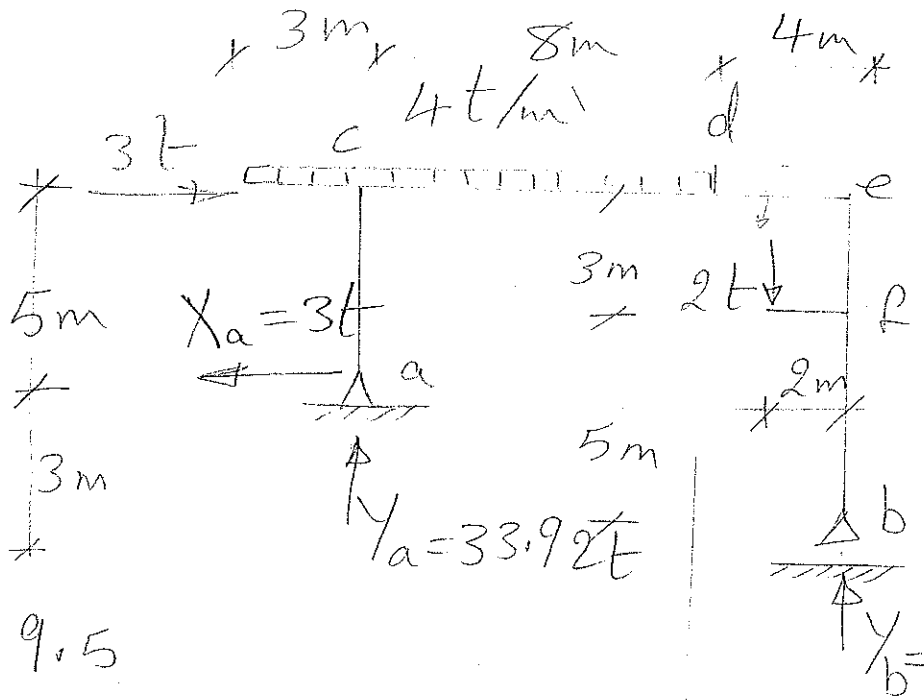
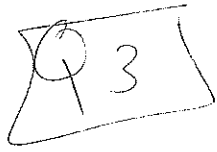
$$M_b = -14 \times 4 = 2 \times 4 \times 2 = -72mt$$



$$\frac{2(6)^2}{8} = 9mt$$

$$\frac{2(4)^2}{8} = 4mt$$

$$20mt = k$$



$$\textcircled{1} \sum M @ b = 0$$

$$2 \times 2 + 4 \times 11 \times 9.5$$

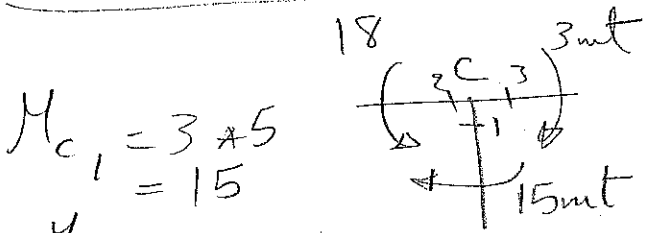
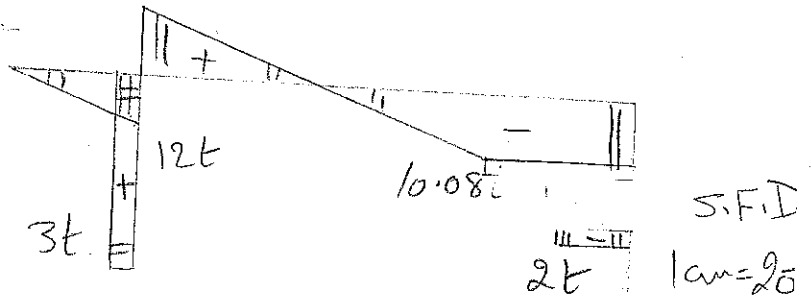
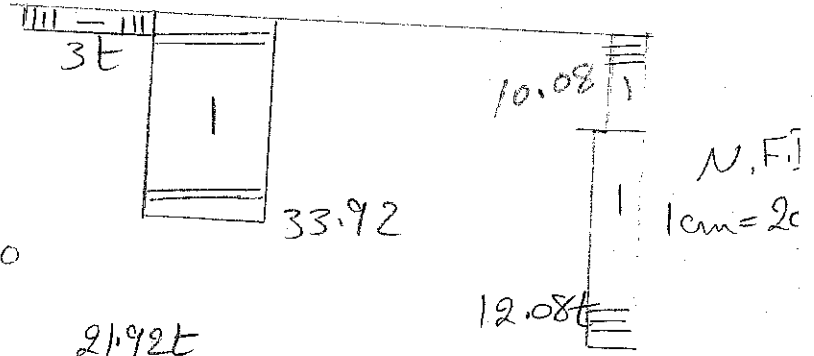
$$+ 3 \times 3 - 3 \times 8 - 12 \frac{Y_a}{a} = 0$$

$$\therefore Y_a = 33.92t$$

$$\textcircled{2} \sum F_y = 0$$

$$\therefore 4 \times 11 + 2 - 33.92 - Y_b = 0$$

$$\therefore Y_b = 12.08t$$

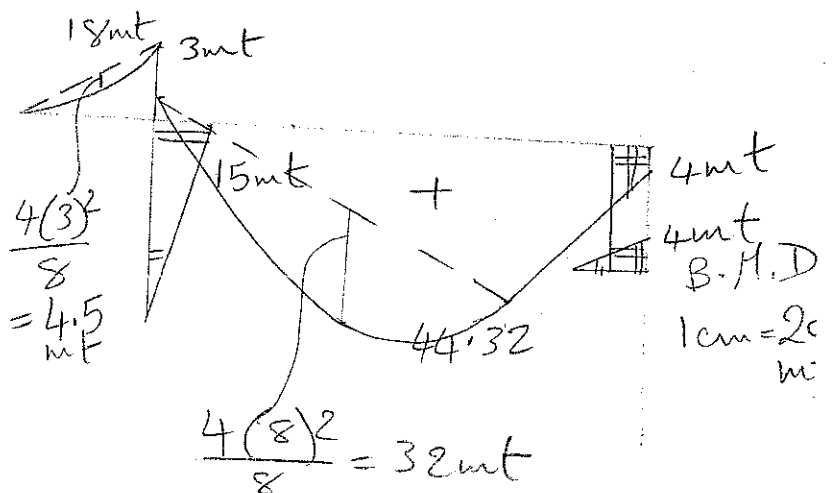


$$M_{c1} = 3 \times 5 = 15$$

$$M_{c2} = 4 \times 3 \times 1.5 = 18mt$$

$$M_e = 2 \times 2 = 4mt$$

$$M_d = 12.08 + 4 - 2 \times 2 = 44.32mt$$

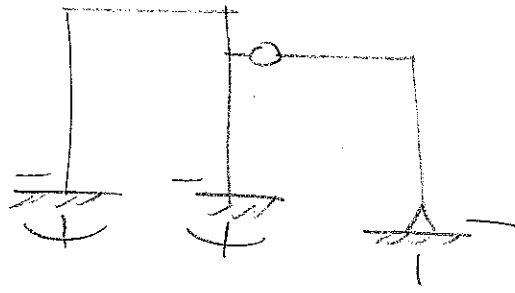


Q4

$$u = 8$$

$$E = 3 + 1 = 4$$

= stable & 4 times st. Indel.



Q1

For the shown beam:

1. Separate at D.
2. Find the reactions.
3. Draw the N.F.D., Q.F.D. & B.M.D.

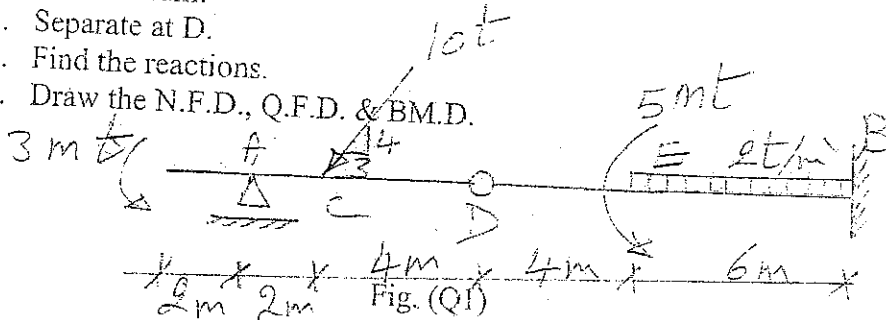


Fig. (Q1)

ILO's

[a2]

[2 marks]

[a2]

[2 marks]

[a2]

[4 marks]

[Total 8]

Q2

For the shown beam :

1. Find the reactions.
2. Draw the N.F.D., Q.F.D.
3. Draw B.M.D.

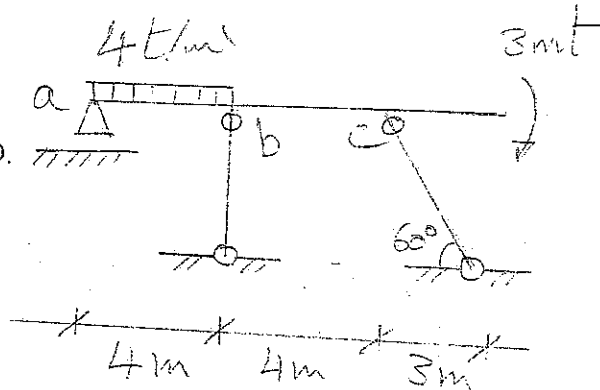


Fig. (Q2)

[a1]

[3 marks]

[a2]

[3 marks]

[a2]

[4 marks]

[Total 10]

Q3

For the shown Frame:

4. Find the reactions.
5. Draw the N.F.D., Q.F.D.
6. Draw B.M.D.

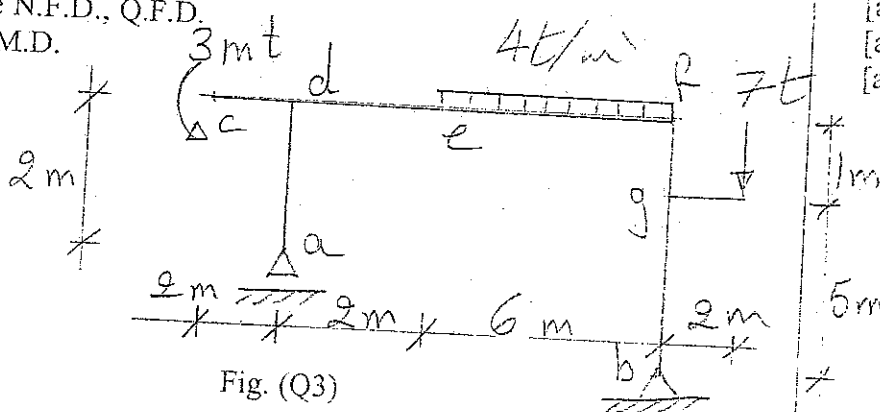


Fig. (Q3)

[a1]

[2 marks]

[a2]

[4 marks]

[a2]

[4 marks]

[Total 10]

Q4

Discuss the stability and determinacy of the shown structure:

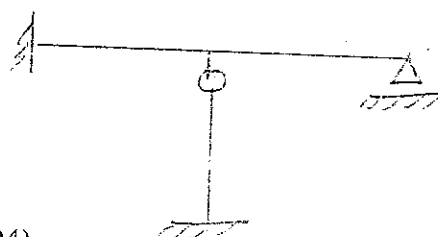


Fig. (Q4)

[d1]

[2 marks]

[Total 2]

[Total 30]

Q11

Upper Part

① $\sum M @ D = 0$
 $\Rightarrow 8 \times 4 + 3 - 6 \times a = 0$
 $\Rightarrow Y_a = 5.83t$

② $\sum F_y = 0$
 $\Rightarrow 5.83 - 8 + Y_D = 0$
 $\Rightarrow Y_D = 2.17t$

Lower Part

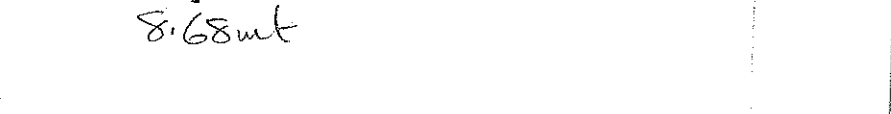
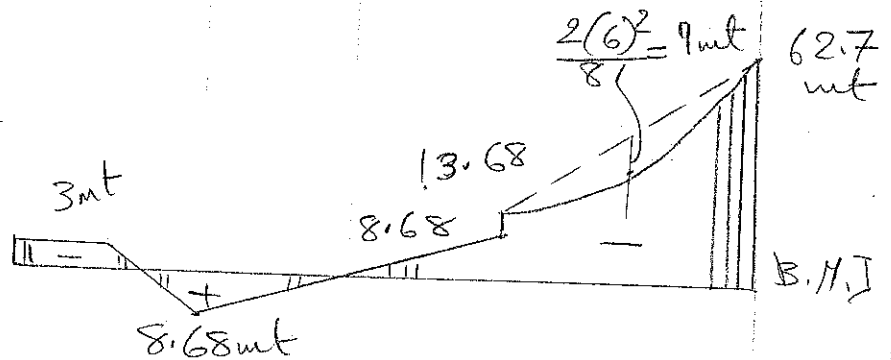
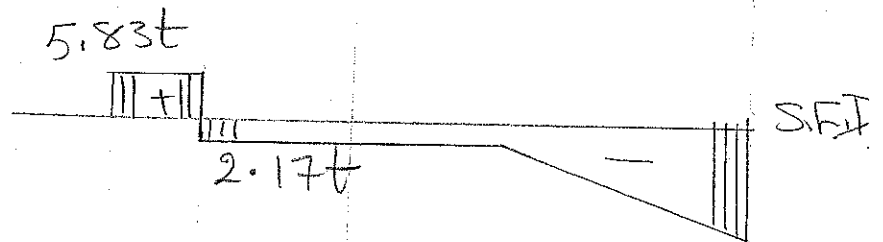
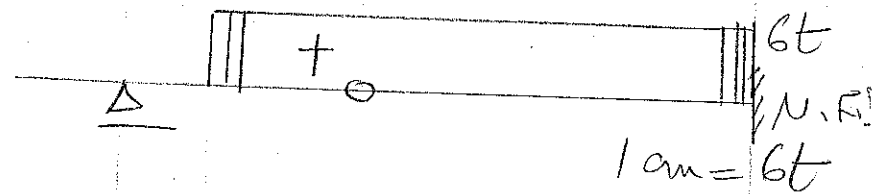
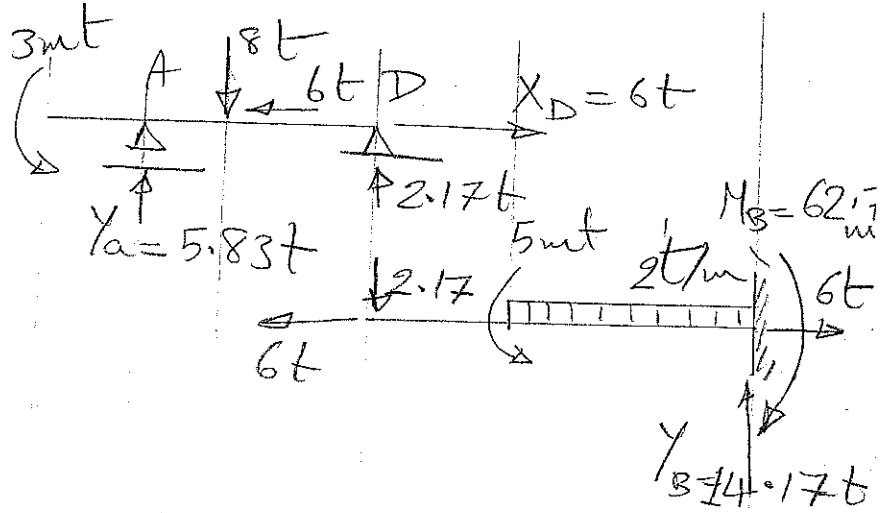
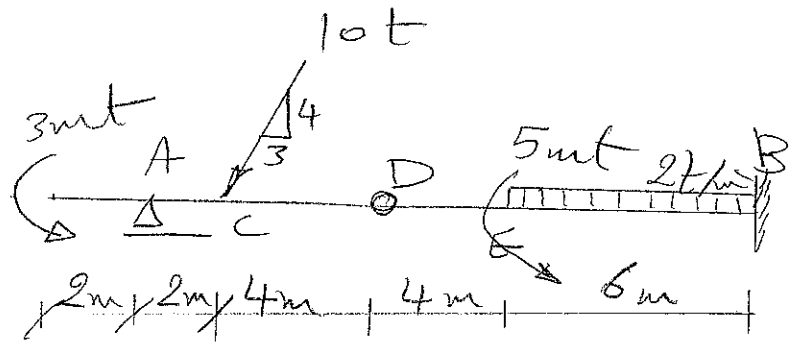
① $\sum F_y = 0$
 $\Rightarrow 2.17 + 2 \times 6 - Y_B = 0$
 $\Rightarrow Y_B = 14.17t$

② $\sum M @ B = 0$
 $\Rightarrow 2.17 \times 10 + 5 + 2 \times 6 \times 3 - M_B = 0$
 $\Rightarrow M_B = 62.7 \text{ mt}$

$M_{\text{right}} = 2.17 \times 4 = 8.68 \text{ mt}$

$M_{\text{left}} = -2.17 \times 4 = -8.68$

$M_{\text{R}} = -8.68 - 5 = -13.68 \text{ mt}$



Q2

$$\textcircled{1} \sum M @ o = 0$$

$$4 \times 4 \times 2 - 3 - 4 Y_a = 0$$

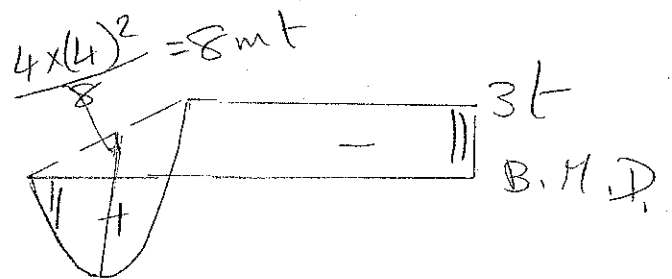
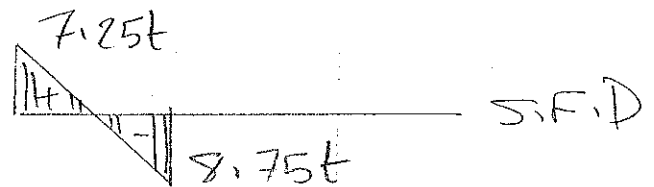
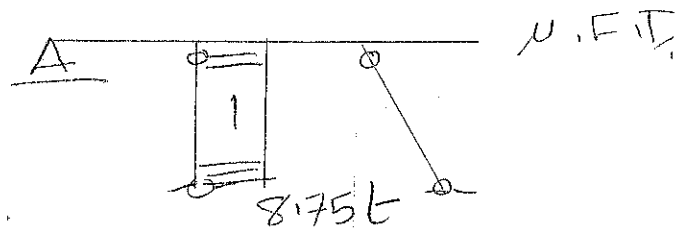
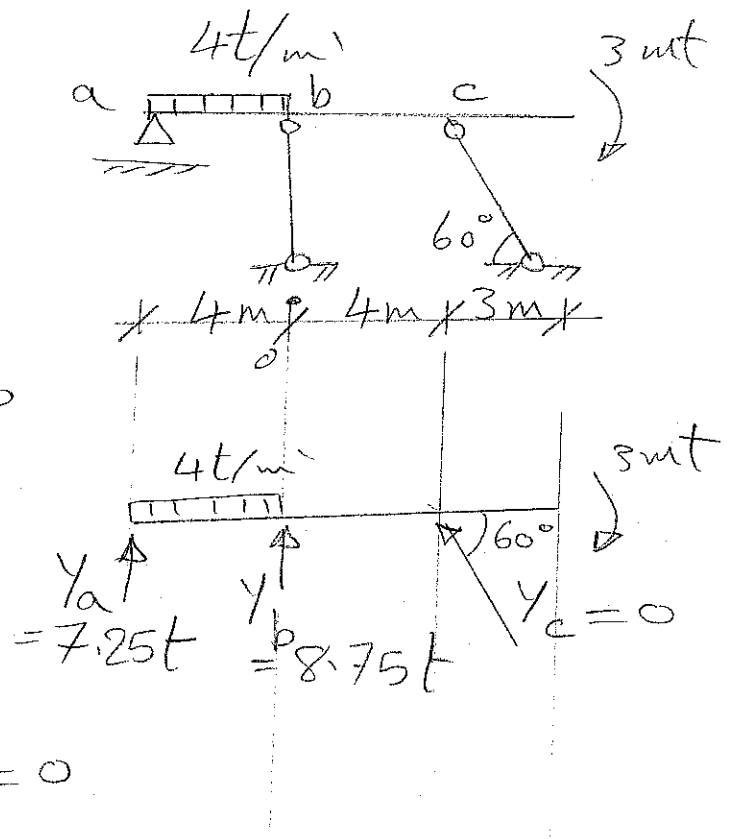
$$\therefore Y_a = 7.25t$$

$$\textcircled{2} \sum F_x = 0 \therefore Y_c = 0$$

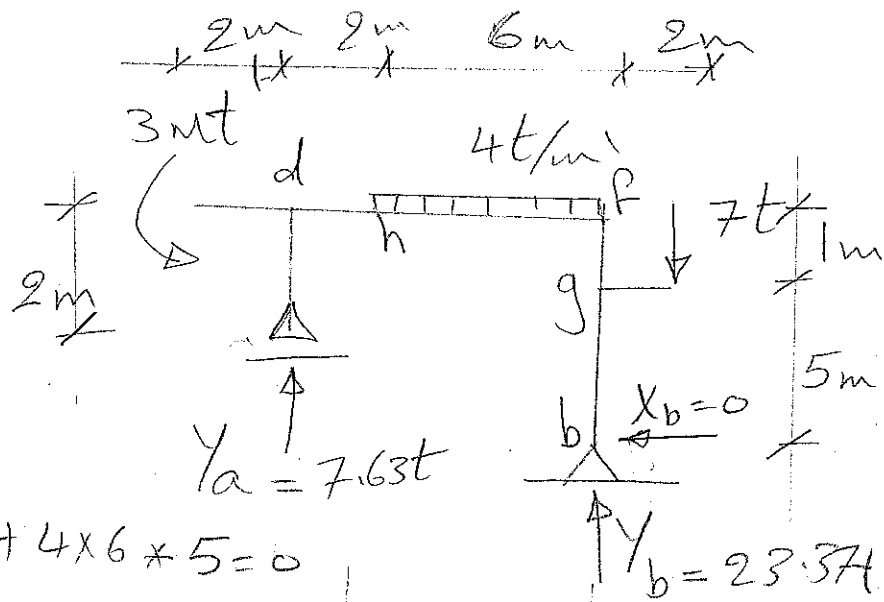
$$\textcircled{3} \sum F_y = 0$$

$$\therefore 4 \times 4 - 7.25 - Y_b = 0$$

$$\therefore Y_b = 8.75t$$



Q3



$$\textcircled{1} \sum M @ a = 0$$

$$-3 - 8Y_b + 7 \times 10 + 4 \times 6 \times 5 = 0$$

$$\therefore Y_b = +23.37t$$

$$\textcircled{2} \sum F_y = 0$$

$$\therefore 23.37 + Y_b - 7 - 4 \times 6 = 0$$

$$\therefore Y_b = 7.63t$$

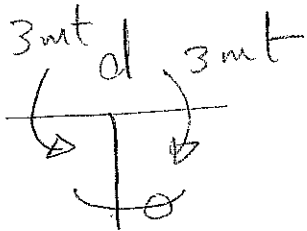
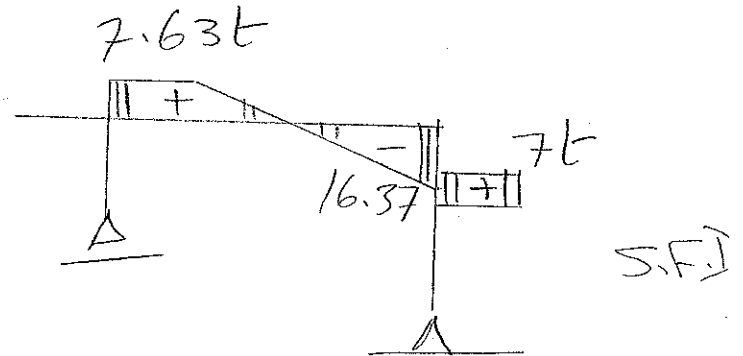
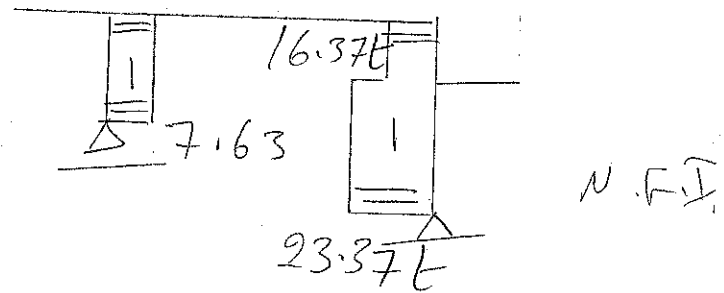
check:

$$\sum M @ b = 0$$

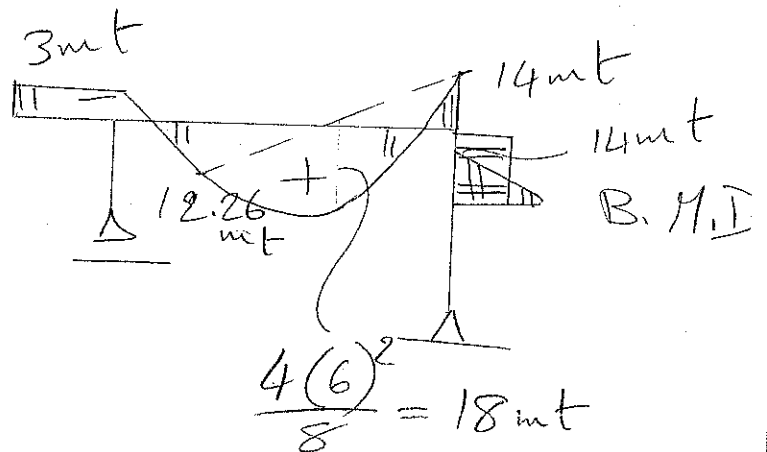
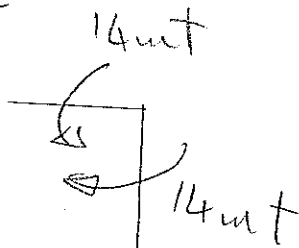
$$7 \times 2 - 4 \times 6 \times 3 - 3$$

$$+ 8Y_a = 0$$

$$\therefore Y_a = 7.63t$$



$$14mt = 7 \times 2$$



$$M_h = -3 + 7.63 \times 2 = 12.96mt$$

Dr. Manal Kamal Zaki

Theory of Structures (2)-CT 112

Time: 1 1/2 hrs.

Q1

For the shown beam:

1. Separate at D.
2. Find the reactions.
3. Draw the N.F.D., Q.F.D. & B.M.D.

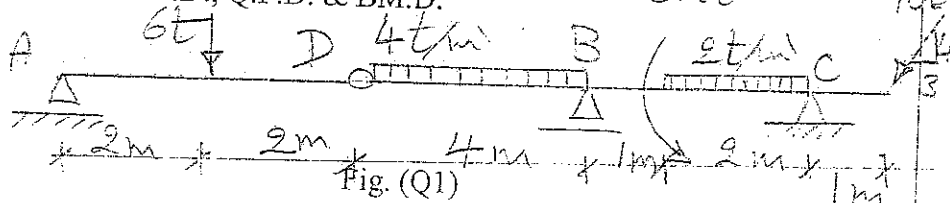


Fig. (Q1)

Separate → 2
 $\gamma_A = 1, \gamma_B = 1$
 N.F. → 1, B.M. → 2
 S.F. → 1
 3mt, 10t, 10t

ILO's
 [a2] [2 marks]
 [a2] [2 marks]
 [a2] [4 marks]

Q2

For the shown beam:

1. Find the reactions.
2. Draw the N.F.D., Q.F.D.
3. Draw B.M.D.

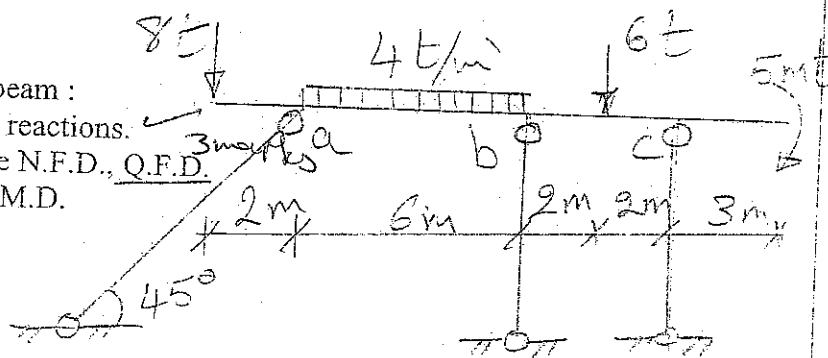


Fig. (Q2)

[a1] [3 marks]
 [a2] [3 marks]
 [a2] [4 marks]

[Total 8]

[Total 10]

Q3

For the shown Frame:

4. Find the reactions.
5. Draw the N.F.D., Q.F.D.
6. Draw B.M.D.

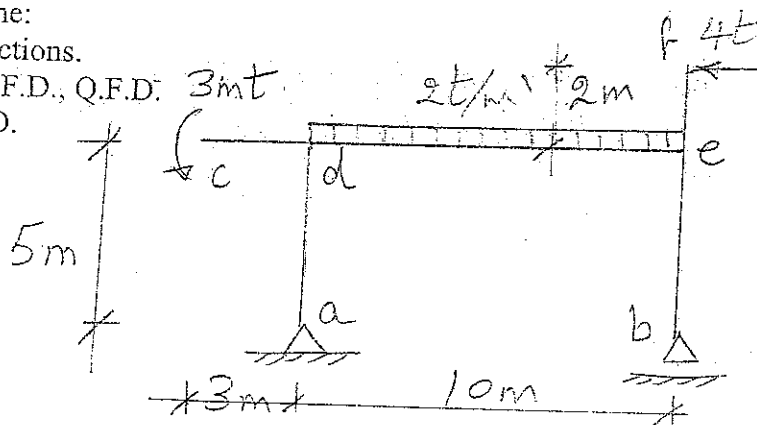


Fig. (Q3)

[a1] [2 marks]
 [a2] [4 marks]
 [a2] [4 marks]

[Total 10]

Q4

Discuss the stability and determinacy of the shown structure:

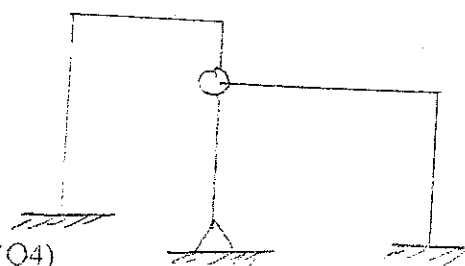


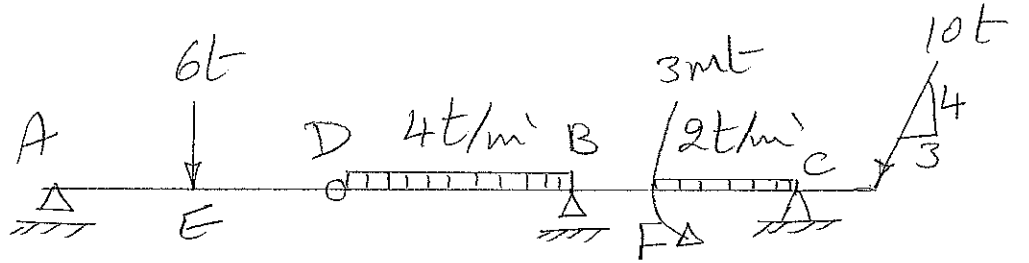
Fig. (Q4)

[d1] [2 marks]

[Total 2]

[Total 30]

Q1



lower part

① $\sum M @ C = 0$

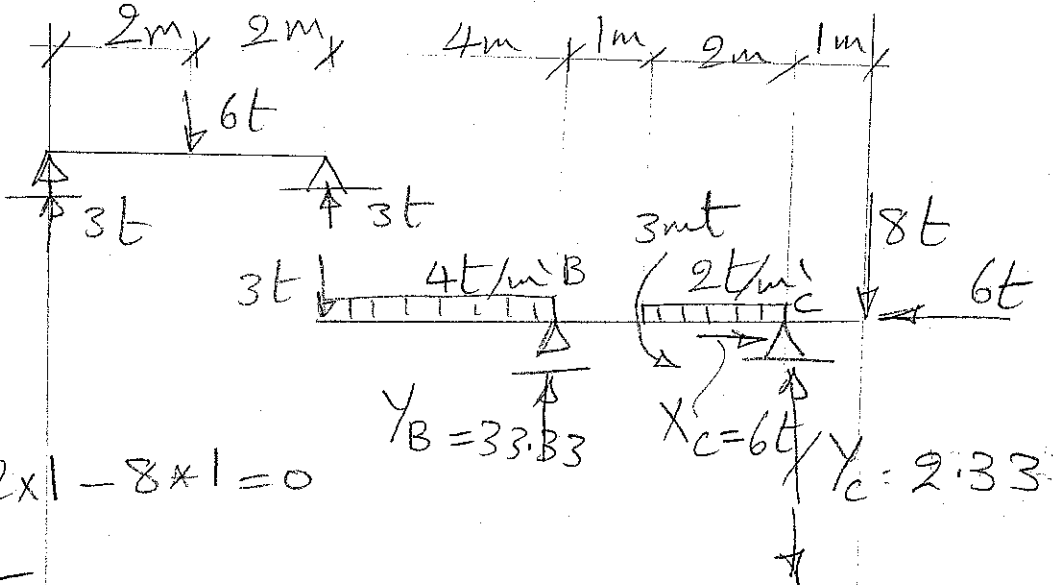
$$3 \times 7 + 4 \times 4 \times 5 - 3 Y_B + 3 + 2 \times 2 \times 1 - 8 \times 1 = 0$$

$$\therefore Y_B = 33.33t$$

② $\sum F_y = 0$

$$3 + 4 \times 4 + 2 \times 2 + 8 - Y_C - 33.33 = 0$$

$$\therefore Y_C = -2.33t$$



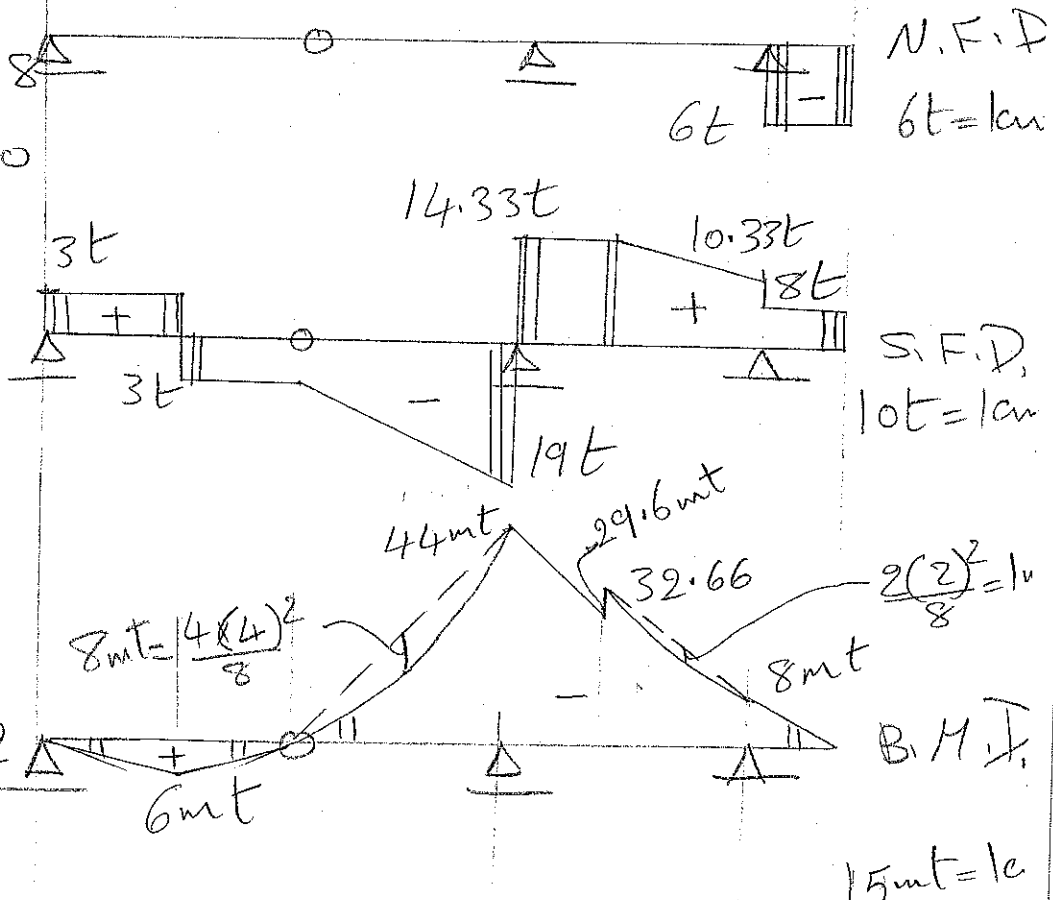
$M_E = 3 \times 2 = 6mt$

$M_B = 3 \times 4 - 4 \times 4 \times 2 = -44mt$

$M_C = -8mt$

$M_{E \text{ right}} = -8 \times 3 - 2.33 \times 2 - 2 \times 2 \times 1 = -32.66$

$M_{C \text{ left}} = -32.66 + 3 = -29.66mt$



N.F.D
6t = 1cm

S.F.D.
10t = 1cm

B.M.D.
15mt = 1cm

Q2

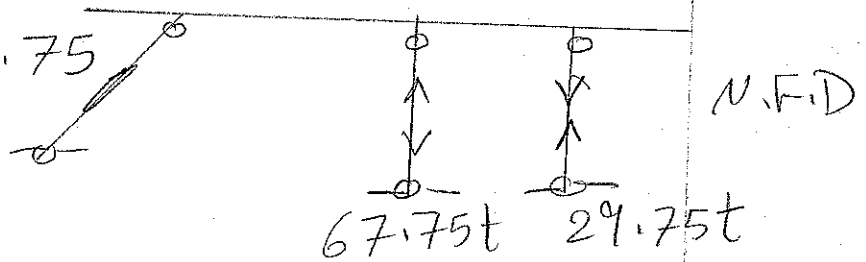
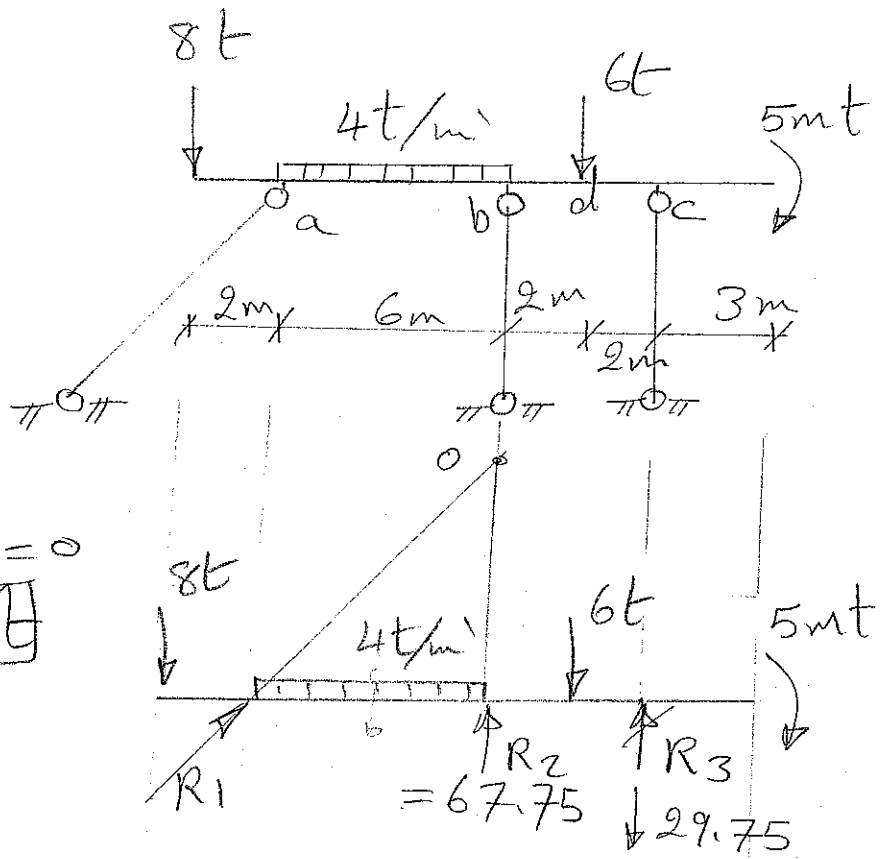
① $\sum M @ o = 0$

$$8 \times 8 + 4 \times 6 \times 3 + 4R_3 - 6 \times 2 - 5 = 0$$

$$\Rightarrow R_3 = -29.75 \text{ t}$$

② $\sum F_x = 0$
 $\Rightarrow R_1 = 0$

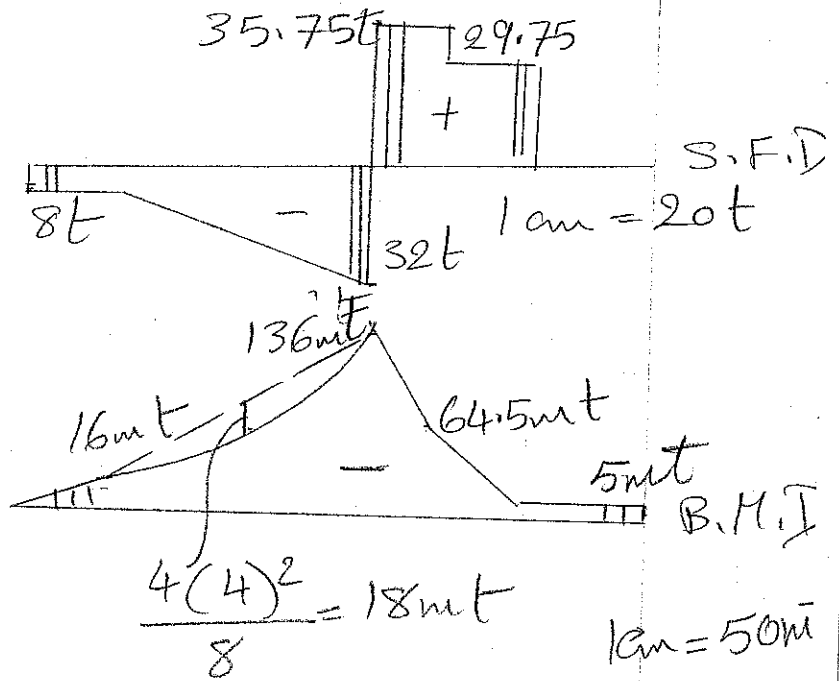
③ $\sum F_y = 0$
 $\Rightarrow 8 + 4 \times 6 + 6 + 29.75 - R_2 = 0$
 $\Rightarrow R_2 = 67.75 \text{ t}$



$$M_a = -8 \times 2 = -16 \text{ mt}$$

$$M_b = -8 \times 8 - 4 \times 6 \times 3 = -136 \text{ mt}$$

$$M_d = -5 - 29.75 \times 2 = -64.5$$



Q3

① $\sum M @ b = 0$

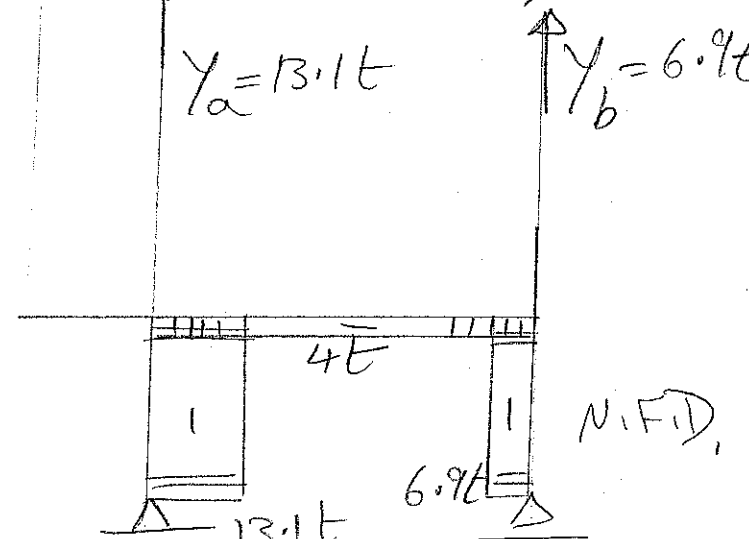
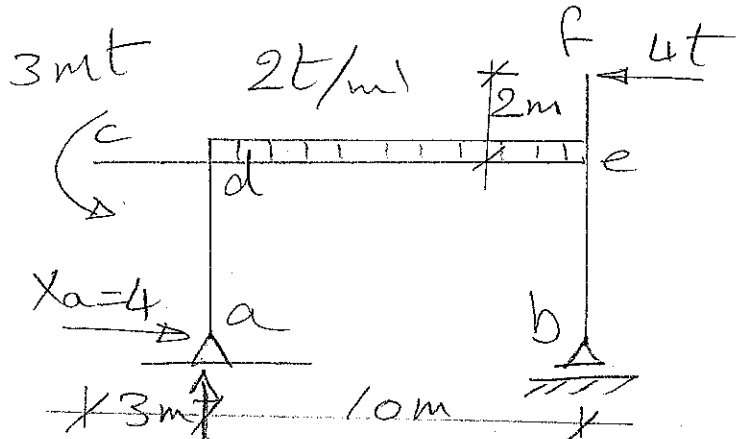
$4 \times 7 + 2 \times 10 \times 5 + 3 - 10 Y_a = 0$

$\therefore Y_a = 13.1 t$

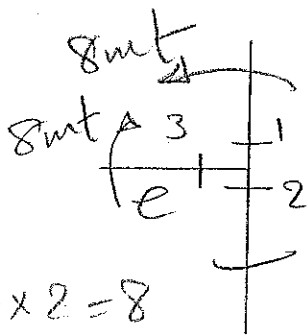
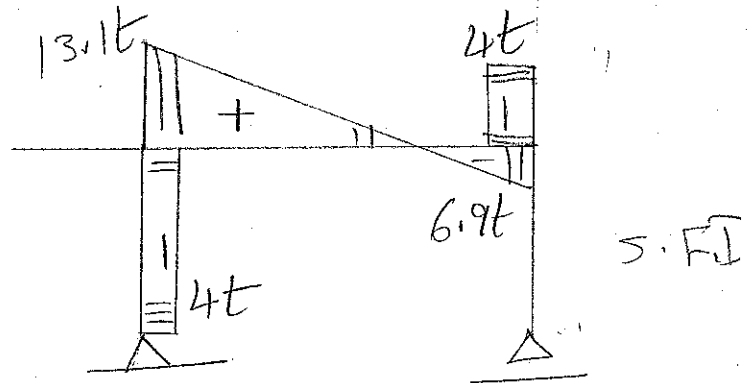
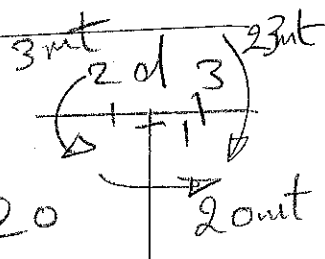
② $\sum F_y = 0$

$\therefore 2 \times 10 - Y_a - Y_b = 0$

$Y_b = 6.9 t$

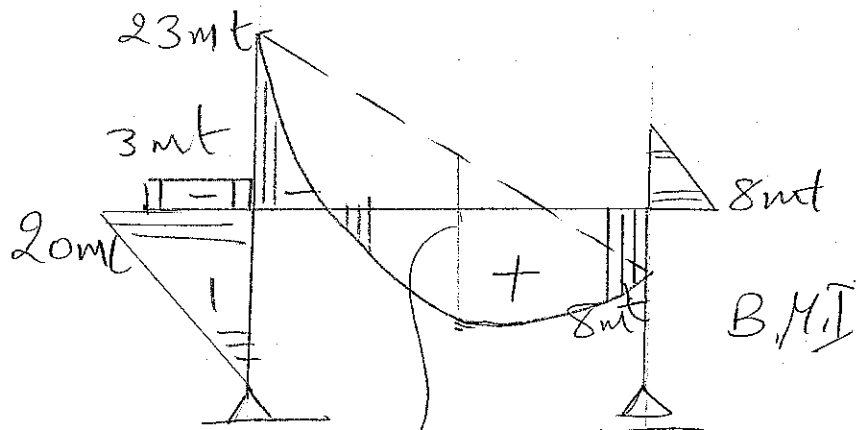


$M_{d1} = 4 \times 5 = 20$
 $M_{d2} = 3 mt$



$M_{e1} = 4 \times 2 = 8$

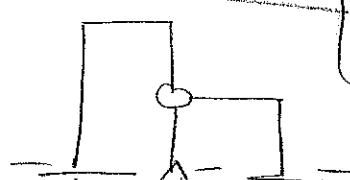
$M_{e2} = 0$



$\frac{2(10)^2}{8} = 25 mt$

stable \rightarrow
 3 times on St. Ind.

Q4 $u = 8$
 $E = 3 + 2 = 5$



Q1

For the shown frame:

1. Find the reactions.
2. Draw the N.F.D., Q.F.D.
3. Draw the B.M.D.

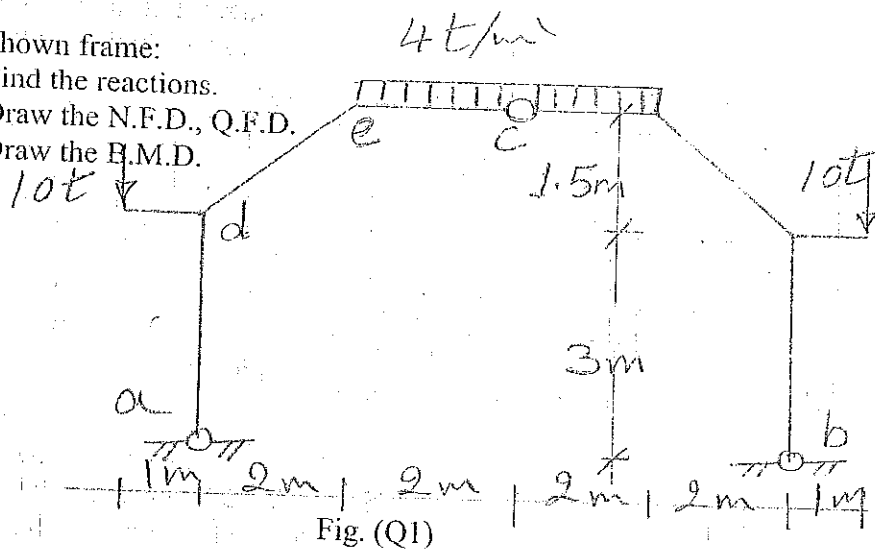


Fig. (Q1)

ILO's

[a2,d1]

[3 marks]

[a2]

[8 marks]

[a2,c1]

[5 marks]

Q2

For the shown truss:

1. Find the reactions.
2. Find the normal forces in the marked members.

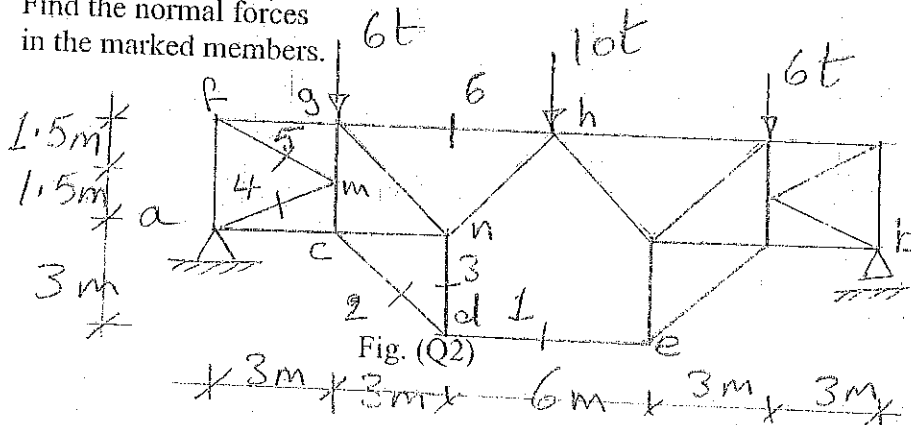


Fig. (Q2)

[a2]

[2 marks]

[a2,c1]

[10 marks]

Q3

For the shown structures:

1. Find the forces in the link members.
2. And draw the B.M.D. only.

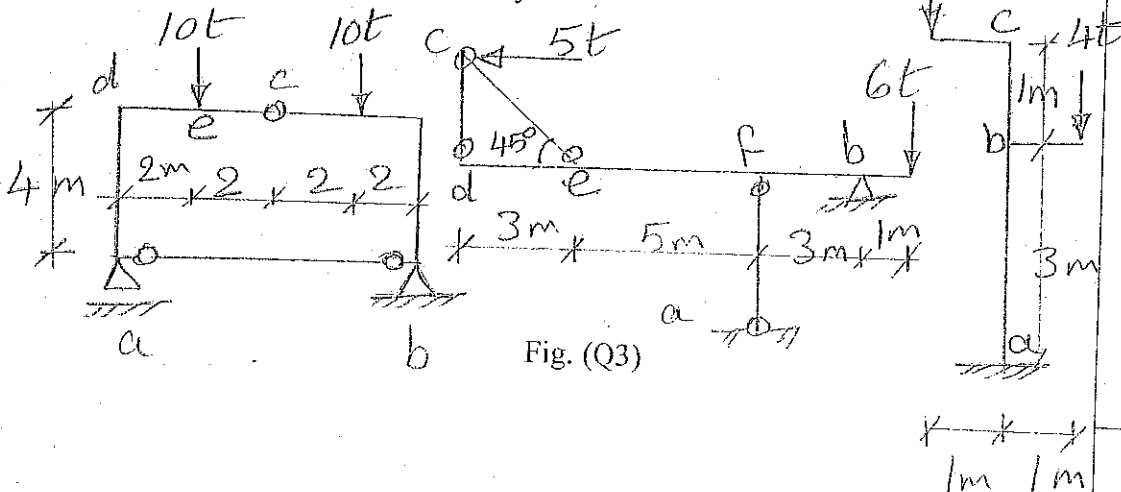


Fig. (Q3)

a2,c1,d1

[12 marks]

[Total 12]

Q1

$$\tan \theta = \frac{1.5}{2} = \frac{3}{4}$$

$$\therefore \sin \theta = 0.6$$

$$\cos \theta = 0.8$$

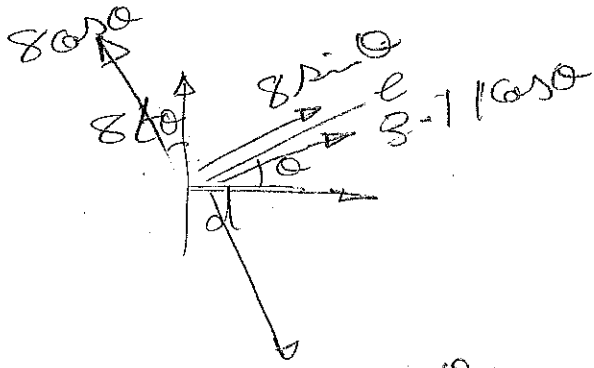
$$Y_a = Y_b = 10 + 4 \times 2 = 18t$$

$$\sum M @ c = 0$$

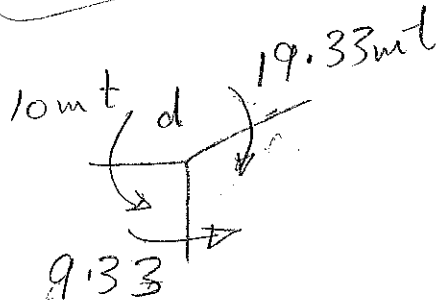
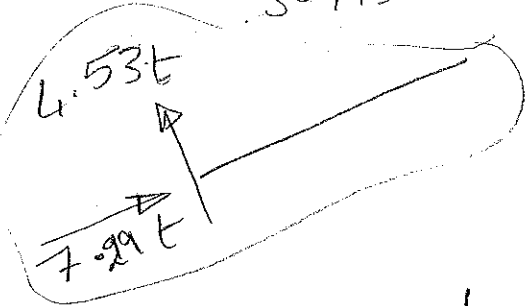
right

$$4 \times 2 \times 1 + 10 \times 5 + 4.5 X_b - 4 Y_b = 0$$

$$\therefore X_b = 3.11t$$

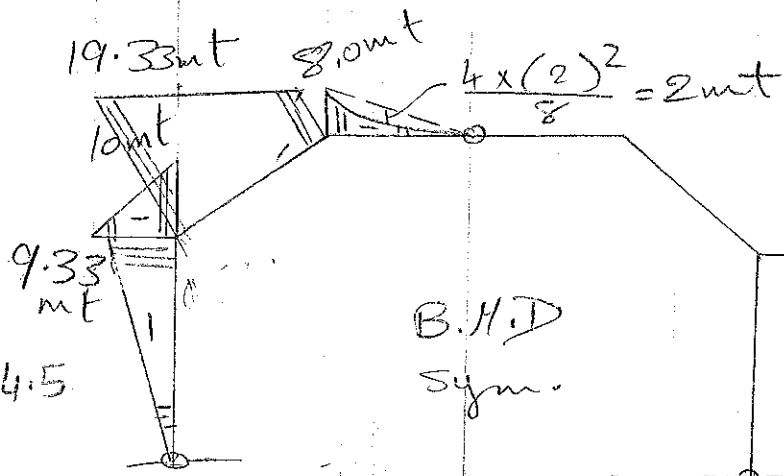
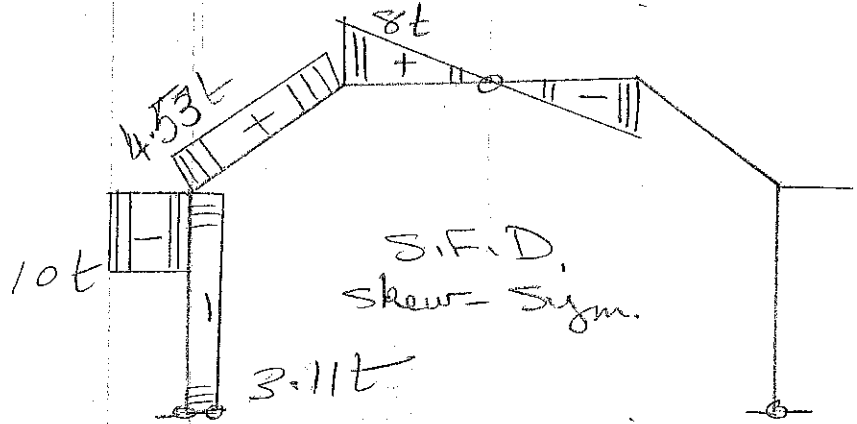
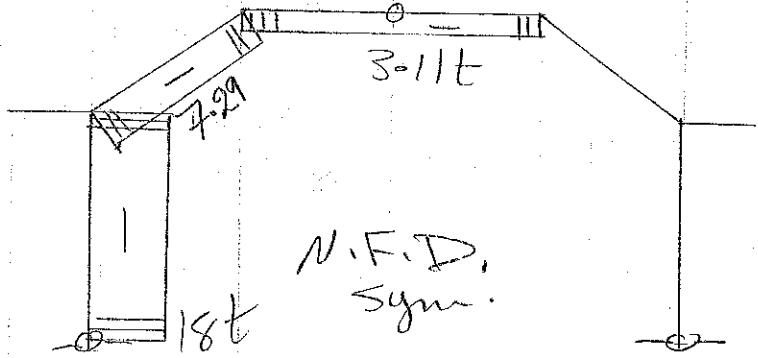
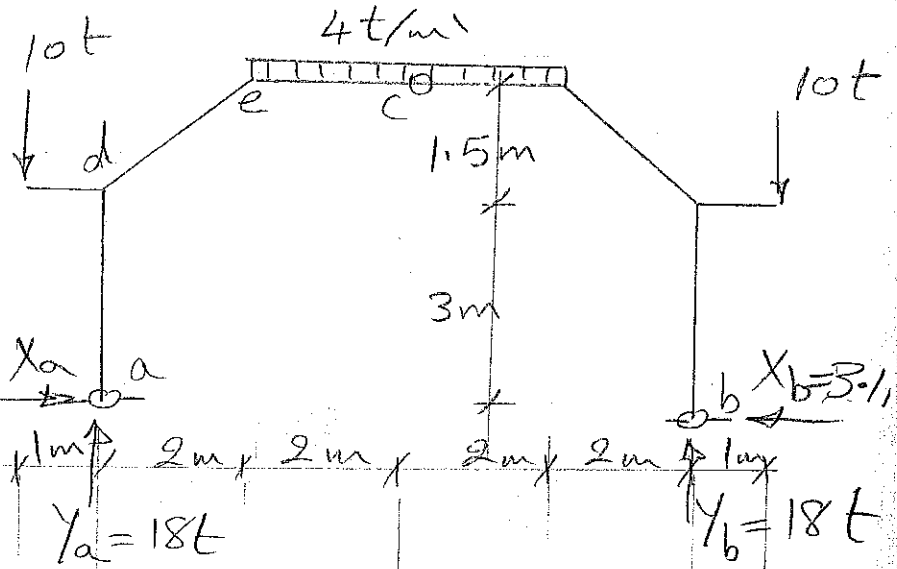


$$3.11 \sin \theta$$



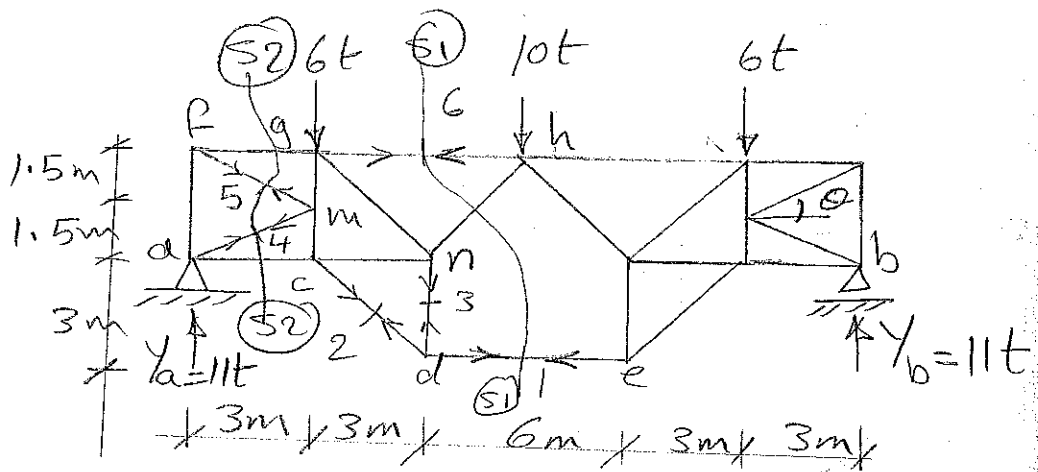
$$M_e = 18 \times 2 - 10 \times 3 - 3.11 \times 4.5$$

$$= -8.0 \text{ mt}$$



Q2

$$\tan \theta = \frac{1}{2}$$



Member 1

$$\text{Sec S1-S1} - \sum M_{\text{right}} = 0$$

$$6F_1 + 6 \times 6 - 9 \times 11 = 0$$

$$\Rightarrow F_1 = 10.5 \text{ tens.}$$

Member 2: Joint d

$$\sum F_x = 0$$

$$\Rightarrow F_1 - F_2 \cos 45 = 0$$

$$\Rightarrow F_2 = \frac{F_1}{\cos 45} = 14.85 \text{ tens}$$

Member 3: Joint d

$$\sum F_y = 0$$

$$\Rightarrow F_2 \sin 45 + F_3 = 0$$

$$\Rightarrow F_3 = -F_2 \sin 45$$

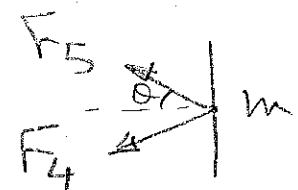
$$\Rightarrow F_3 = -10.5 \text{ comp.}$$

Members F_4 & F_5 :

$$\text{Joint m: } \sum F_x = 0$$

$$\Rightarrow F_4 \cos \theta + F_5 \cos \theta = 0$$

$$\Rightarrow F_4 = -F_5$$



$$\text{Sec S2-S2: } \sum F_y = 0$$

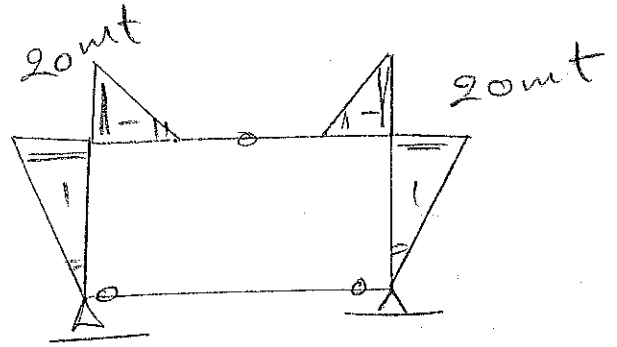
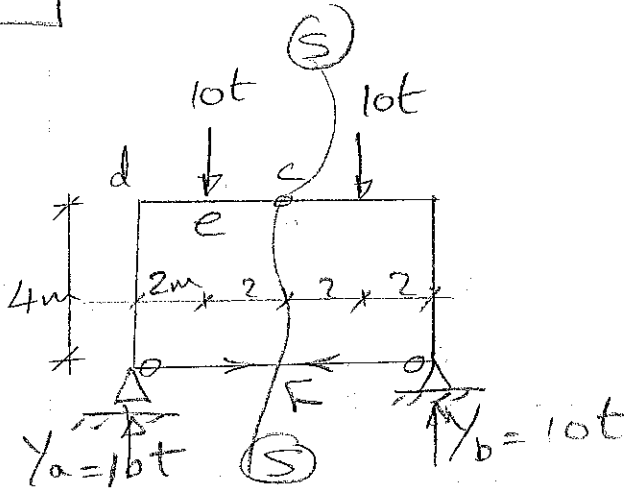
$$\Rightarrow 11 + F_4 \sin \theta - F_5 \sin \theta = 0 \Rightarrow 11 - 2F_5 \sin \theta = 0$$

$$\Rightarrow F_5 = 12.30 \text{ tens.}$$

Member 6: Sec S1-S1 - $\sum M_{\text{left}} = 0$

$$11 \times 6 + F_6 \times 3 - 6 \times 3 - F_1 \times 3 = 0 \Rightarrow F_6 = -5.5 \text{ comp.}$$

Q3



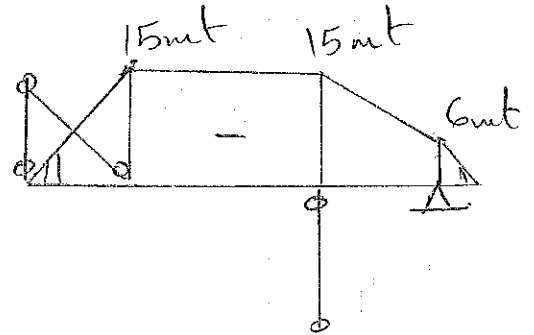
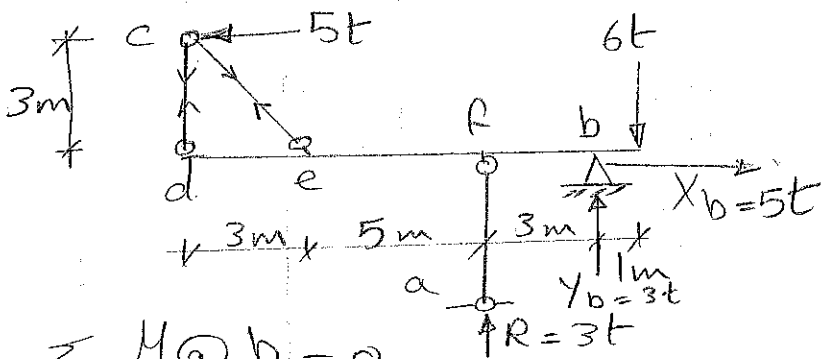
Sec S-S : $\sum M @ e \text{ right} = 0$

$$10 \times 4 - 10 \times 2 - 4F = 0$$

$$\Rightarrow F = 5t \text{ tens.}$$

$$M_d = -F \times 4 = -20mt$$

$$M_e = 10 \times 2 - F \times 4 = 0$$



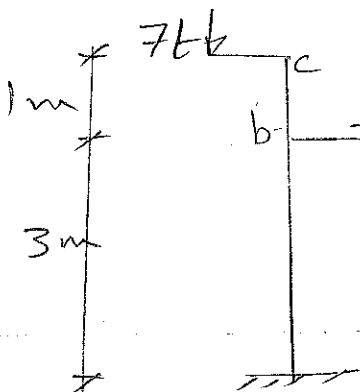
$$\sum M @ b = 0 \Rightarrow 5 \times 3 - 3R - 6 \times 1 = 0 \Rightarrow R = 3t \Rightarrow Y_b = 3t$$

Joint c : $\sum F_x = 0 \Rightarrow F_{c-e} \cos 45 - 5 = 0 \Rightarrow F_{c-e} = 7.07t$

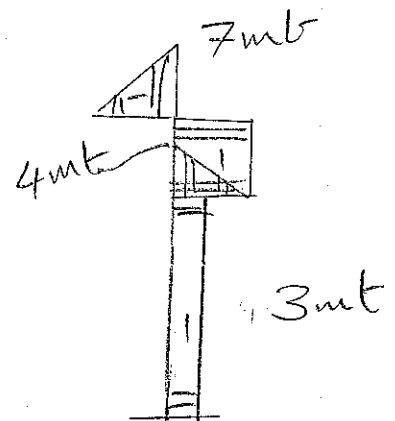
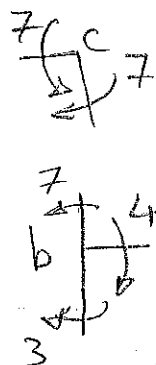
$\sum F_y = 0 \Rightarrow F_{c-d} + F_{c-d} \sin 45 = 0 \Rightarrow F_{c-d} = 5t$

$$M_e = 3 \times 5 + 3 \times 8 - 6 \times 9 = -15t$$

$$M_f = -6 \times 4 + 3 \times 3 = -15t$$



$$M_c = 7 \times 1$$

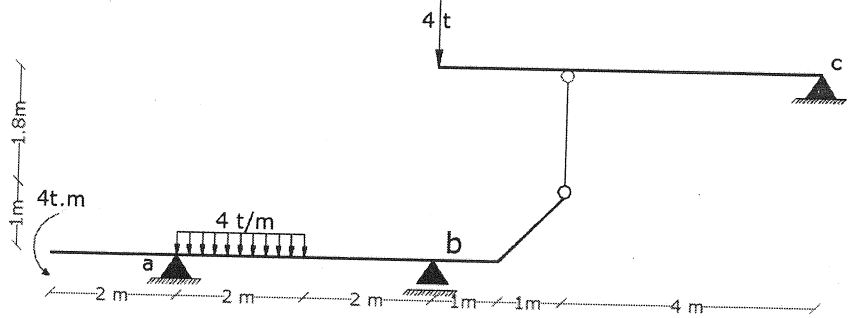




*** The exam consists of five questions in two pages attempt all.

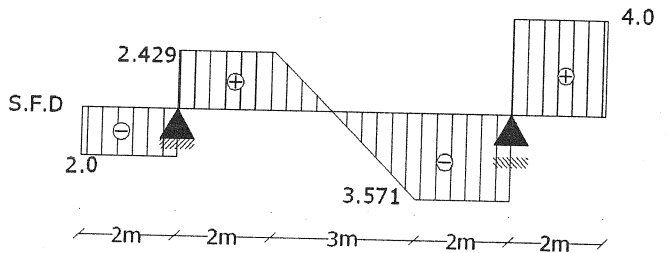
Question (1): a2, b2, c1, c2 (11 Marks)

Draw the straining action diagrams for the given beam.



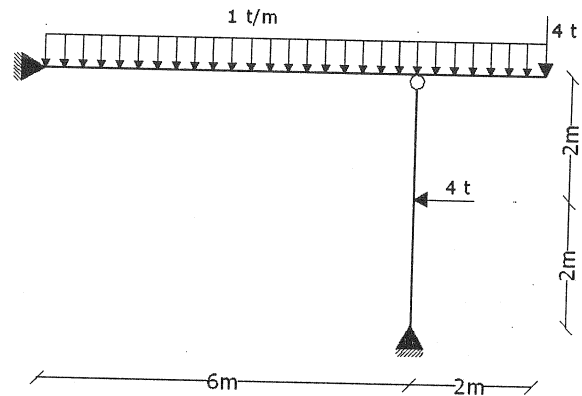
Question (2): a2, b2, c1, c2, d1 (6 Marks)

For the shown shear force diagram deduce the corresponding B.M.D.

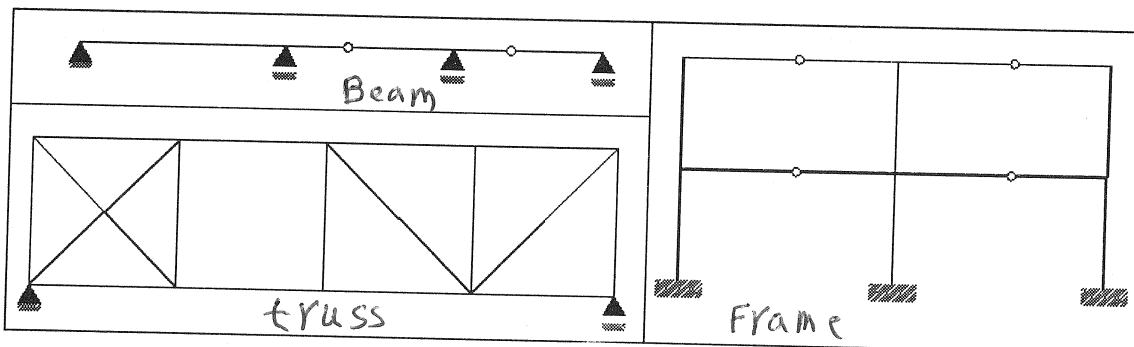


Question (3): a2, b2, c1, c2 (11 Marks)

Draw the straining action Diagrams for the shown frame.

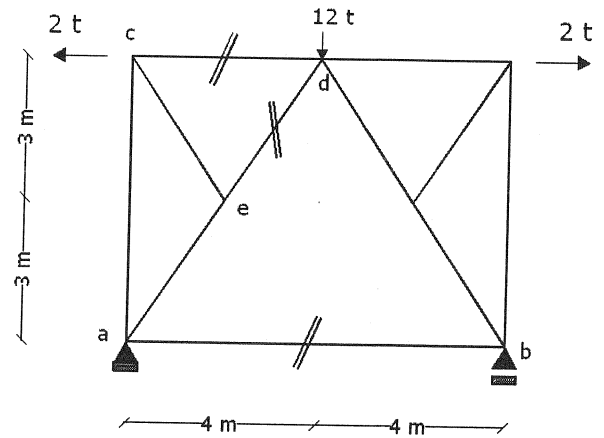


Question (4): a1, b1, d1, d2 (6 Marks) Discuss the stability and determinacy of the shown structures:



Question (5): a1, a2, b2, c1, c2 (9 Marks)

For the shown truss determine the force in the market members.

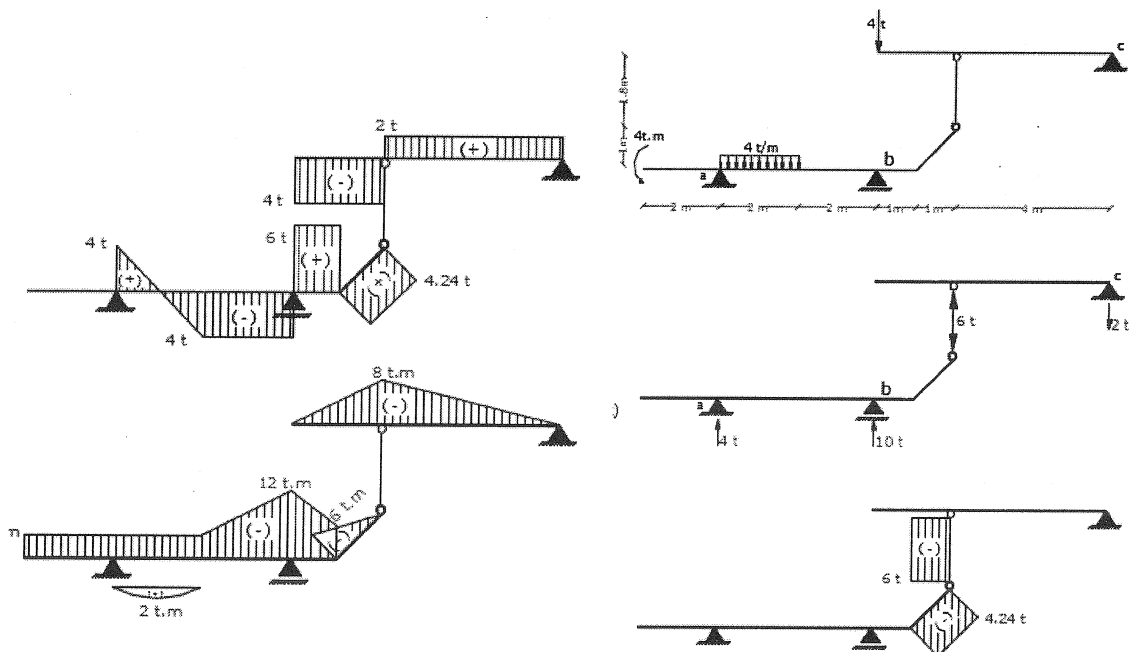




*** The exam consists of five questions in two pages attempt all.

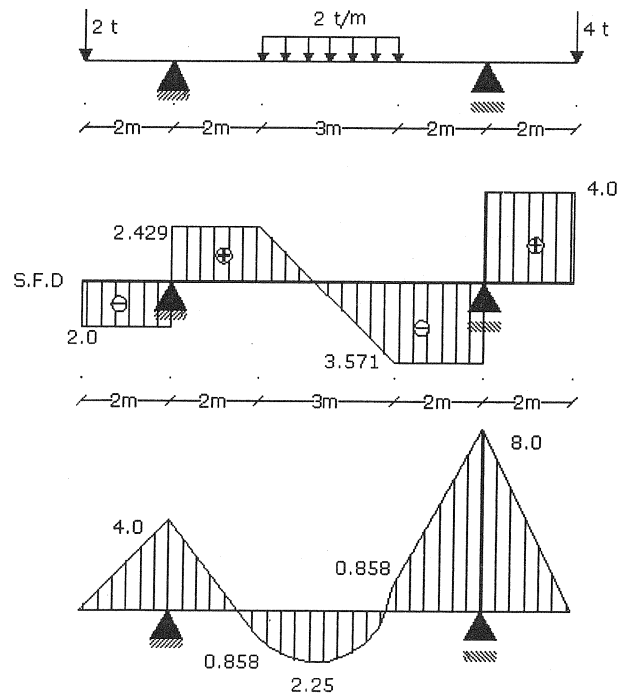
Question (1): (11 Marks)

Draw the straining action diagrams for the given beam.



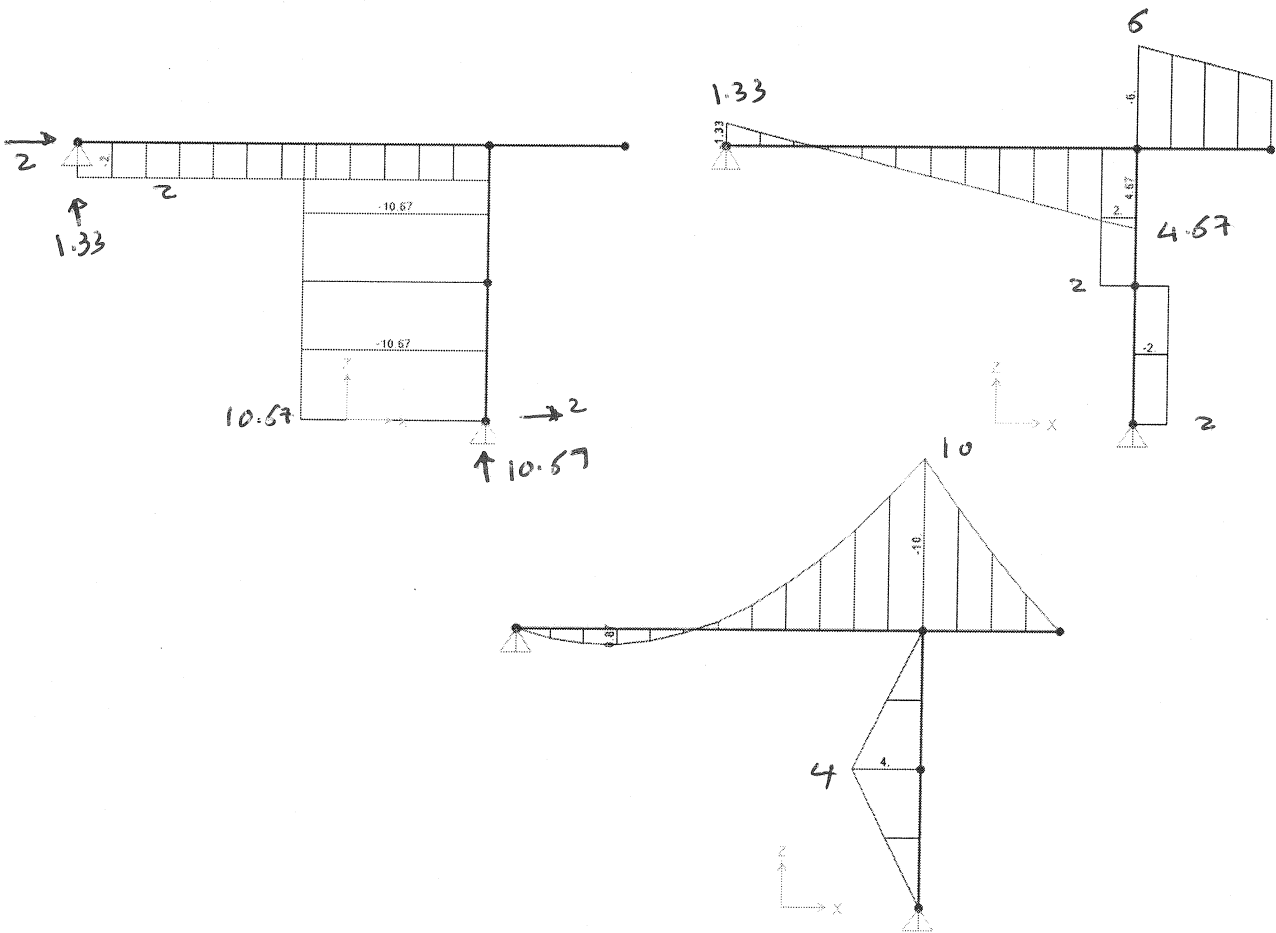
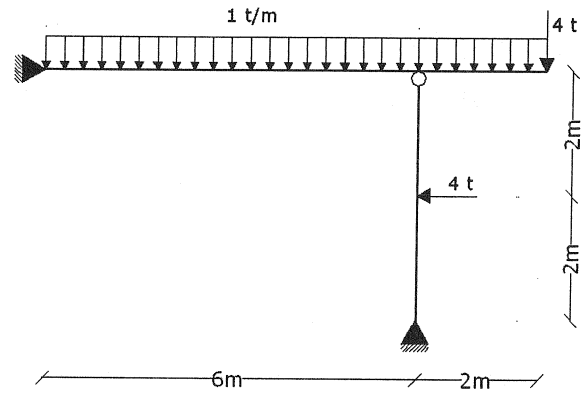
Question (2): (6 Marks)

For the shown shear force diagram deduce the corresponding bending moment diagram. (3 marks Loads + 3 B.M.D)



Question (3): (11 Marks)

Draw the straining action Diagrams for the shown frame.



QUESTION (4) : 6

For the beam: $(r, 3 + c)$

$$r=5, C=2 \quad 5 = 2+3$$

∴ This beam is statically determinate.

For the Frame: $(3m + r, 3j + c)$

$$m=14, r=9, C=4, J=13 \quad (3)(14) + 9 > (3)(13) + 4$$

∴ This frame is statically indeterminate (8th degree)

For the Truss: $(m + r, 2j)$

∴ This truss is geometric unstable (since the second panel has not bracing)

QUESTION (5) : 9

$$Y_a = Y_b = 6t \text{ upward}$$

Cut the structure into two parts.

For the left part:

$$\sum M_a = 0$$

$$0 = (2)(6) - F_{cd} (6)$$

$$\therefore F_{cd} = 2t \text{ tension}$$

$$\sum M_d = 0$$

$$0 = (4)(6) - F_{ab} (6) \quad \therefore F_{ab} = 4t \text{ tension}$$

$$\sum Y = 0$$

$$0 = F_{ed} (\sin \theta) + 6 \quad \therefore F_{ed} = 7.21t \text{ compression}$$

